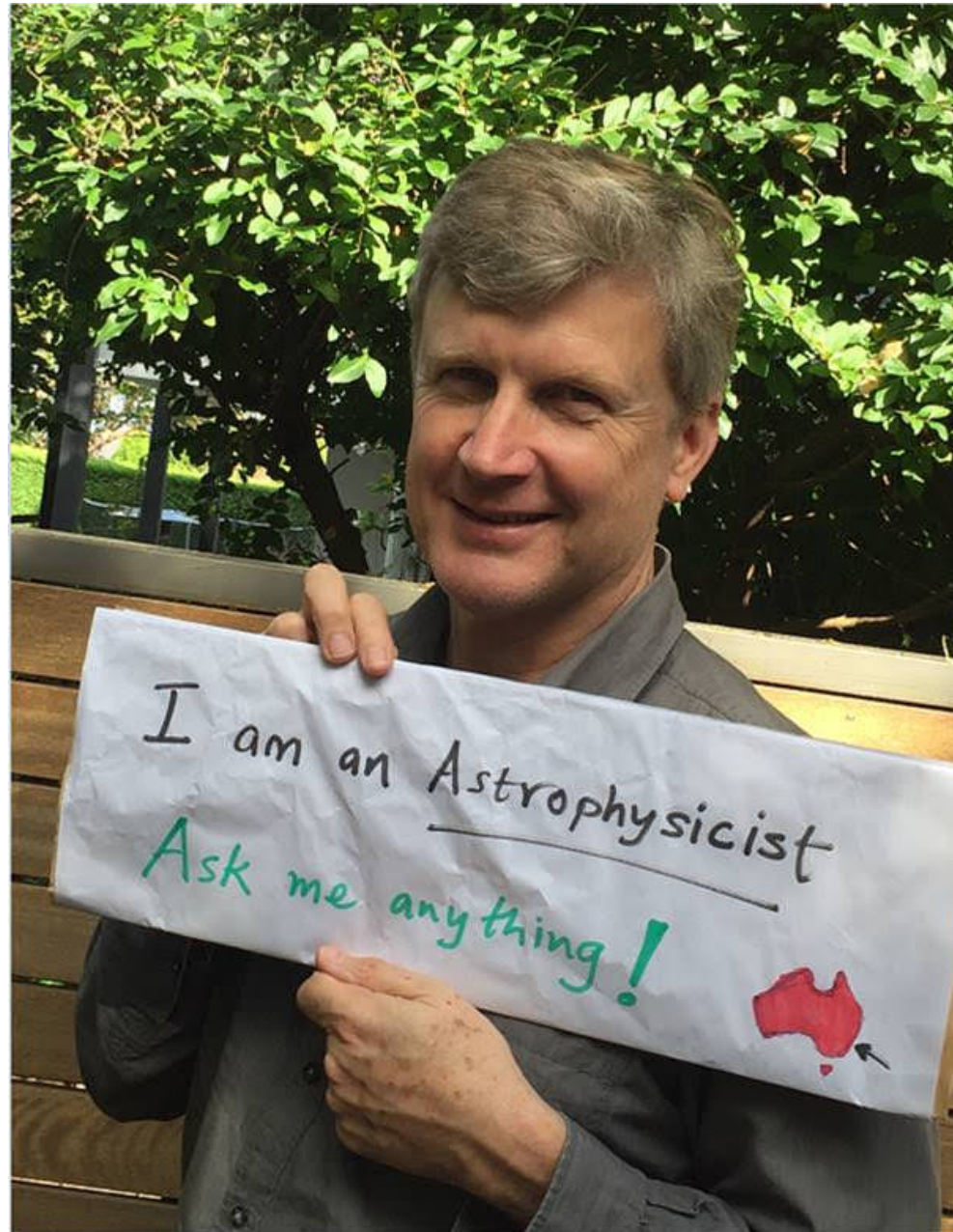


# Stellar chemistry: The way forward

1 H																	2 He
3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba	71 Lu	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra	103 Lr	104 Ku	105 Ha	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Uub	113 Uut	114 Uuq	115 Uup	116 Uuh	117 Uus	118 Uuo
		57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb		
		89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No		

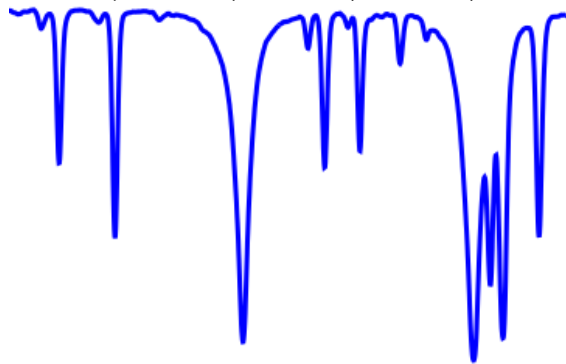
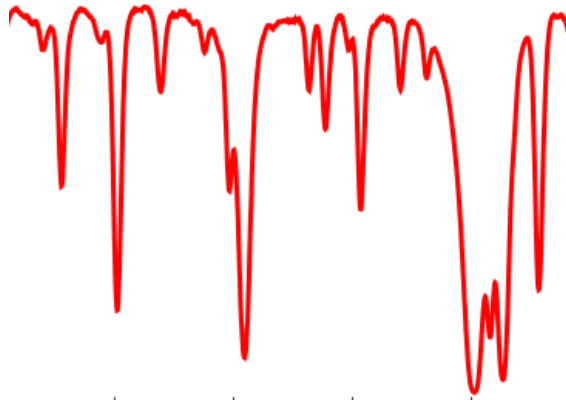
# Happy [REDACTED] birthday Joss!

---



# Stellar spectroscopy

---

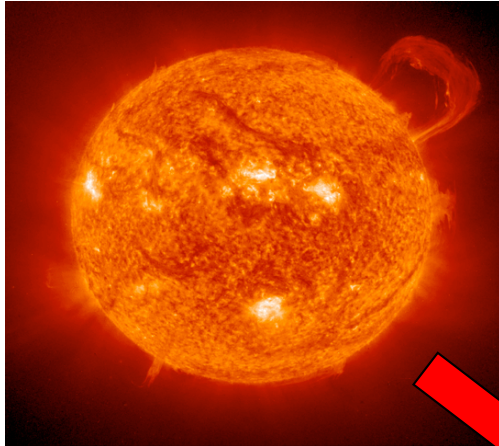


Temperature  
Radius  
Mass  
Chemistry  
Age  
Rotation  
Magnetic  
fields  
etc

Stellar Atmosphere  
Magnetohydrodynamics  
Radiative transfer  
Atomic physics

Optimal solution  
Robustness  
Speed

# Stellar analysis



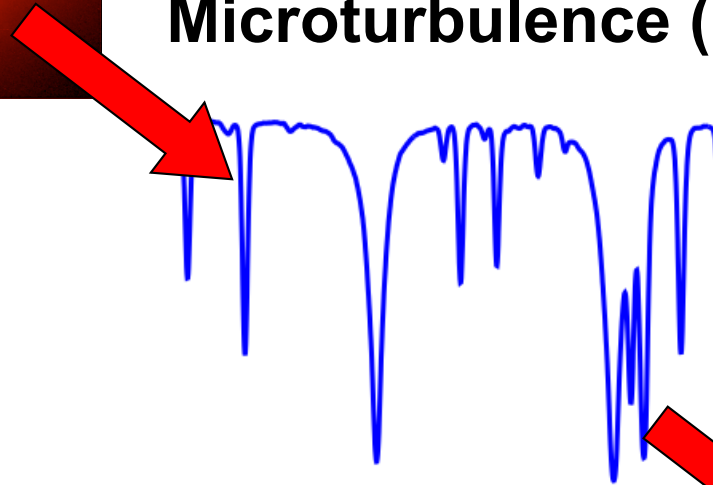
## Stellar atmospheres & parameters

Effective temperature  $T_{\text{eff}}$

Surface gravity  $\log g$

Metallicity  $[\text{Fe}/\text{H}]$

Microturbulence (1D)



## Radiative transfer:

LTE vs non-LTE

1D vs 3D

## Stellar abundances:

$\log \epsilon(X)$ ,  $[\text{X}/\text{H}]$

Uncertainties

Large stellar surveys

Auxiliary information

										Hydrogen		Helium	
										Li		Be	
										Boron		Carbon	
										Nitrogen		Oxygen	
										Fluorine		Neon	
										Sodium		Magnesium	
										Aluminum		Silicon	
										Phosphorus		Sulfur	
										Chlorine		Argon	
										Potassium		Calcium	
										Scandium		Titanium	
										Vanadium		Chromium	
										Manganese		Iron	
										Cobalt		Nickel	
										Copper		Zinc	
										Gallium		Germanium	
										Arsenic		Selenium	
										Bromine		Krypton	
										Rubidium		Strontium	
										Yttrium		Zirconium	
										Niobium		Molybdenum	
										Technetium		Ruthenium	
										Rhodium		Palladium	
										Silver		Cadmium	
										Indium		Tin	
										Antimony		Tellurium	
										Bismuth		Polonium	
										Thallium		Lead	
										Mercury		Thoron	
										Thallium		Bismuth	
										Polonium		Astatine	
										Francium		Radium	
										Actinium		Thorium	
										Protactinium		Uranium	
										Neptunium		Plutonium	
										Americium		Curium	
										Berkelium		Californium	
										Einsteinium		Fermium	
										Mendelevium		Nobelium	
										Lawrencium		Rutherfordium	
										Dubnium		Seaborgium	
										Bohrium		Hassium	
										Meitnerium		Darmstadtium	
										Roentgenium		Copernicium	
										Nihonium		Flerovium	
										Tennessine		Oganesson	

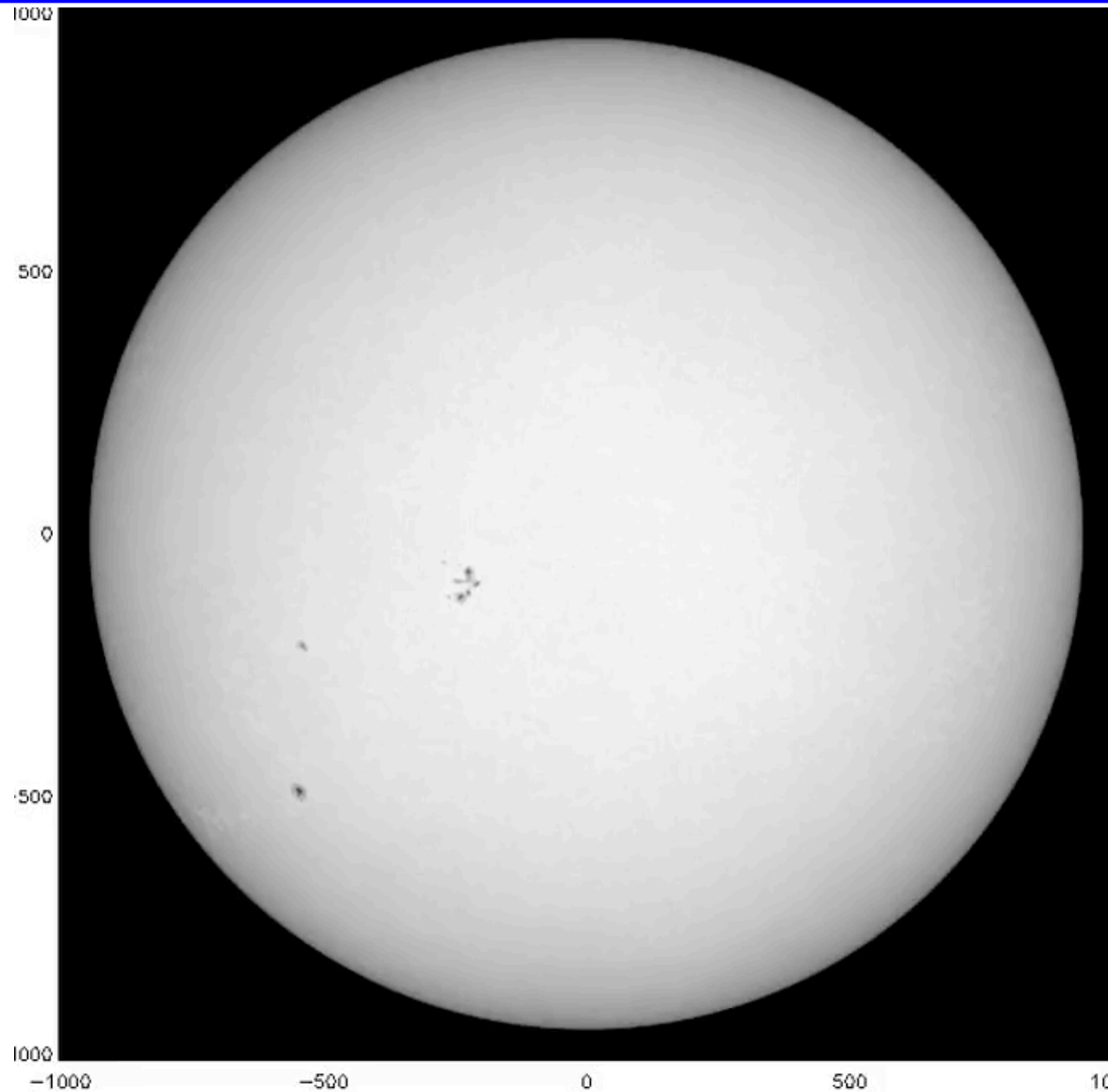
\* Lanthanide Series

Lanthanum	Cerium	Praseodymium	Neodymium	Promethium	Samarium	Europium	Gadolinium	Terbium	Dysprosium	Holmium	Erbium	Thulium	Ytterbium
57	58	59	60	61	62	63	64	65	66	67	68	69	70
138.91	140.12	140.91	144.24	145	150.36	151.96	157.25	158.93	162.50	164.93	167.26	168.93	173.04
Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No
89	90	91	92	93	94	95	96	97	98	99	100	101	102
227	232.04	231.04	238.03	237	244	243	247	247	251	252	252	258	259

\*\* Actinide Series

# Stellar surface convection

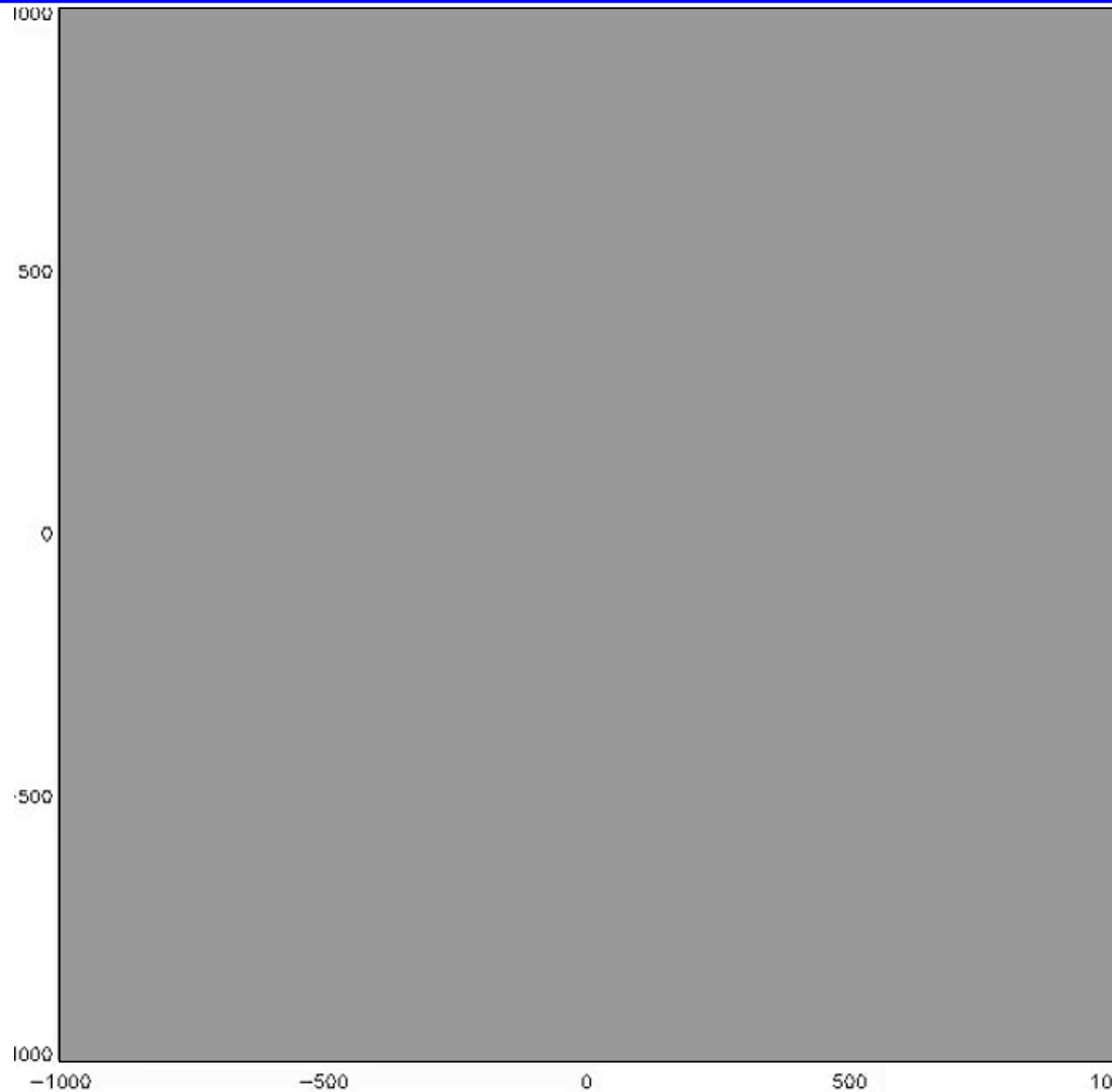
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© Mats Carlsson (Oslo)

# Stellar surface convection

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© Mats Carlsson (Oslo)

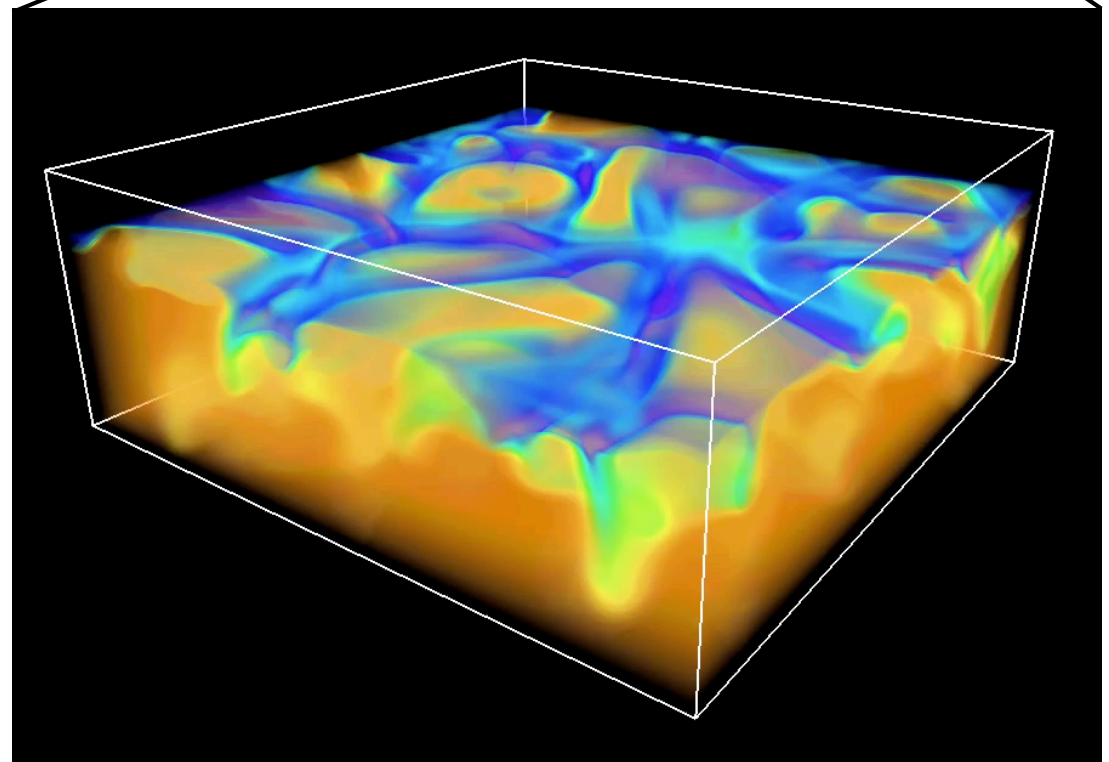
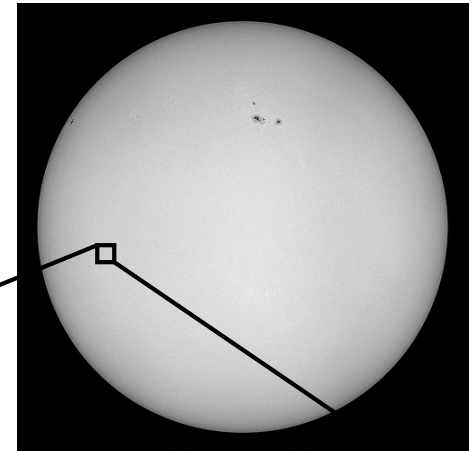
# 3D stellar atmosphere models

---

## Ingredients:

- Radiative-hydrodynamical
- Time-dependent
- 3-dimensional
- **Simplified radiative transfer**

Essentially parameter free



## For the aficionados:

Stagger-code (Nordlund et al.)

MHD EoS (Mihalas et al.)

Opacities (Gustafsson et al.)

Opacity binning

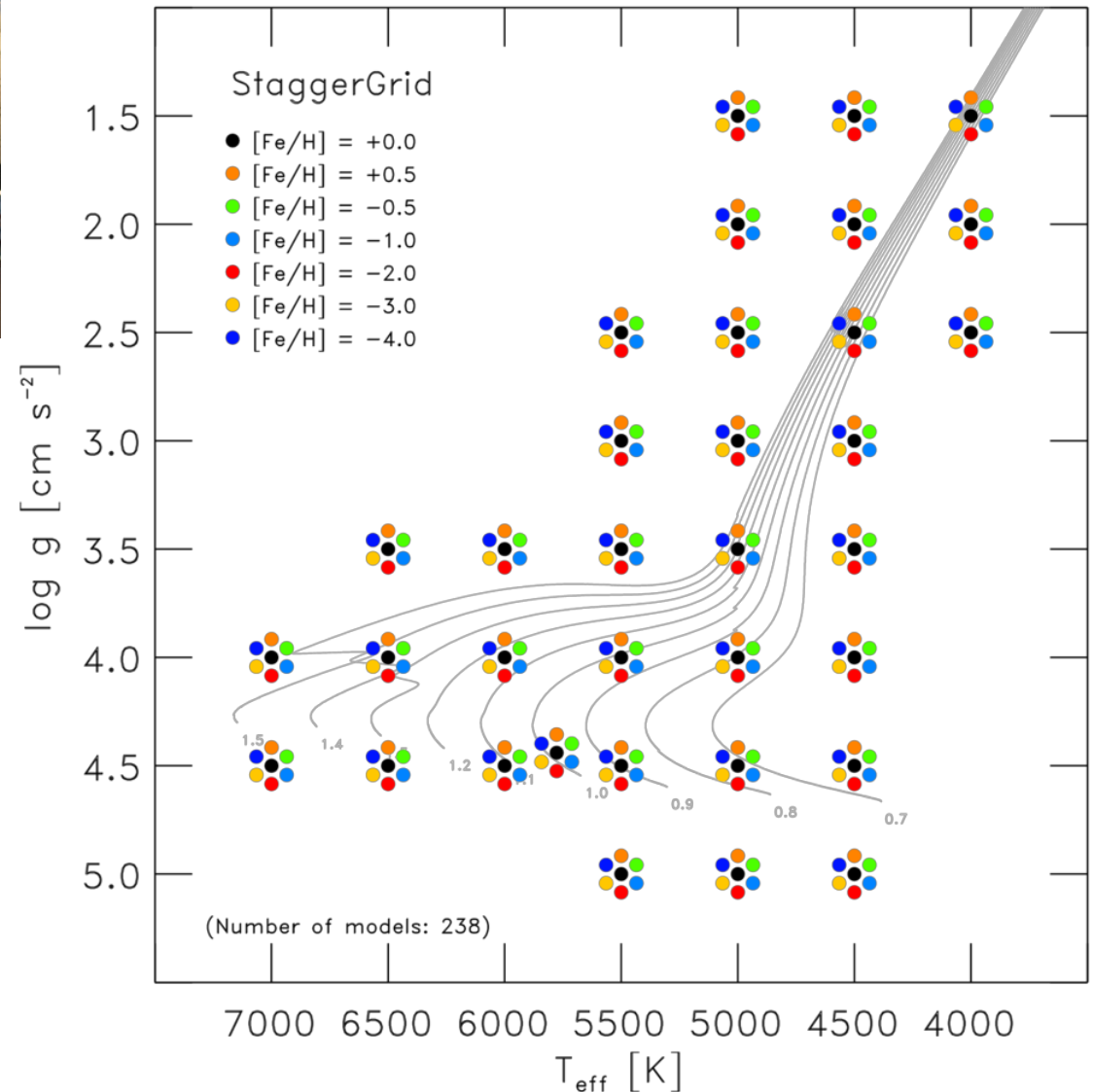
# Stagger-grid of 3D stellar models



**Magic et al. 2013;**  
**Collet et al. 2018:**

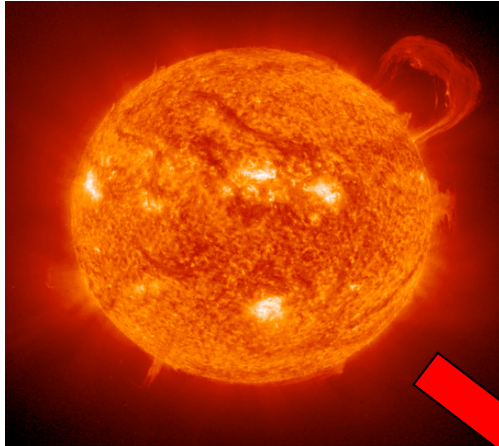
**3D and <3D> models  
and fluxes public:**

- **Stellar spectroscopy**
- **Stellar evolution**
- **Asteroseismology**
- **Exoplanet searches**
- **Etc, etc**





# Stellar analysis



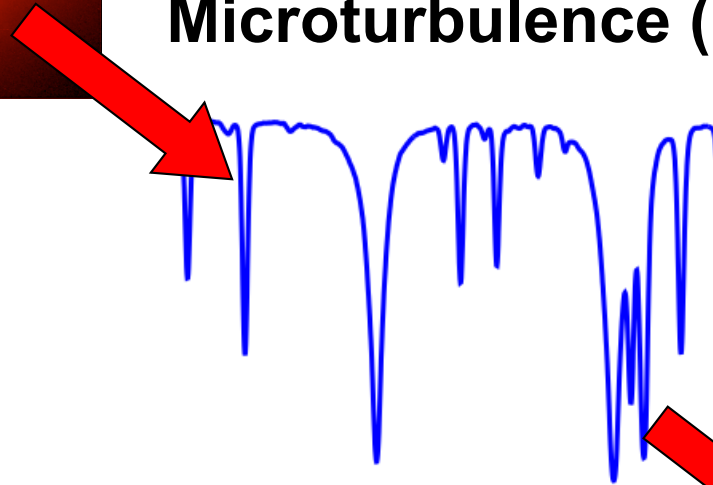
## Stellar atmospheres & parameters

Effective temperature  $T_{\text{eff}}$

Surface gravity  $\log g$

Metallicity  $[\text{Fe}/\text{H}]$

Microturbulence (1D)



## Radiative transfer:

LTE vs non-LTE

1D vs 3D

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Uncertainties

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										Bismuth		Polonium	
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										Francium		Radium	
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										Nihonium		Flerovium	
										Tennessine		Oganesson	

\* Lanthanide Series

La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb
138.91	140.12	140.91	144.24	144.91	150.36	151.96	157.25	158.93	162.50	164.93	167.26	168.93	173.04
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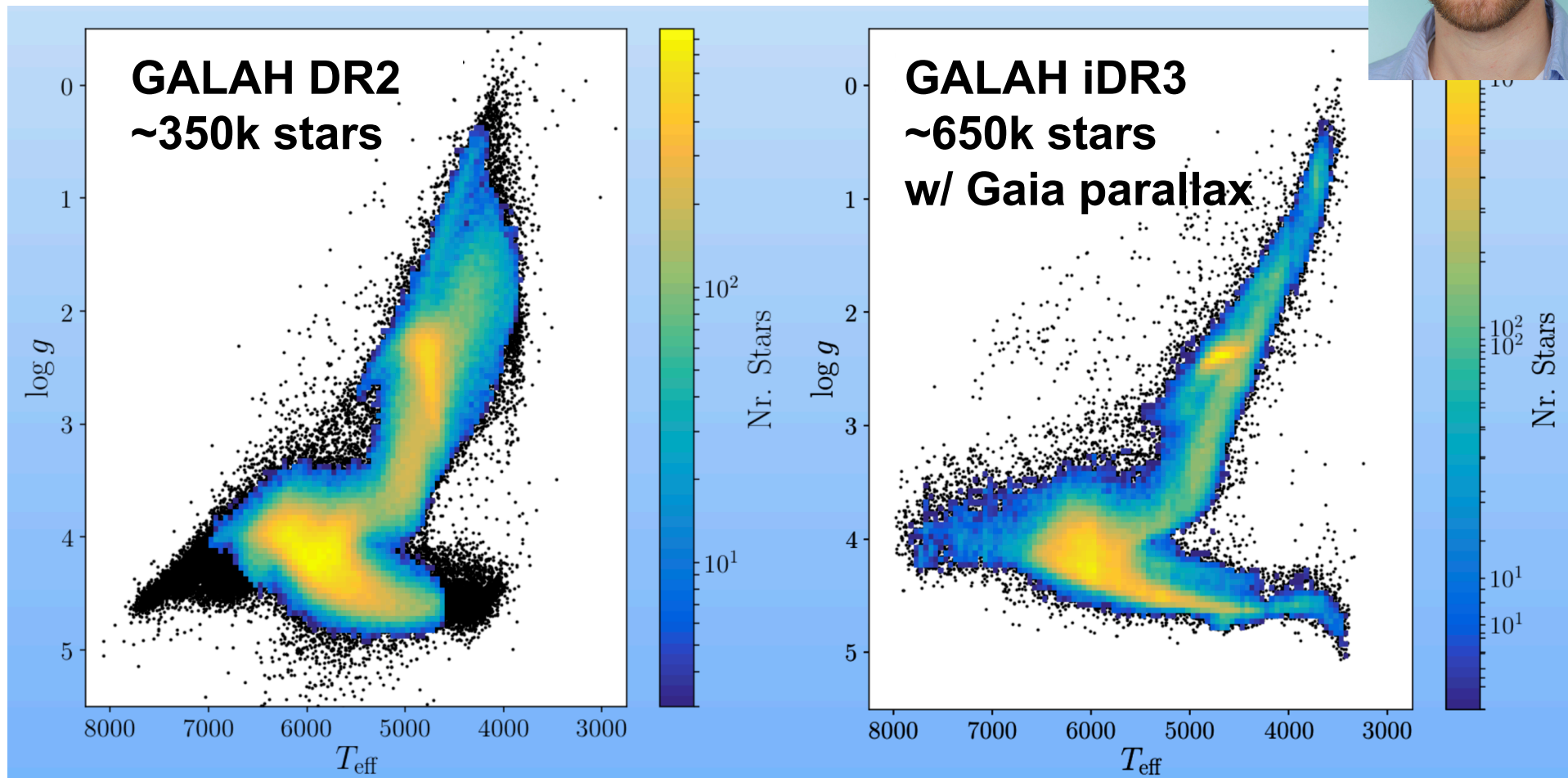
\*\* Actinide Series

# Surface gravity: Gaia revolution

$$\log \frac{g}{g_0} = 4 \log \frac{T_{eff}}{T_{eff,0}} + \log \frac{M}{M_0} + 2 \log \pi + 0.4(m_V + BC_V - A_V) + 0.10$$

Parallax

Buder et al. 2019:



# Effective temperature: Gaia

## Gaia BP/RP spectrophotometry

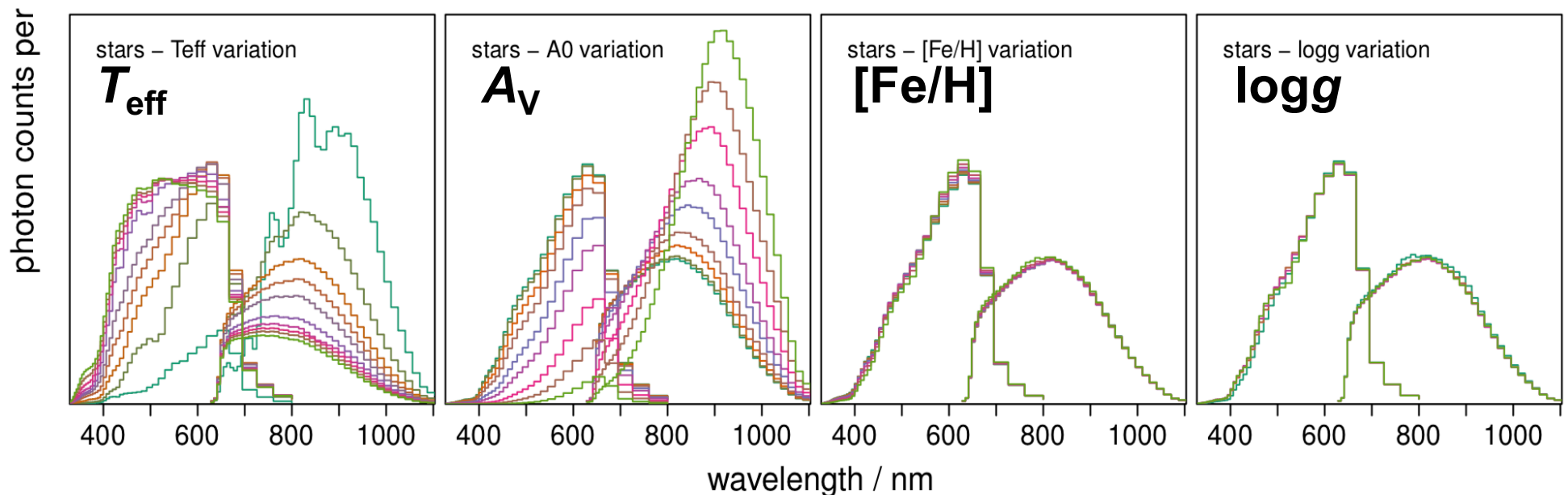
R~50, 330-1050nm

~10<sup>9</sup> stars with G<20

$\delta T_{\text{eff}} \sim 100\text{K}$ ,  $\delta \log g \sim 0.2$ ,  $\delta [\text{Fe}/\text{H}] \sim 0.2$ ,  $\delta A_V \sim 0.1\text{mag}$

Gaia DR3: end of 2021 (incl. BP/RP & RVS spectra)

## Bailer-Jones et al. 2013



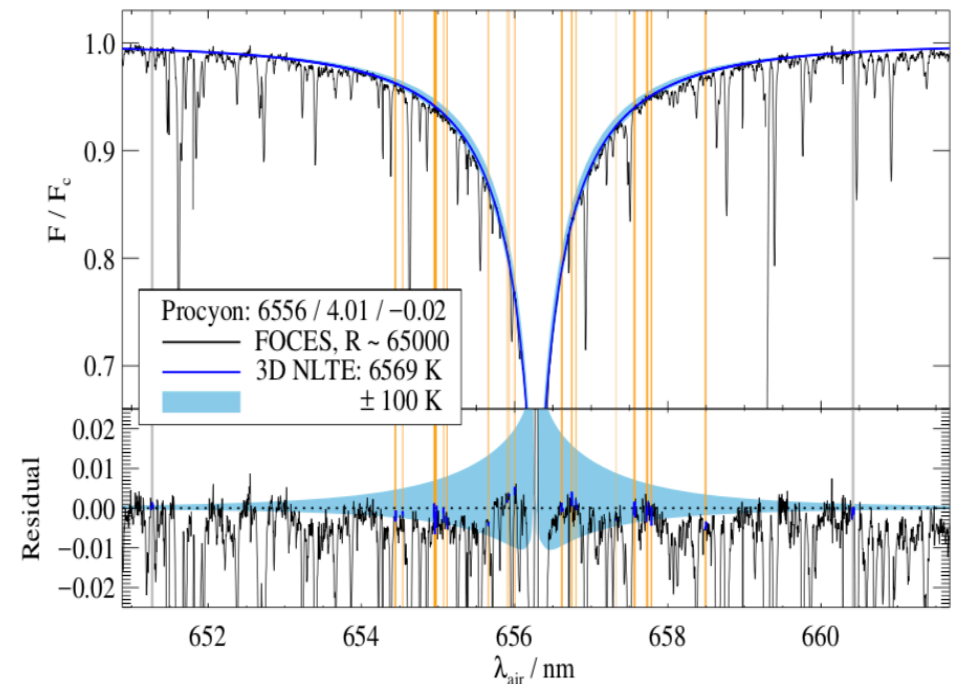
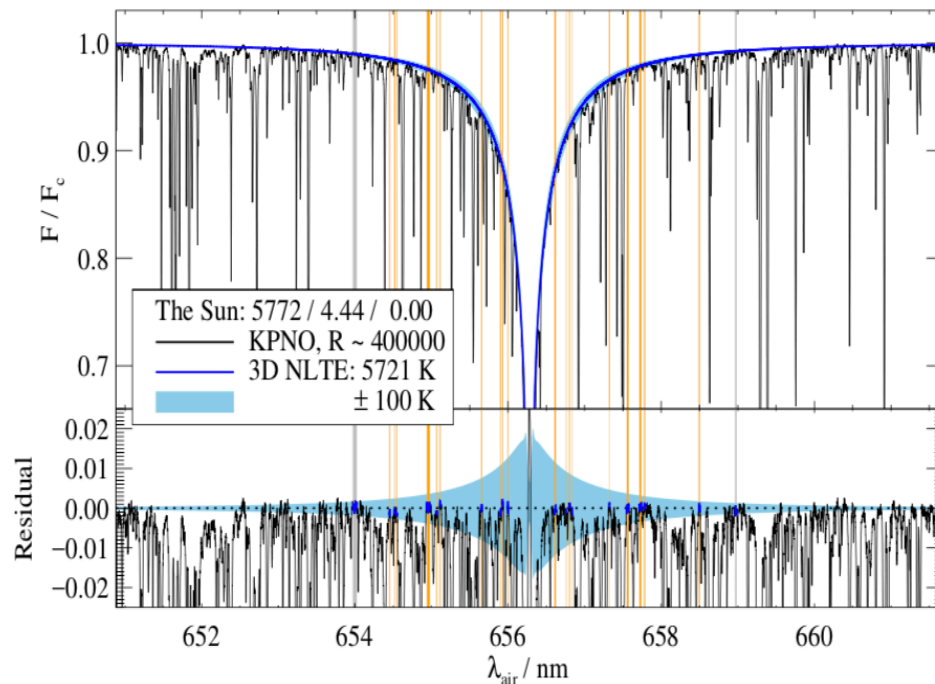
# Effective temperature: H lines

Very  $T_{\text{eff}}$  sensitive but sophisticated modelling needed:

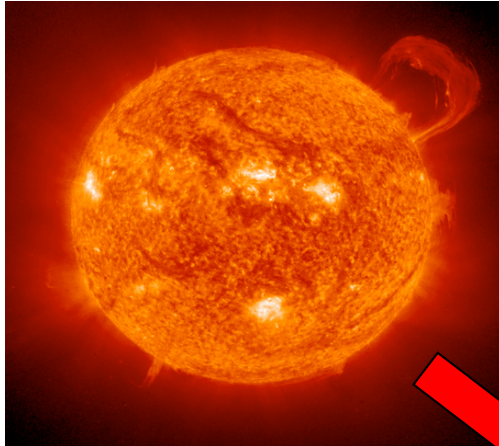
**3D:** Realistic atmospheric temperature structure

**Non-LTE:** Small effects flux variations  $\Rightarrow$  large  $T_{\text{eff}}$  effect

**Amarsi et al. 2017:** grid of 3D non-LTE H line profiles



# Stellar analysis



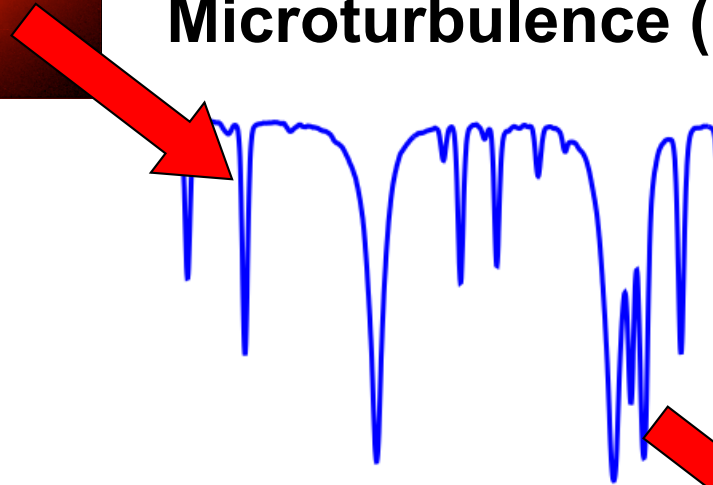
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Microturbulence (1D)



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										Aluminum		Silicon		Phosphorus		Sulfur		Chlorine		Argon																									
										K		Ca		Scandium		Titanium		Vanadium		Chromium		Manganese		Iron		Cobalt		Nickel		Copper		Zinc		Gallium		Germanium		Arsenic		Selenium		Bromine		Krypton	
										Rb		Sr		Y		Zr		Nb		Mo		Tc		Ru		Rh		Pd		Ag		Cd		In		Sn		Sb		Te		I		Xe	
										Cs		Ba		* Lu		Hf		Ta		W		Re		Os		Ir		Pt		Au		Hg		Tl		Pb		Bi		Po		At		Rn	
										Fr		Ra		* * Lr		Rf		Db		Sg		Bh		Hs		Mt		Uun		Uuu		Uub		Uuq											

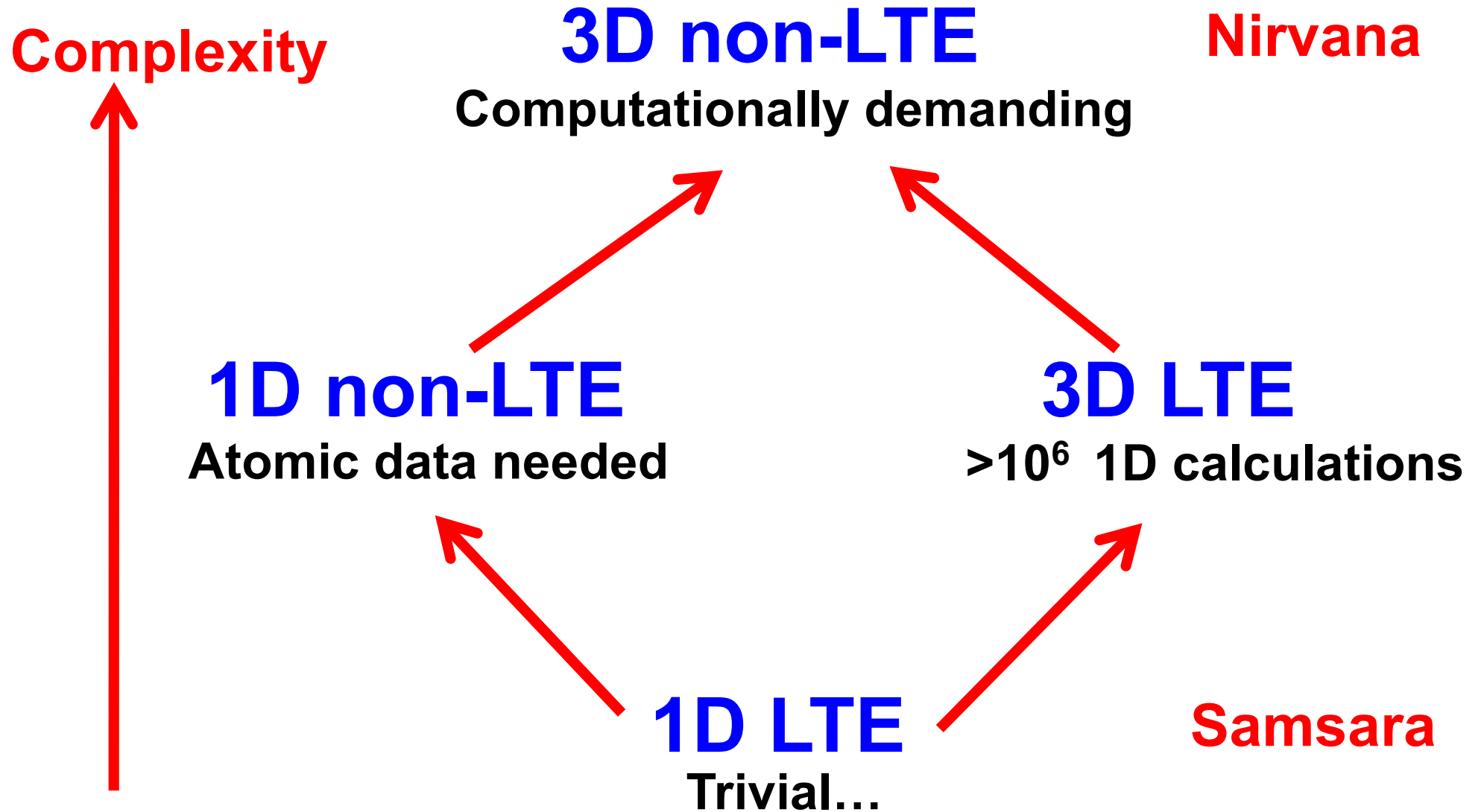
\* Lanthanide Series

La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb
138.91	140.12	140.91	144.24	145	150.36	151.96	157.25	158.93	162.50	164.93	167.26	168.93	173.04
Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No
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\*\* Actinide Series

# Radiative transfer

---



**LTE:** Maxwell + Boltzmann + Saha + Planck

# Non-LTE radiative transfer

Level populations not determined by Saha & Boltzmann

Radiative transfer eq.

$$\frac{dI_\nu}{d\tau_\nu} = S_\nu - I_\nu$$

Source function:

$$S_\nu^l = (1 - \varepsilon_\nu) J_\nu + \varepsilon_\nu B_\nu$$

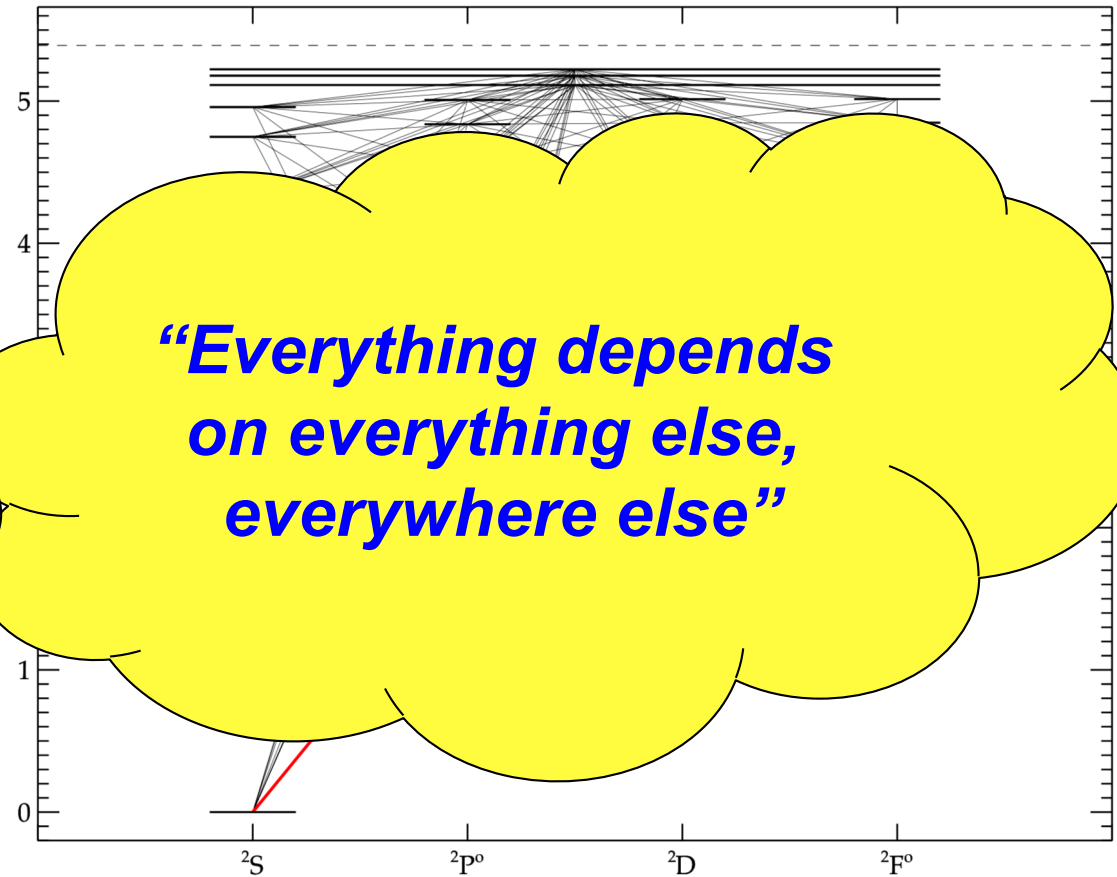
Level rate equations:

$$\frac{dn_i}{dt} = \sum_{j \neq i}^N n_j P_{ji} - n_i \sum_{j \neq i}^N P_{ij} = 0$$

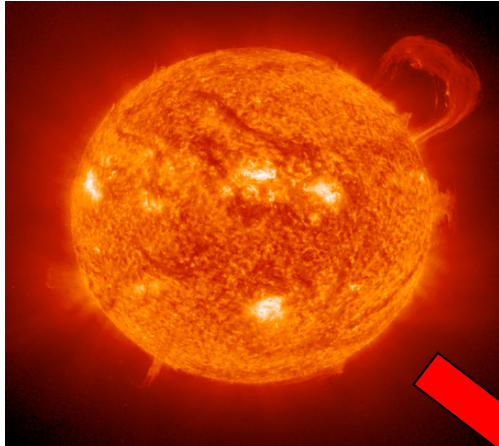
Collisional & radiative rates:

$$P_{ij} = A_{ij} + B_{ij} \bar{J}_{\nu_0} + C_{ij}$$

Lithium term diagram



# Stellar analysis



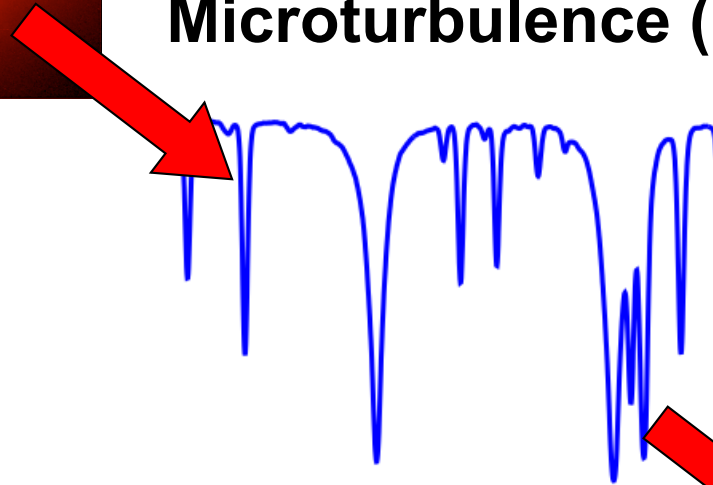
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										Al		Si	
										P		S	
										Cl		Ar	
										K		Ca	
										Sc		Ti	
										V		Cr	
										Mn		Fe	
										Co		Ni	
										Cu		Zn	
										Ga		Ge	
										As		Se	
										Br		Kr	
										Rb		Sr	
										Y		Zr	
										Nb		Mo	
										Tc		Ru	
										Rh		Pd	
										Ag		Cd	
										In		Sn	
										Sb		Te	
										Bi		Po	
										At		Rn	
										Fr		Ra	
										Ac		Th	
										Pa		U	
										Np		Pu	
										Am		Cm	
										Bk		Cf	
										Es		Fm	
										Md		No	
										Lr		Rf	
										Db		Sg	
										Bh		Hs	
										Mt		Uun	
										Uuu		Uub	
										Uuq			

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La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb
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\*\* Actinide Series

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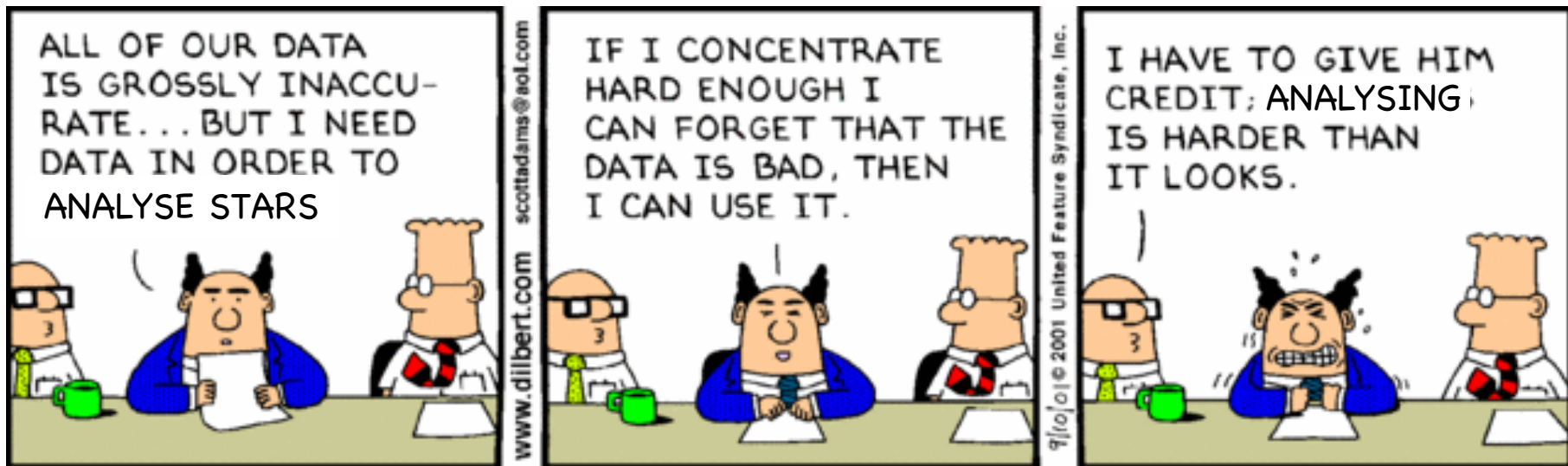
# Atomic data

---

**Huge amount of (uncertain) data needed in non-LTE:**

Transition probabilities, photo-ionisation cross-sections, collisional excitation/ionisation with H and  $e^-$ , charge transfer, pressure broadening, hyperfine splitting etc

⇒ **Support your local atomic physicist!**



# Differential stellar analysis

Extremely high precision (0.01 dex)  
for stars with similar parameters:

Melendez et al. 2009:

⇒ Signature of planet formation

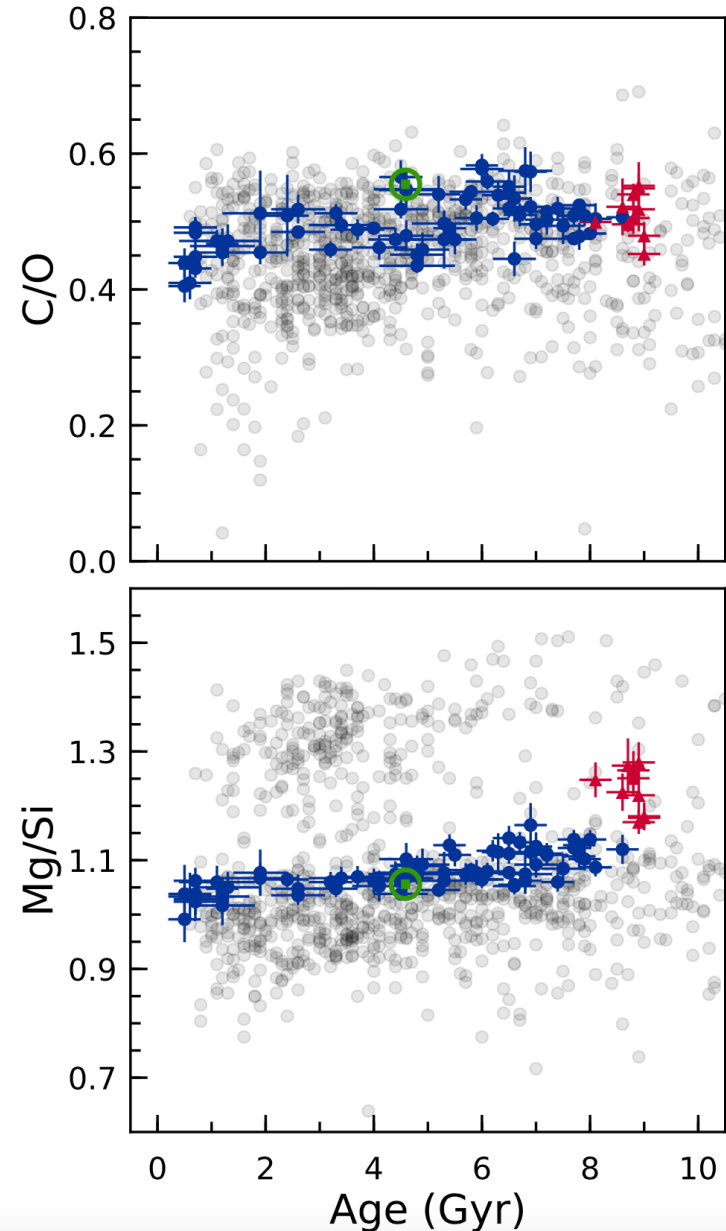
Bedell et al. 2018:

⇒ Chemical enrichment vs time

Reggiani et al. 2017:

⇒ Tiny abundance scatter in halo

Bedell et al. 2018



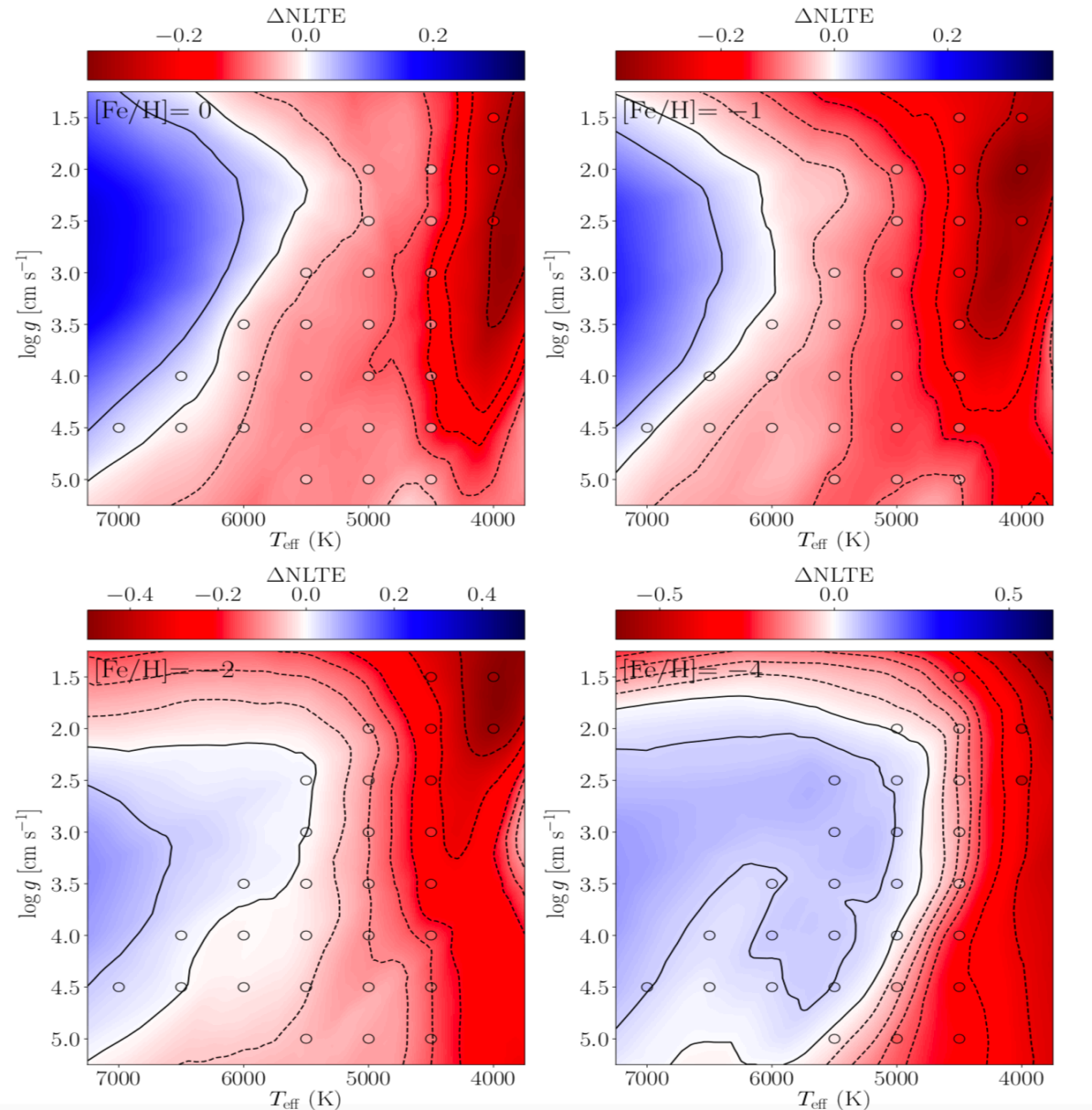
# 3D non-LTE line formation



**Wang et al. 2019:**  
**3D non-LTE for Li for**  
**FGK dwarfs/giants**  
**and Li abundances**

**Interpolation in parameters**  
**and abundances using**  
**neural networks (MLP)**  
**publicly available**

## 3D non-LTE – 1D LTE abundances

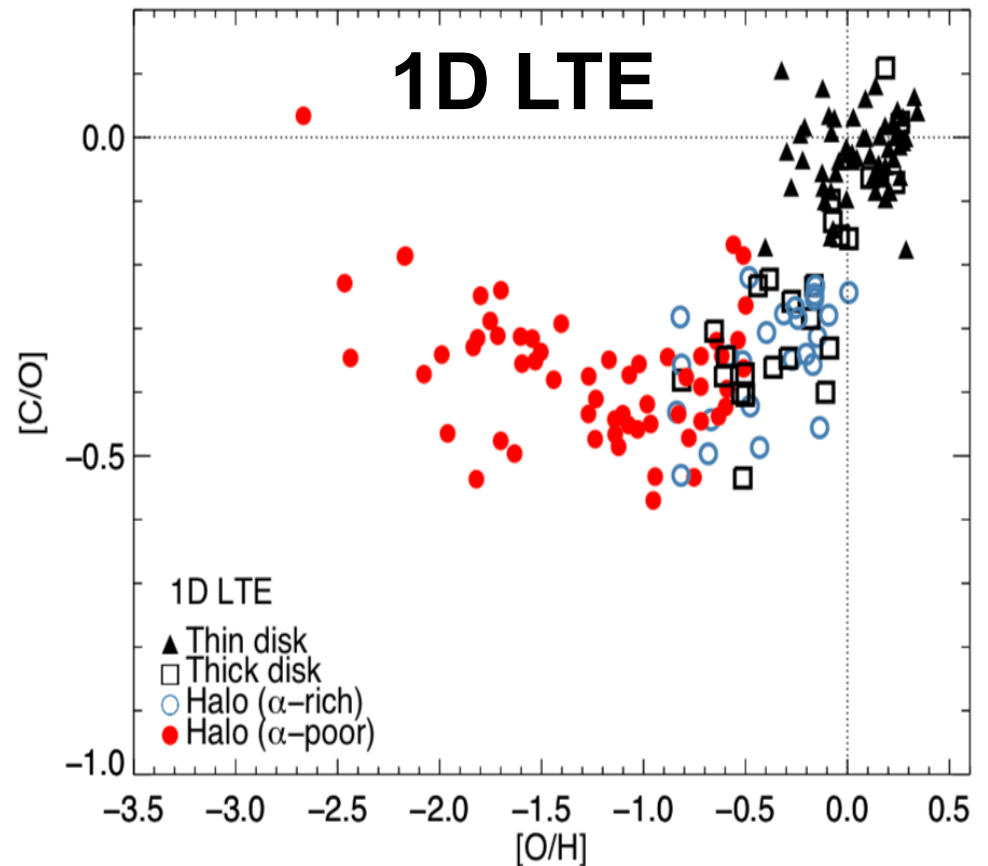
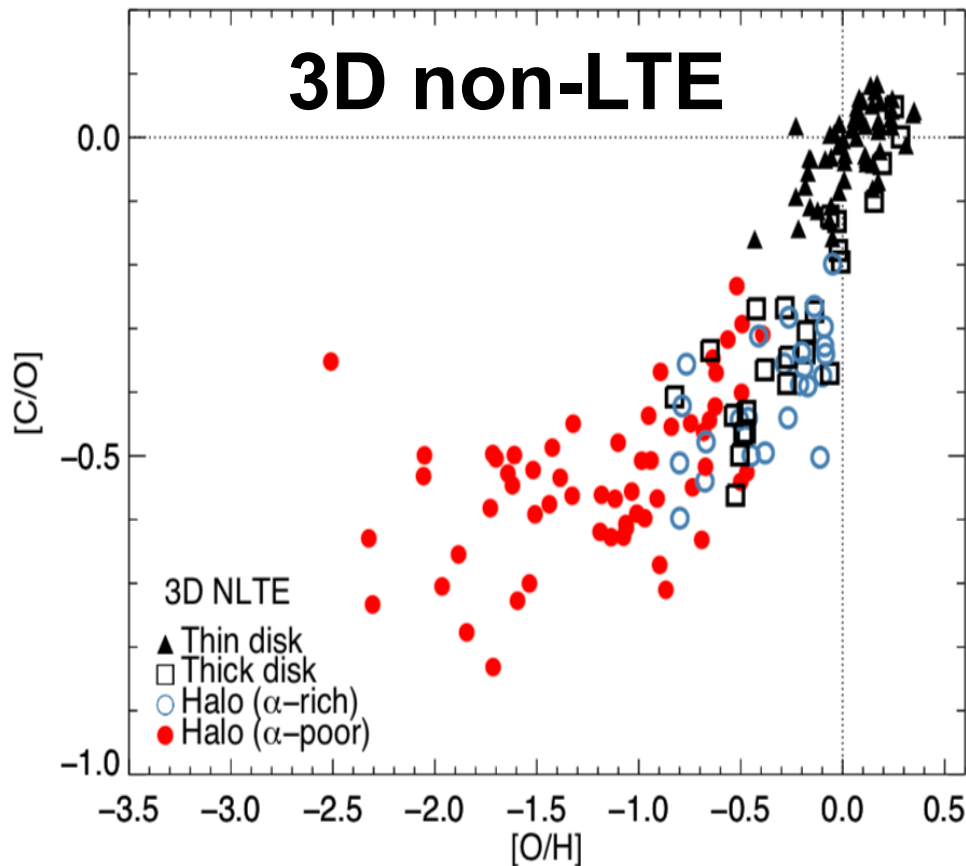


# Evolution of C and O

Amarsi et al. 2019a,b:

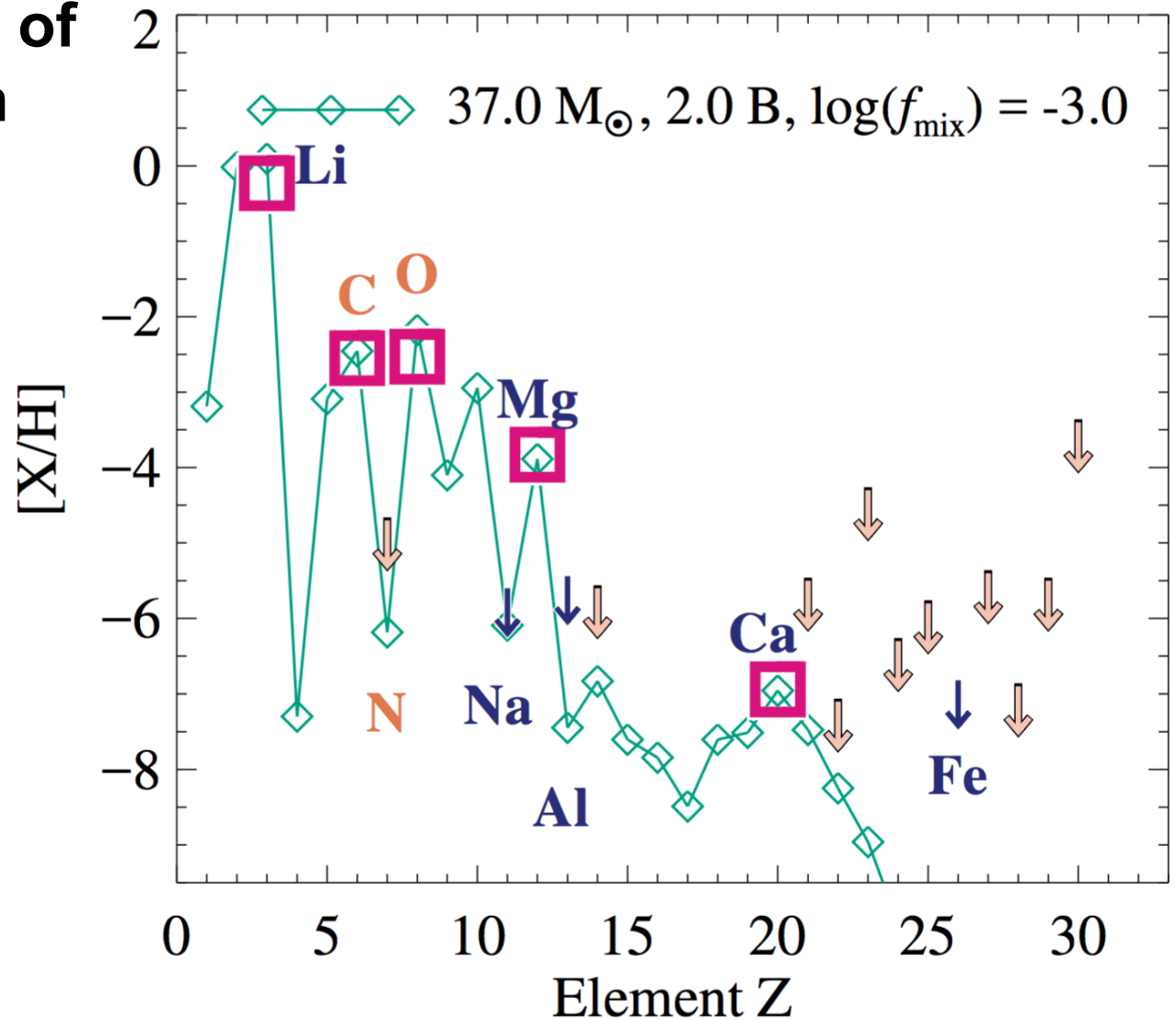
3D non-LTE line formation of C, O and Fe

⇒ No signature of Pop III nucleosynthesis



# First stars

**Nordlander et al. 2017:**  
3D non-LTE analysis of  
SMSS0313-6708 with  
[Fe/H] < -6.5  
Non-LTE abundance  
corrections > 0.5 dex  
for Mg, Al, Ca, Fe



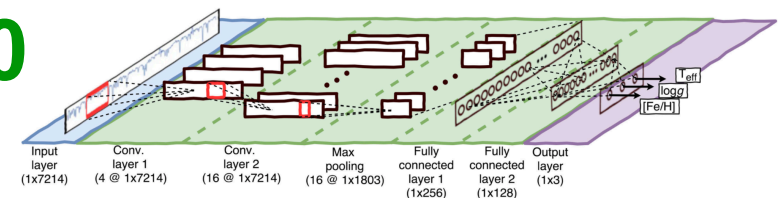
# How to analyse a million stars?

---

- **Automated**
- **Accurate**
- **Precise**
- **Fast**
- **Reliable**
- **Reproducible**

# Large spectroscopic surveys

- **Spectrum synthesis**
  - Automated, brute force
- **Grids of spectra**
  - **Recio-Blanco et al. 2006**
  - **Garcia Perez et al. 2016**
- **Data-driven analysis**
  - **Ness et al. 2015**
  - **Casey et al. 2017**
- **Neural networks**
  - **Bailer-Jones et al. 2000**
  - **Fabbro et al. 2017**



# Smart & sparse grids

Rectilinear grids very expensive for high dimensions:

$$N_{\text{models}} \propto (N_{\text{bin}})^{\text{dimensions}}$$

Ting et al. 2016;

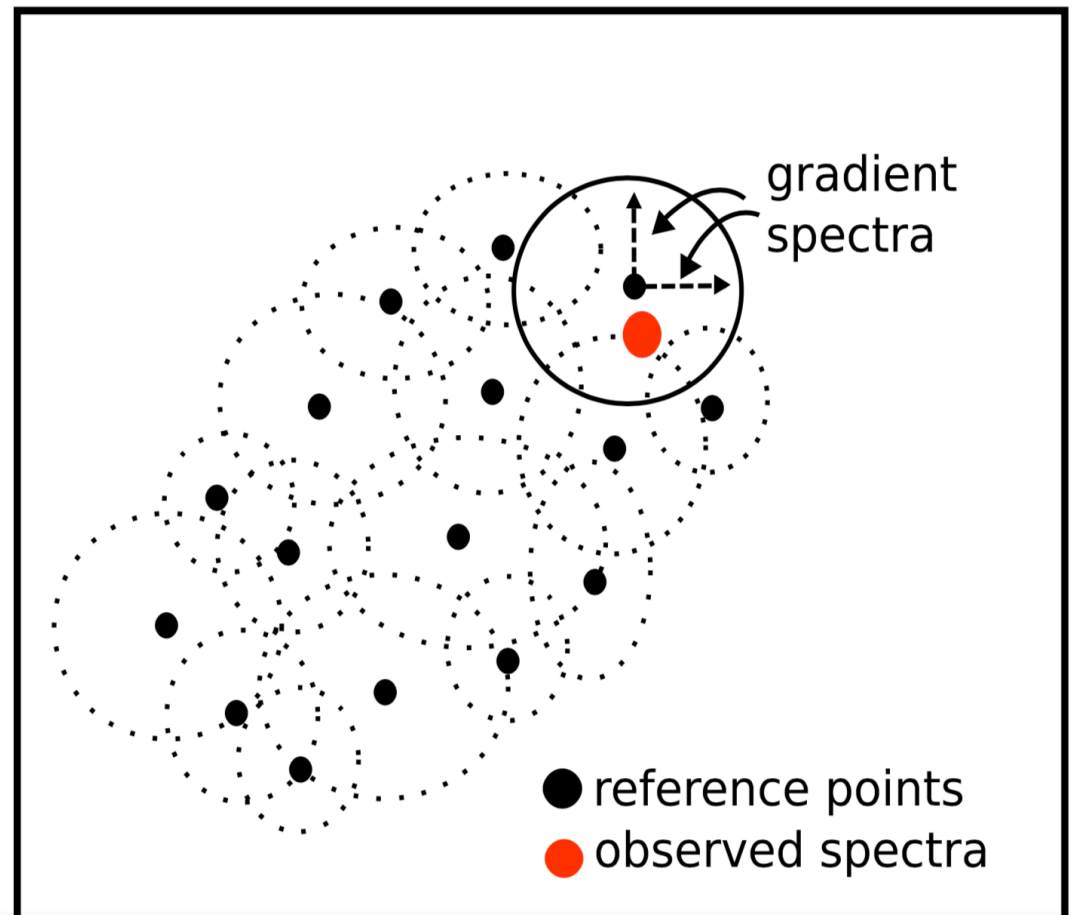
Rix et al. 2016:

Grid models only were needed combined with linear expansion of gradient spectra

$$N_{\text{models}} \propto \text{dimensions!}$$

$$N_{\text{models}} \sim 1000?$$

3D non-LTE grids with ~30 dimensions!





# Cannon: data-driven analysis

Ness et al. 2015:

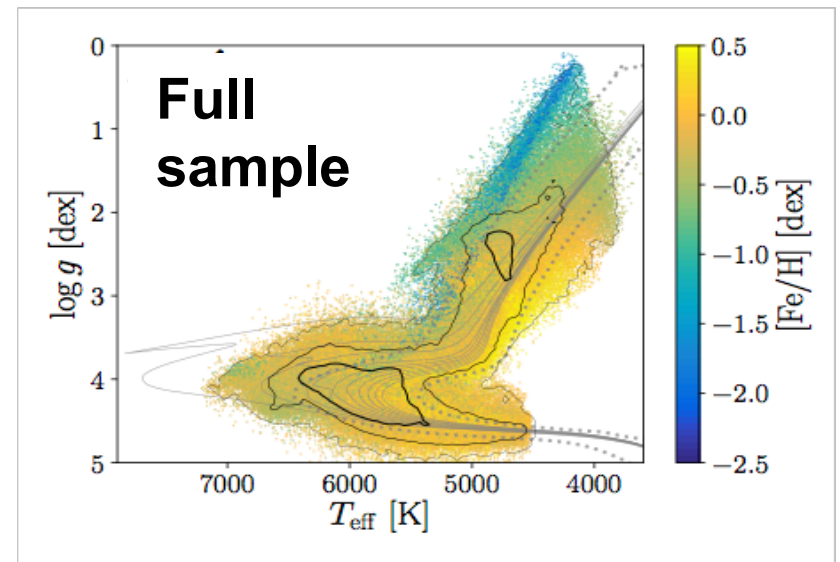
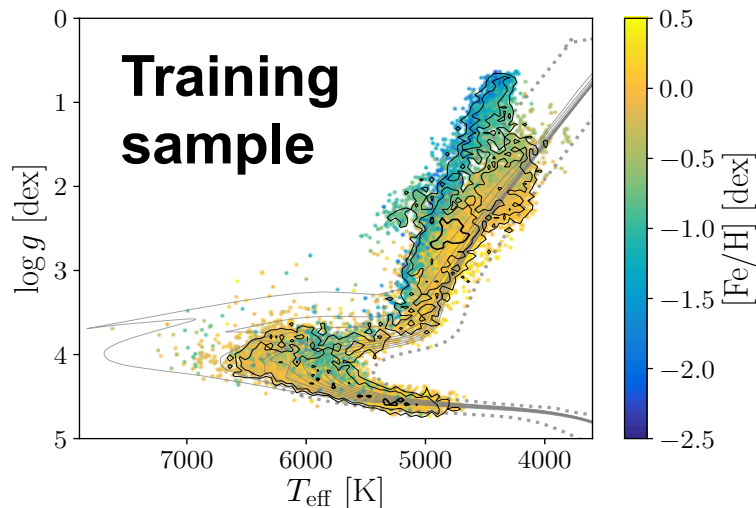
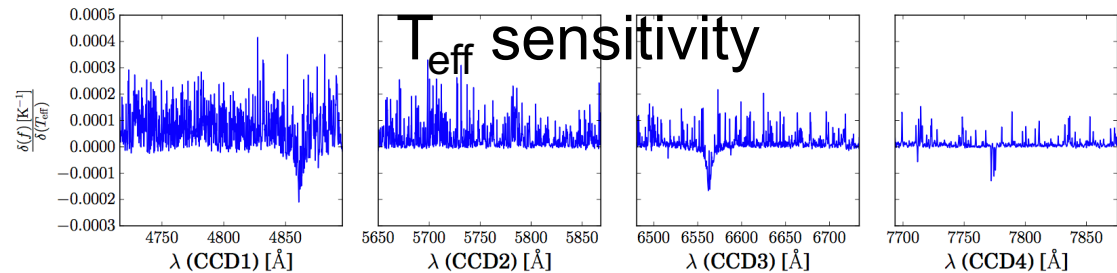
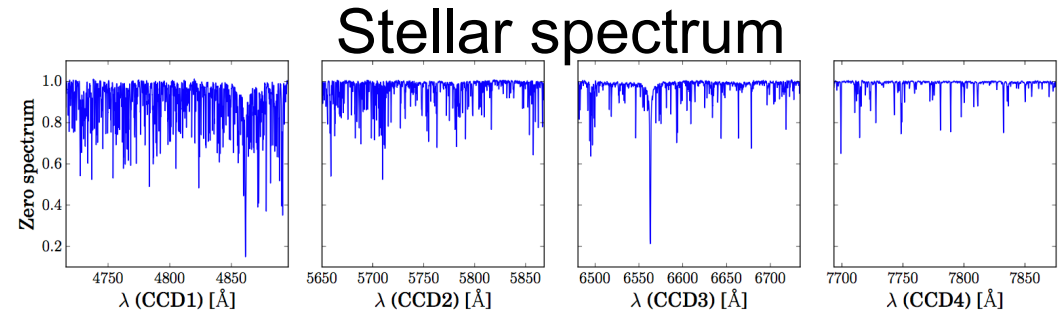
Use linear algebra to construct flux spectra in terms of stellar labels

Flux at a pixel

Label coefficients

Labels

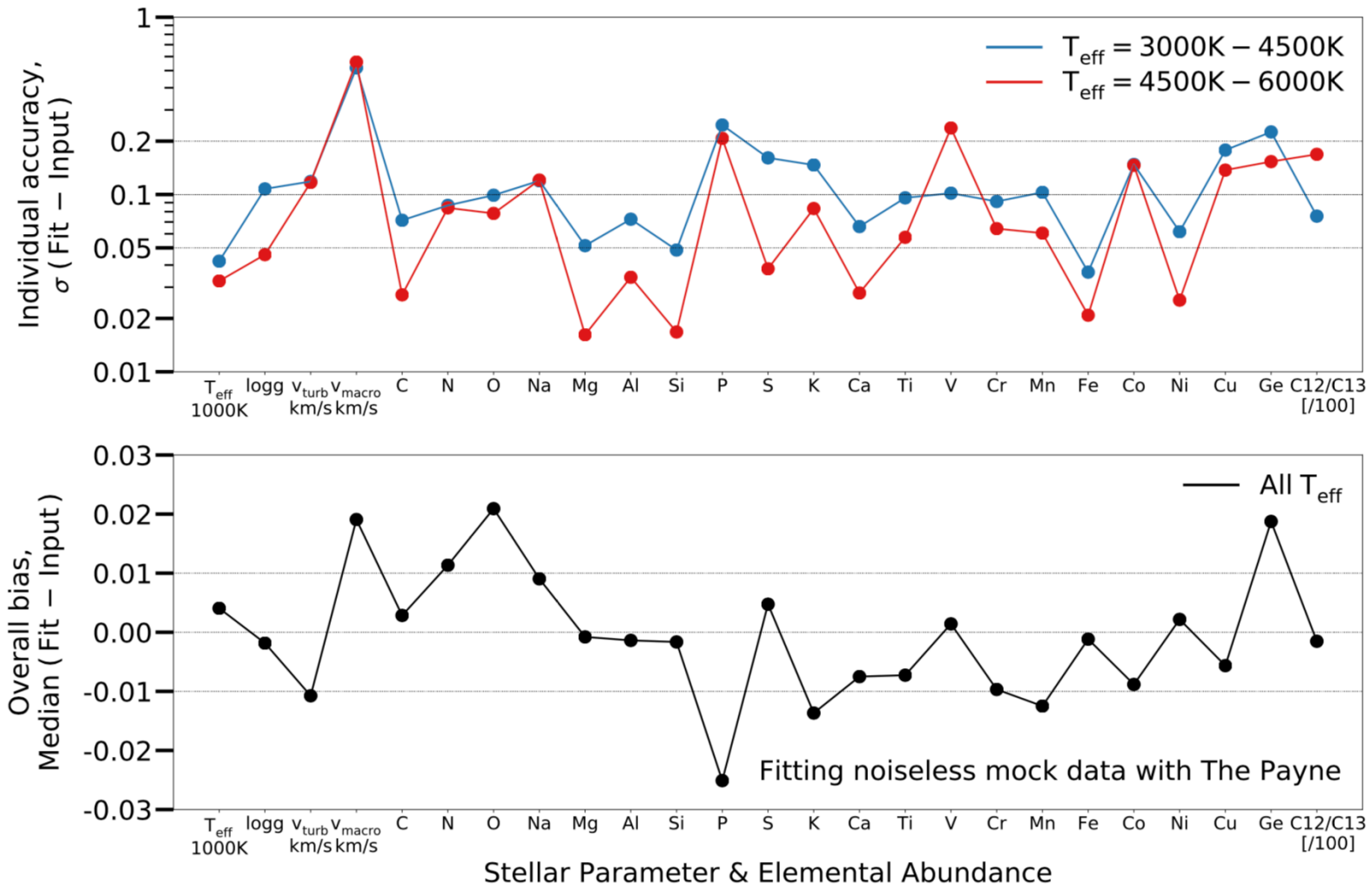
$$f_{n\lambda} = \theta_{\lambda}^T \cdot \ell_n + \text{noise}$$



# Payne

Ting et al. 2019:

Physics-informed ab-initio theoretical spectra for sparse and randomly selected grid models with ANN interpolation



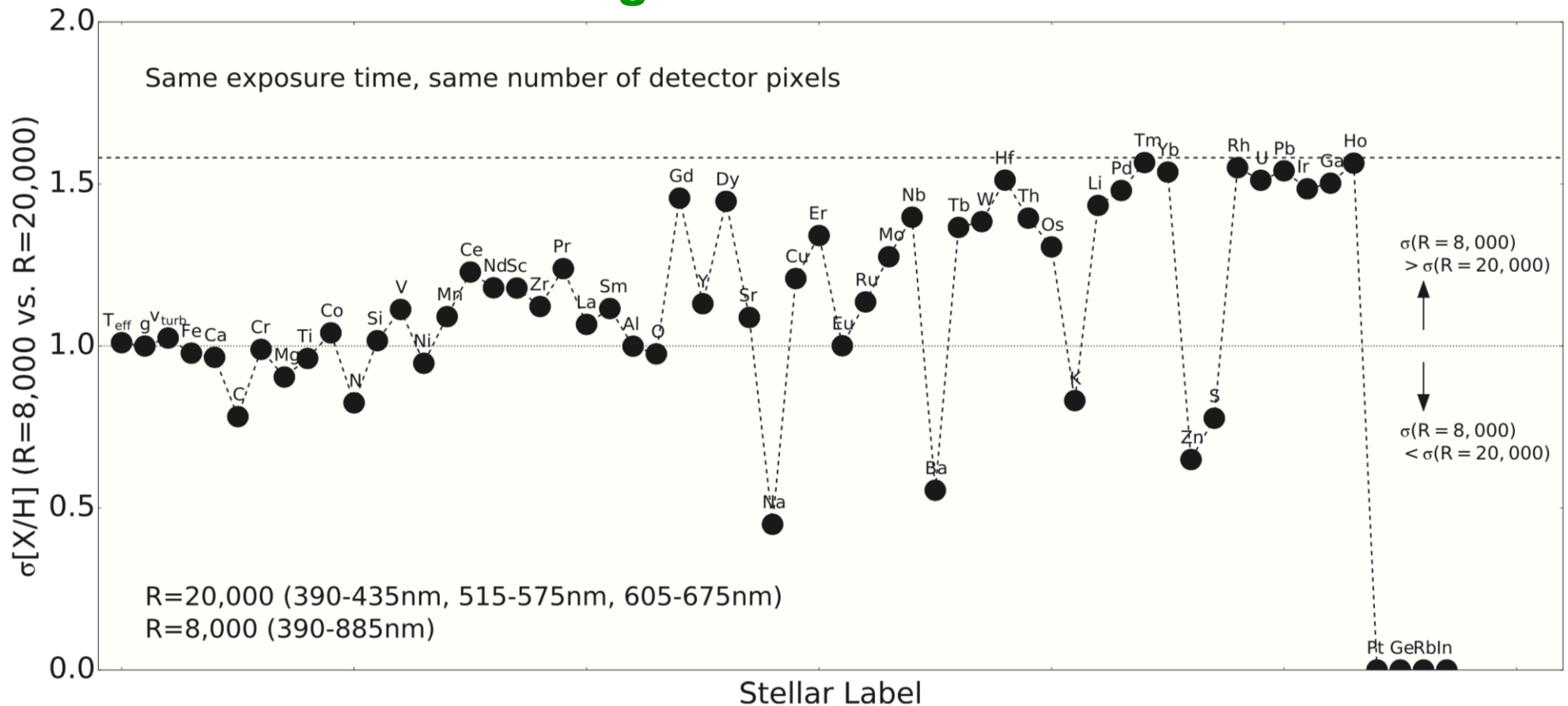
# Low vs high resolution

High-res: analysis of selected “good” lines

Low-res: global fit to whole spectrum

Similar information content for equal  $\tau_{\text{exposure}}$  and  $N_{\text{pixels}}$

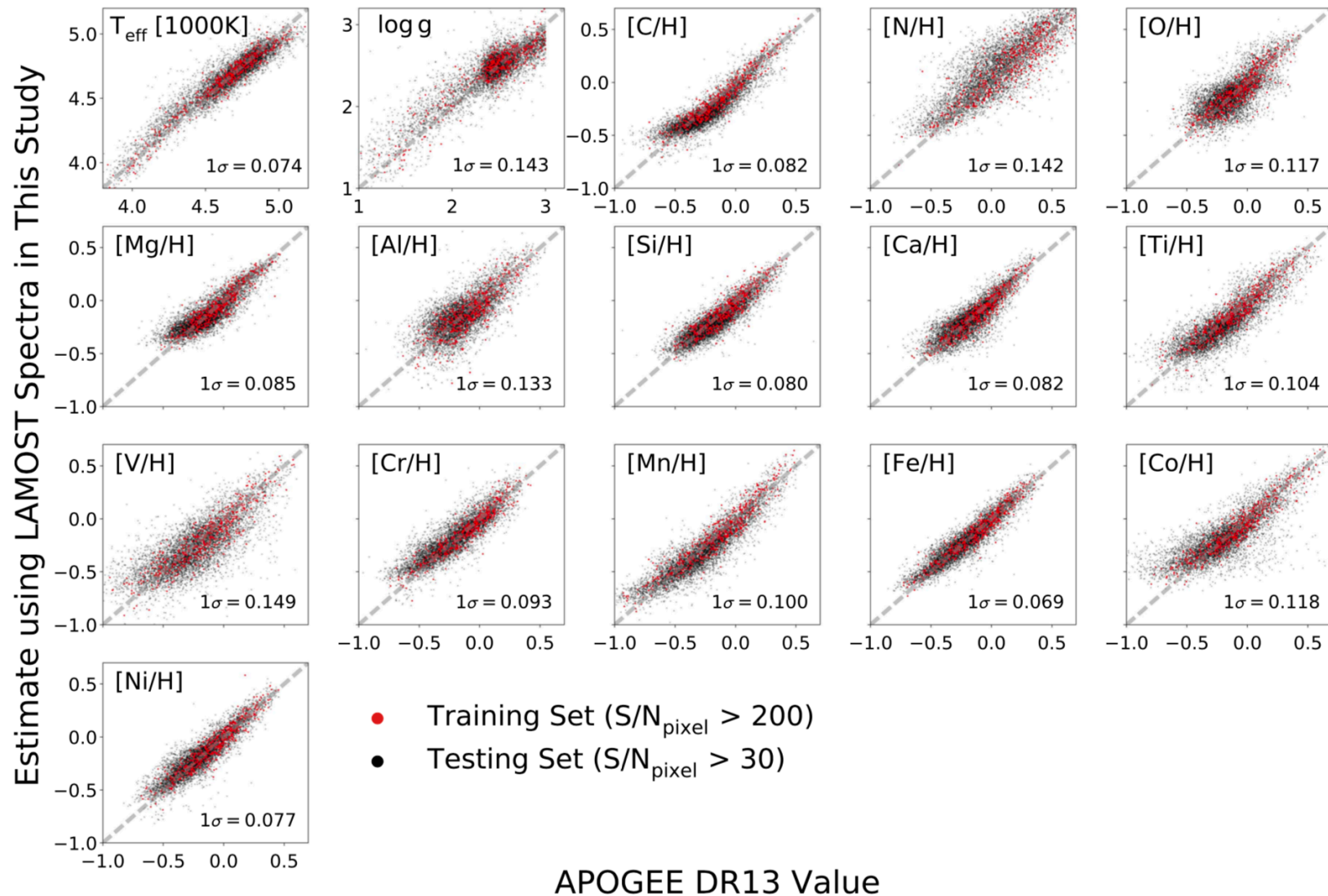
Ting et al. 2017:



# Payne + LAMOST

Ting et al. 2017:

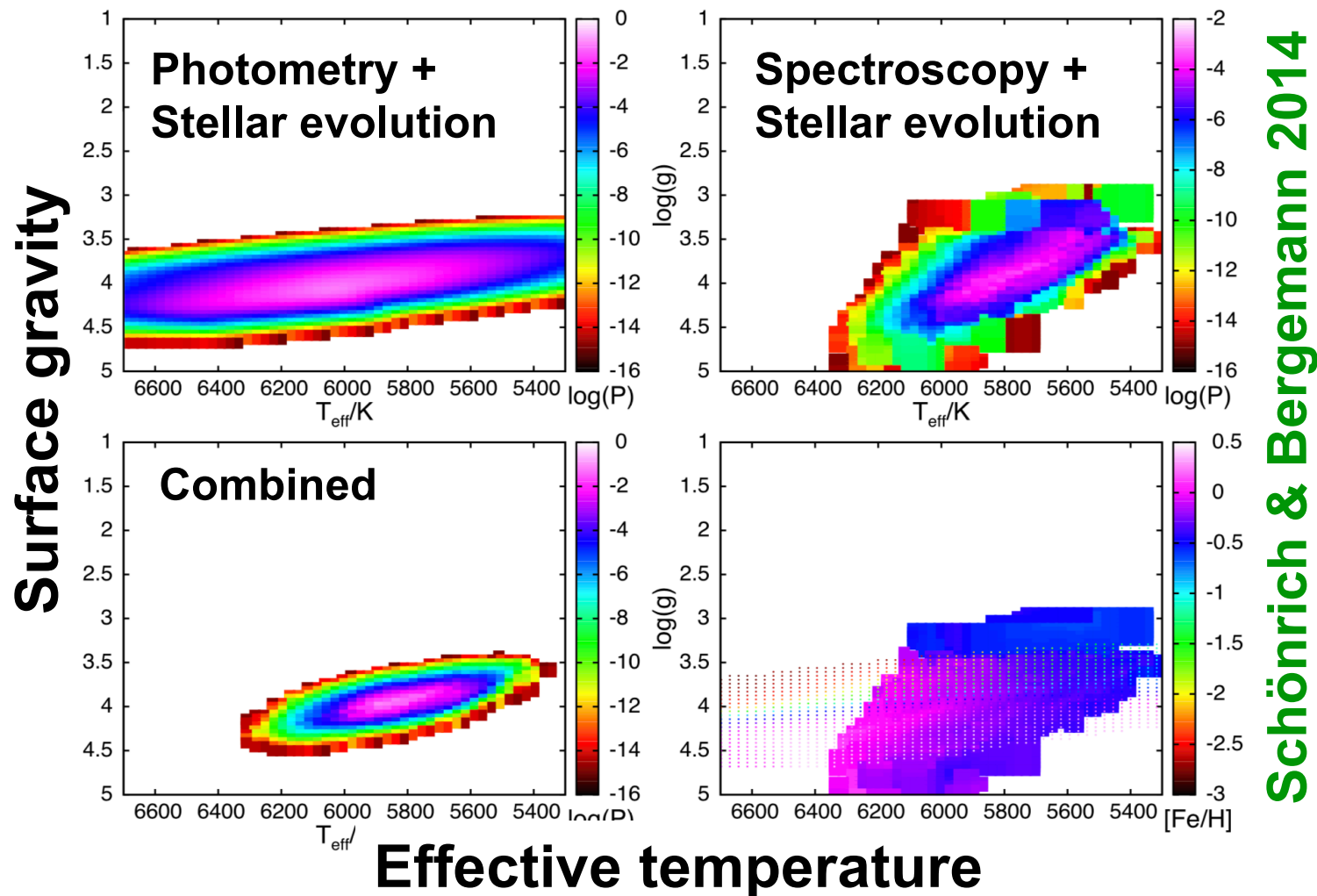
Measure 14 elements with R=1800 spectra with 0.1 dex precision



# Bayesian spectroscopy

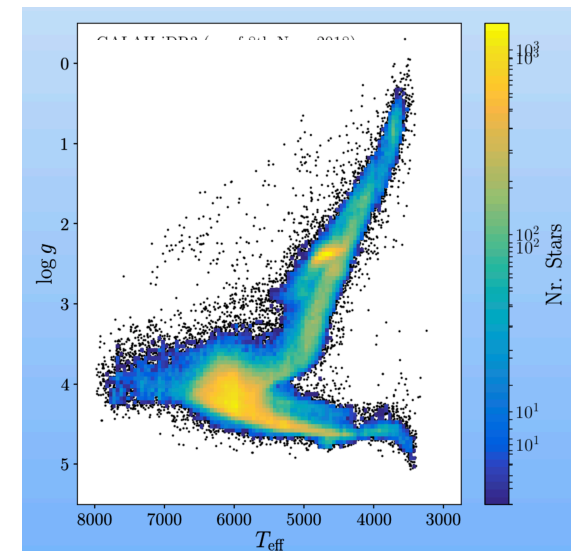
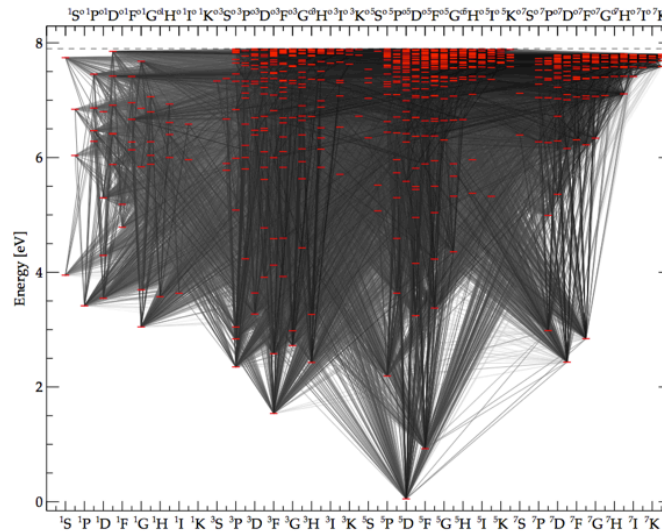
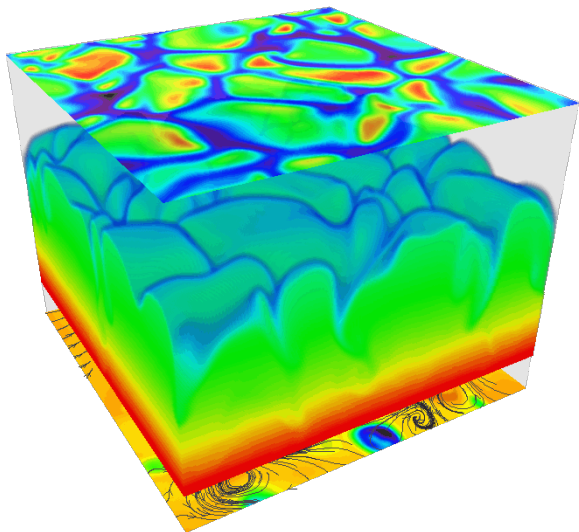
Schönrich & Bergemann 2014 (also Bailer-Jones et al. 2013)

Combine all spectroscopic, photometric, astrometric, and asteroseismic information with stellar evolution priors



# Outlook

- **3D stellar atmosphere models**
- **3D non-LTE spectrum formation**
- **Large spectroscopic surveys**
- **Physics-informed machine learning**
- **Bayesian spectroscopy**



# Great collaborators

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