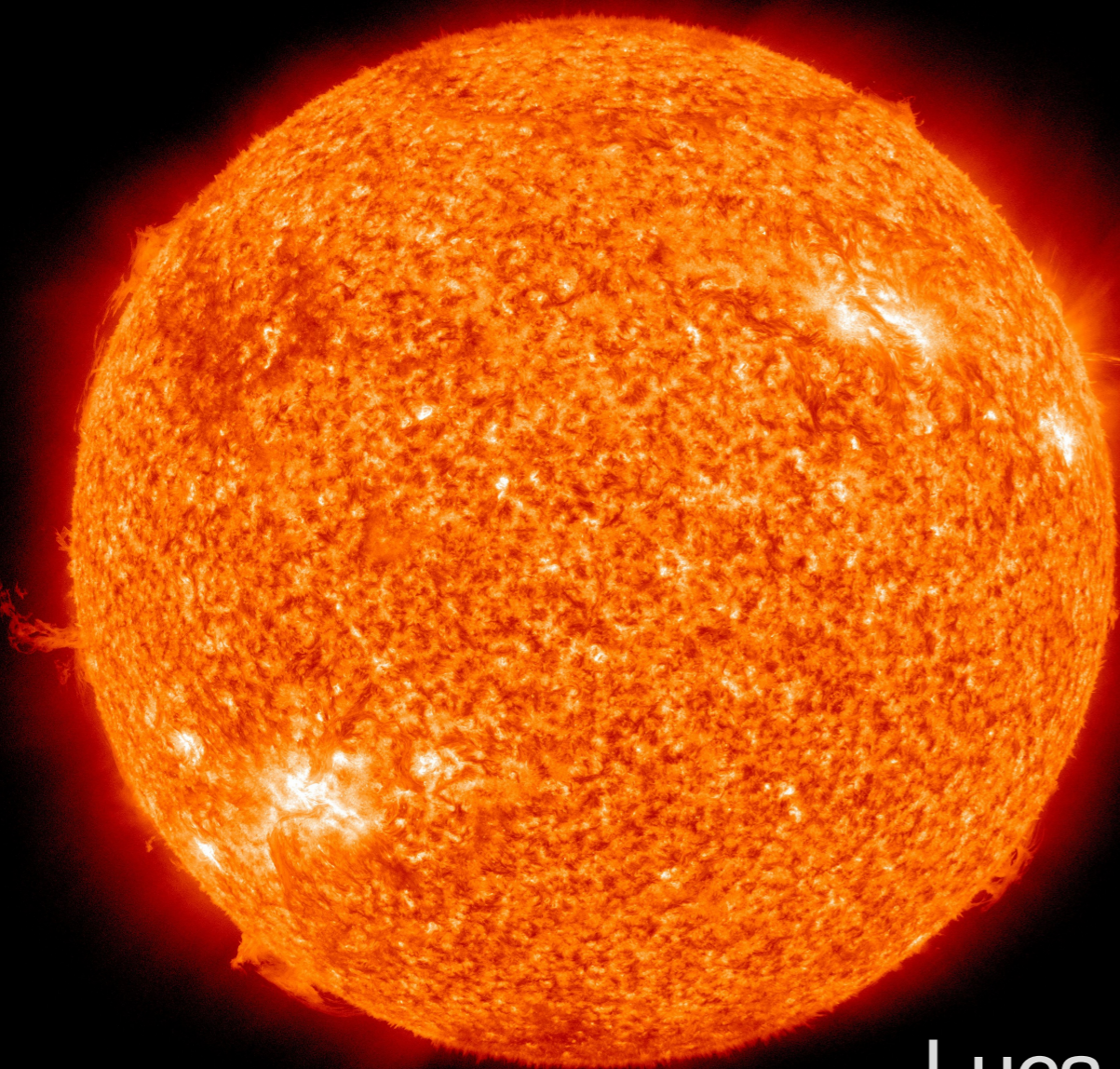


# Asteroseismology & better stellar ages



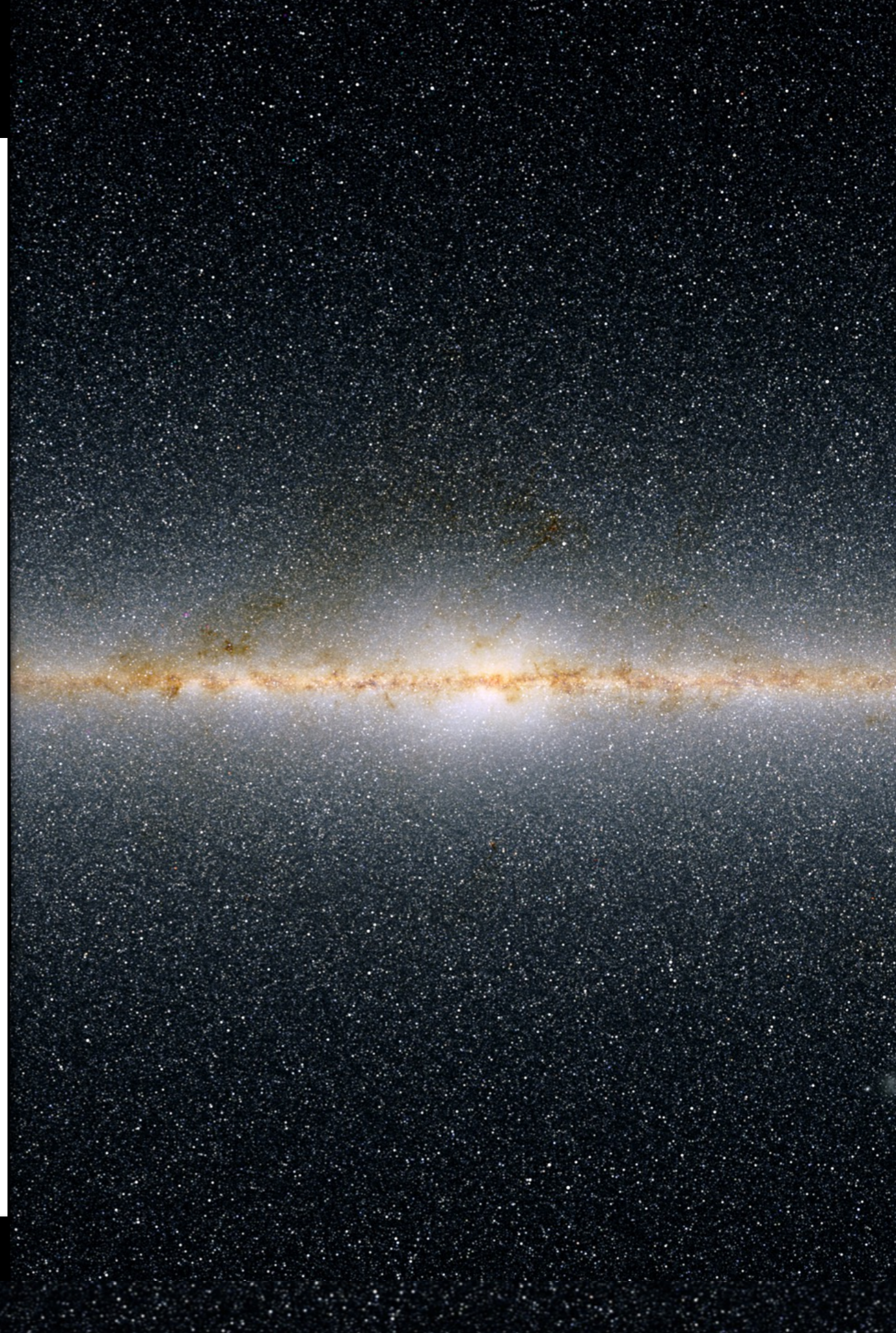
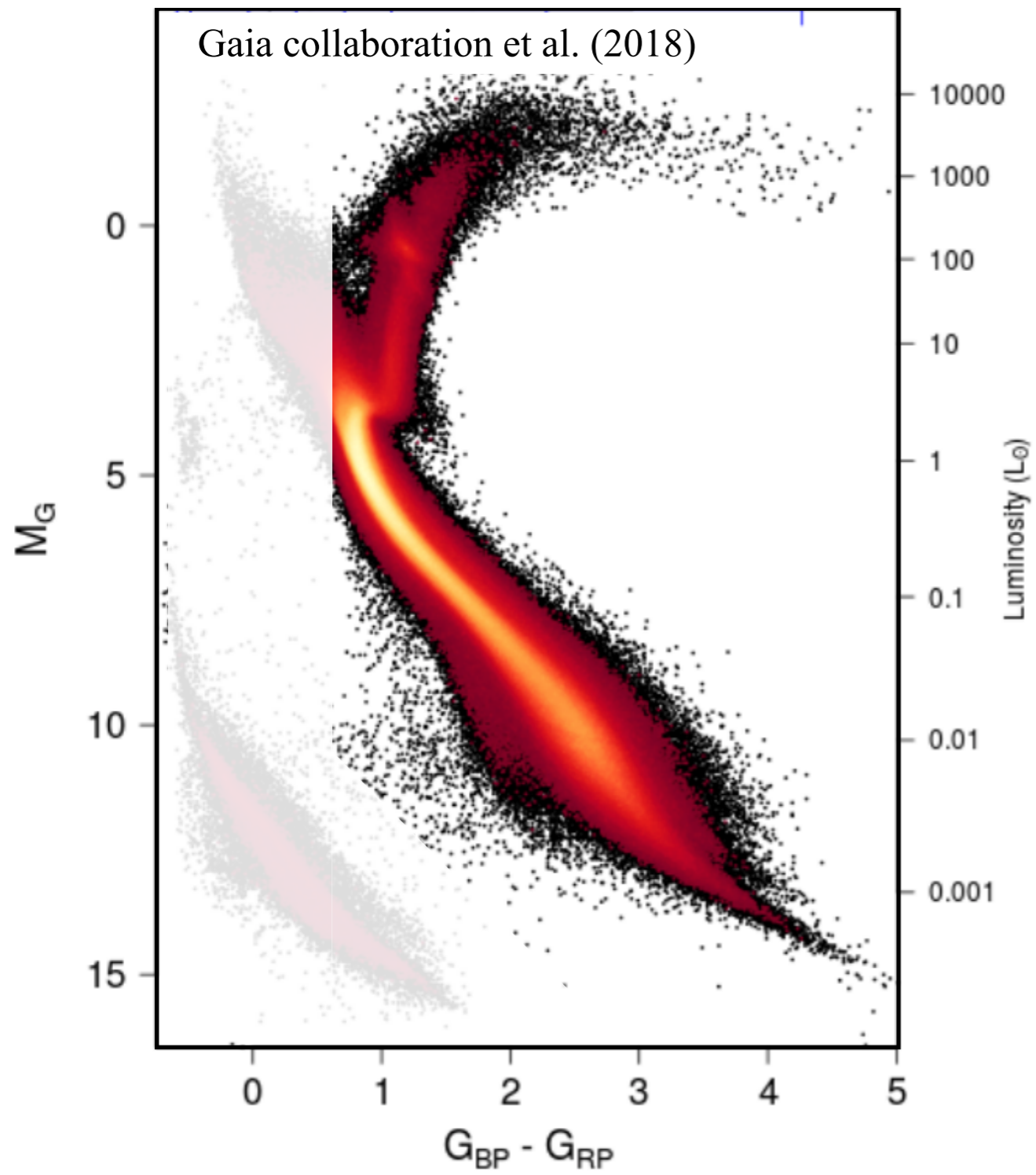
Luca Casagrande



Australian  
National  
University

D. Huber, A. Miglio, B. Rendle, A. Serenelli, V. Silva Aguirre, D. Stello



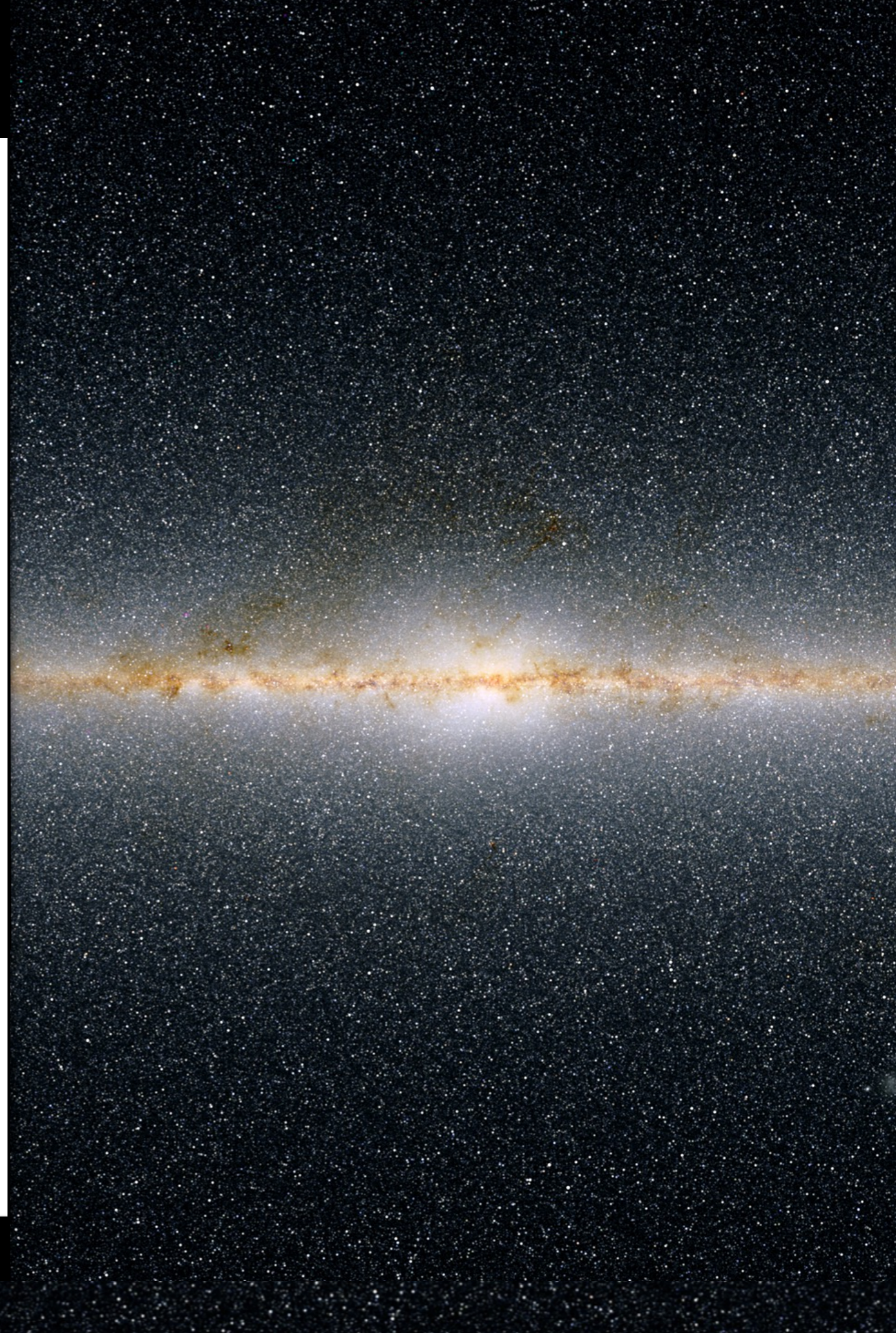
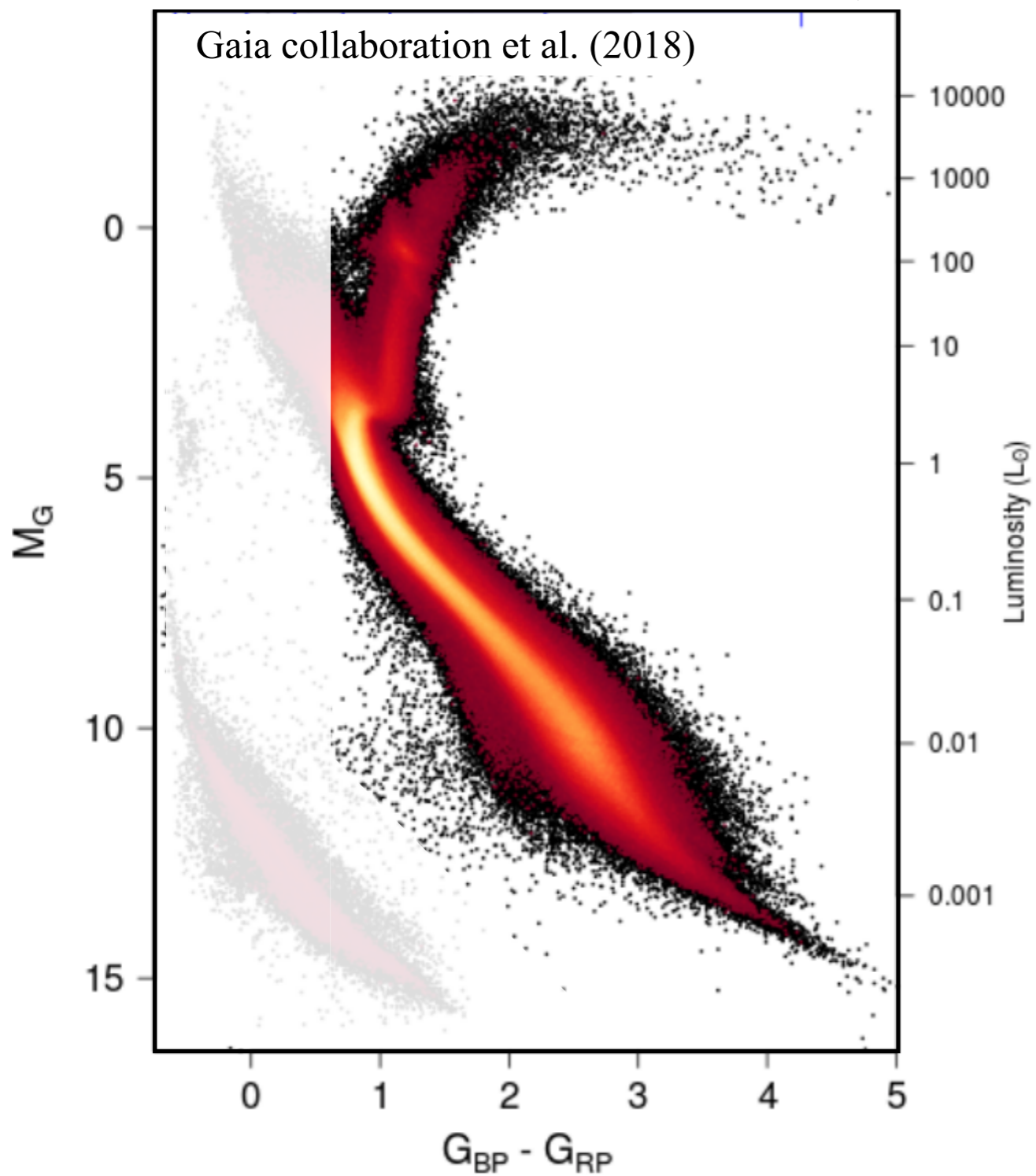




# Solar-like Oscillations



Gaia collaboration et al. (2018)

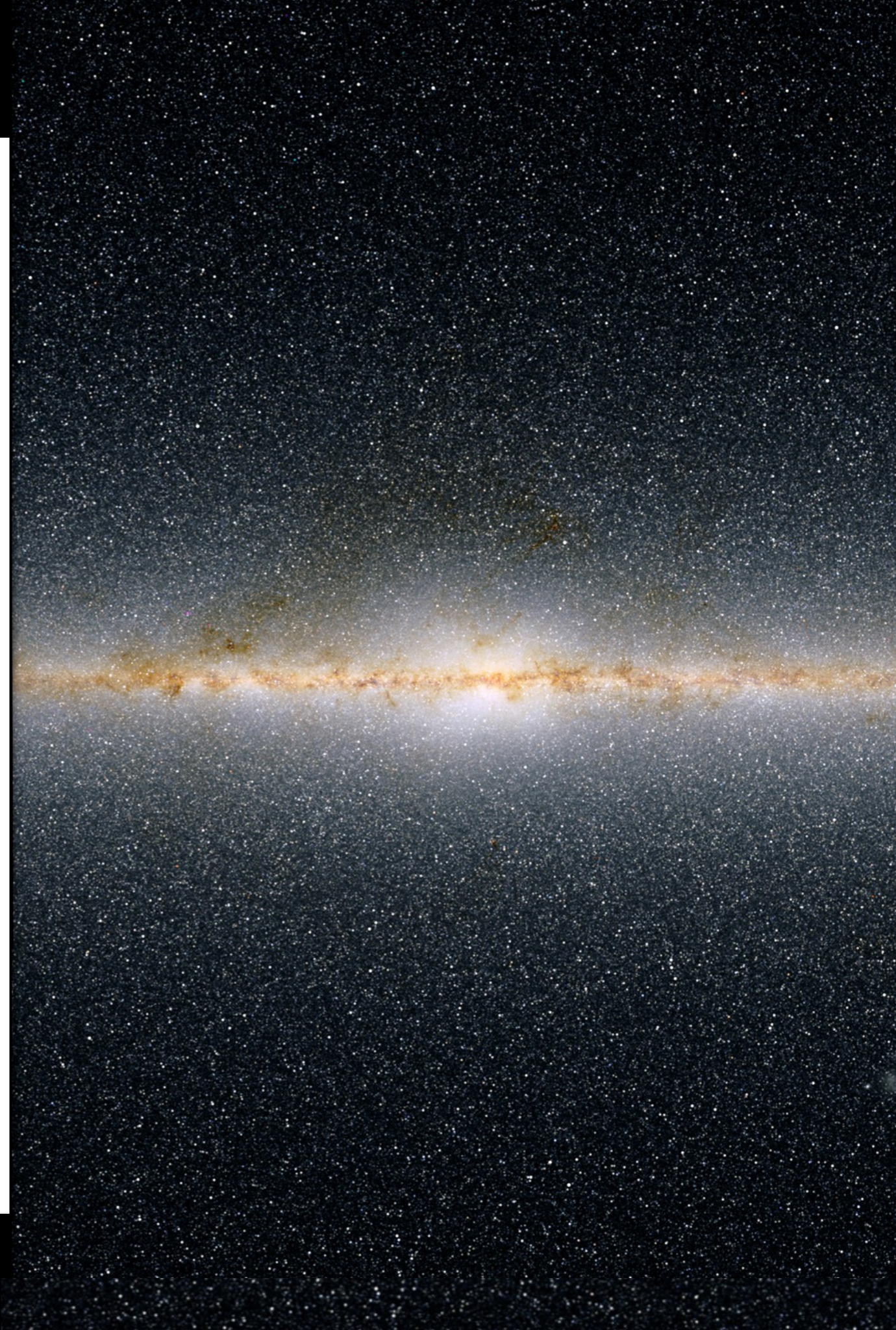
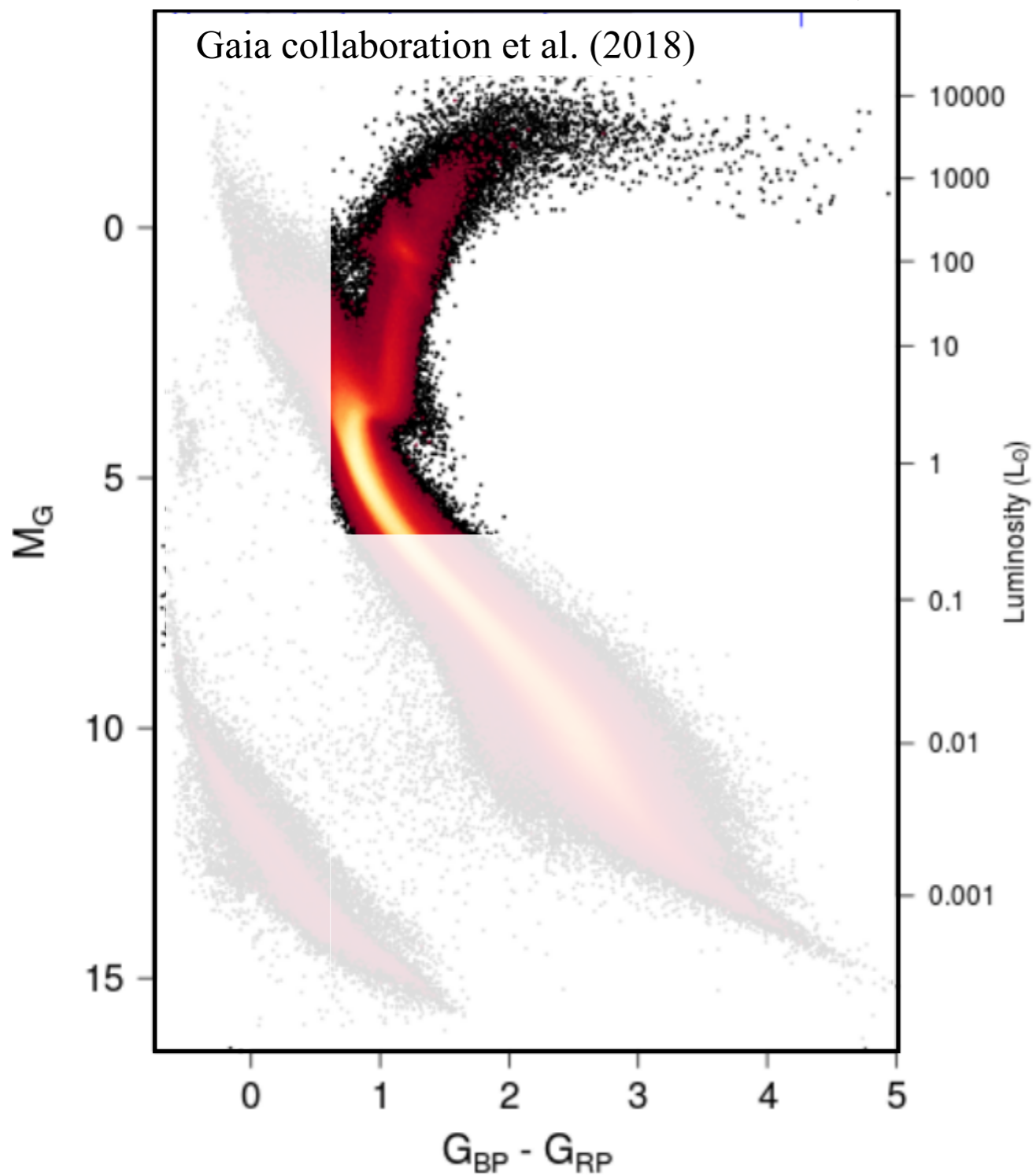




# Solar-like Oscillations



Gaia collaboration et al. (2018)

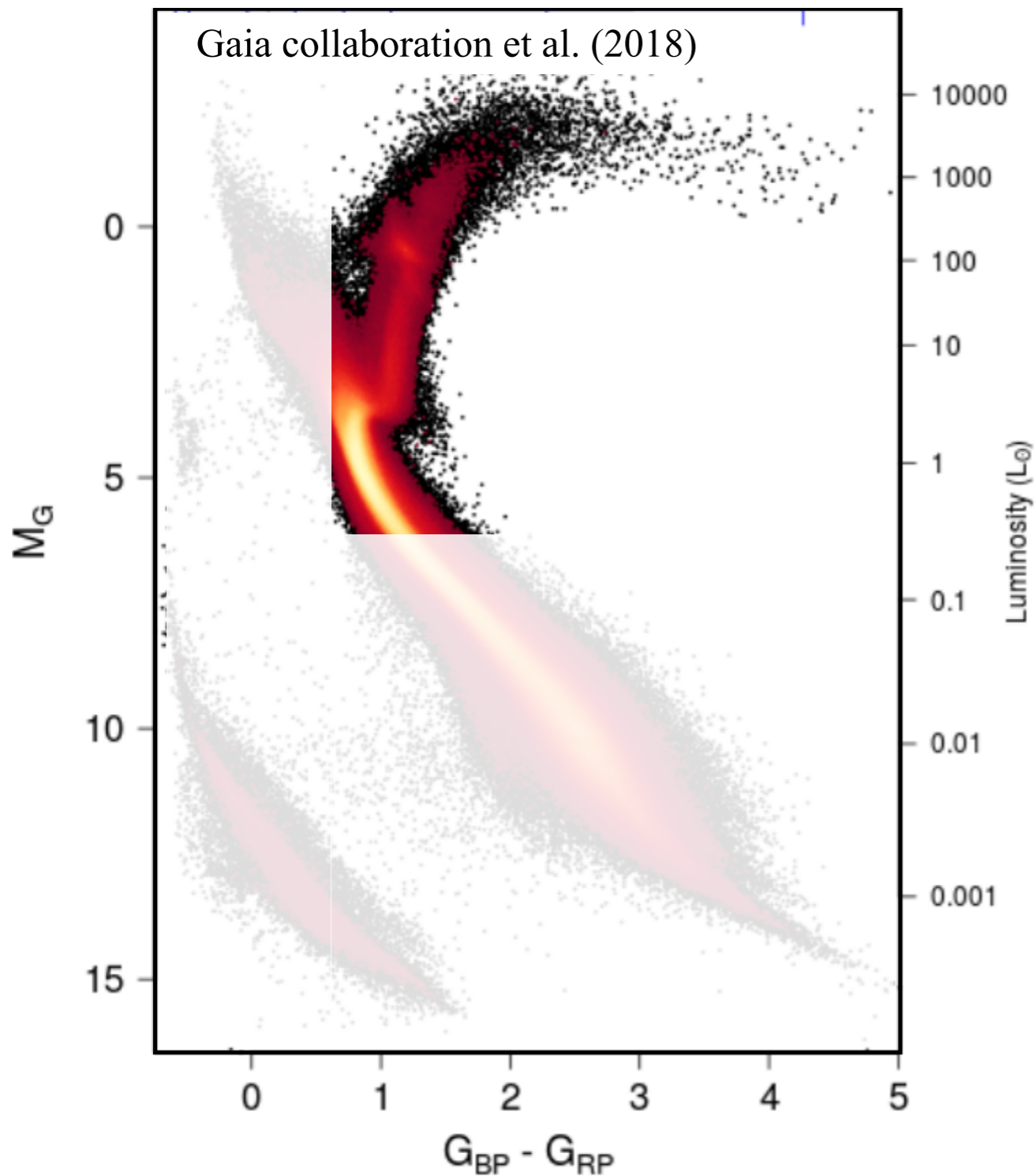




## Solar-like Oscillations



Gaia collaboration et al. (2018)



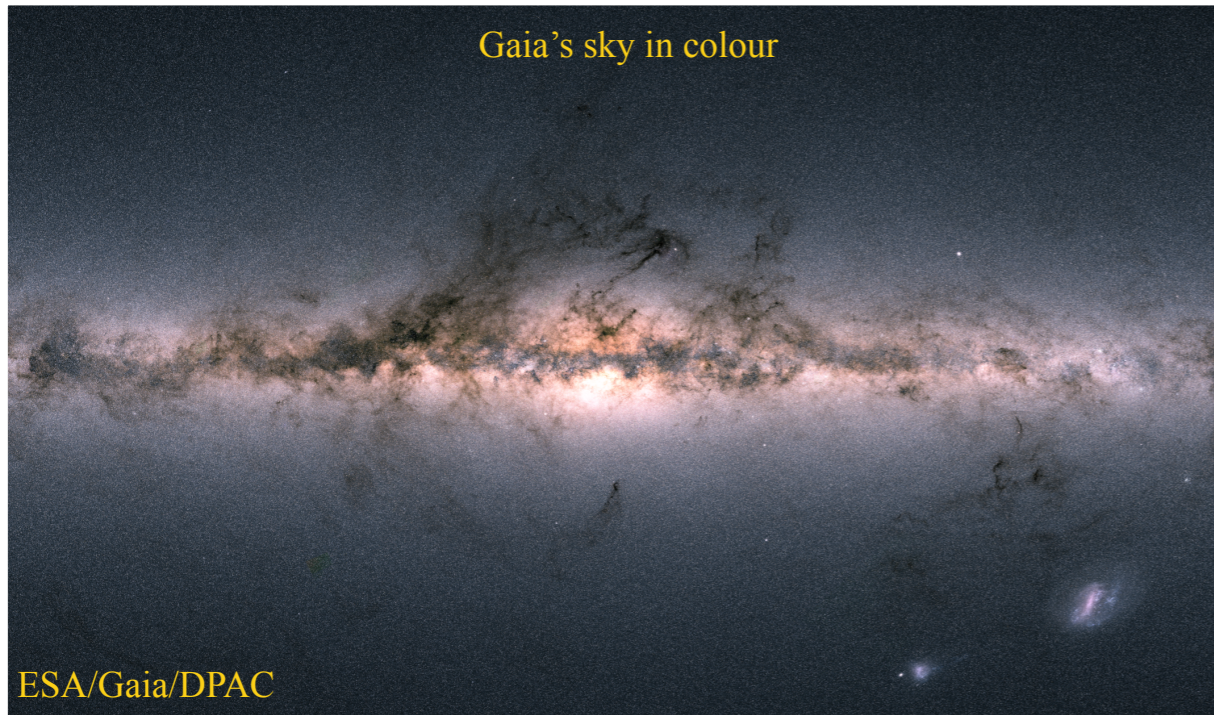
Is the distribution of stellar ages  
telling us about past star  
formation events?

What's the interplay between  
chemistry, kinematic and ages?

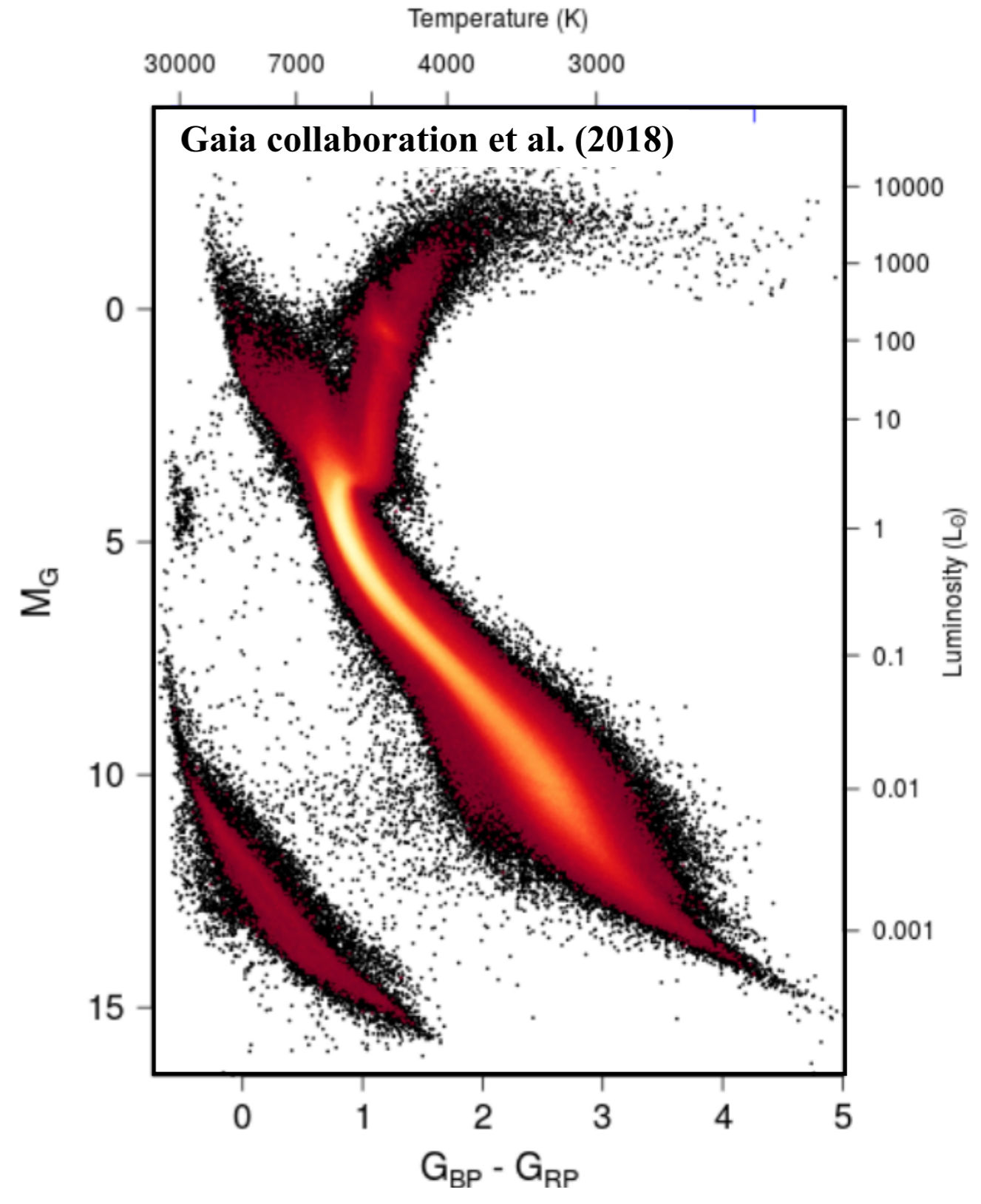
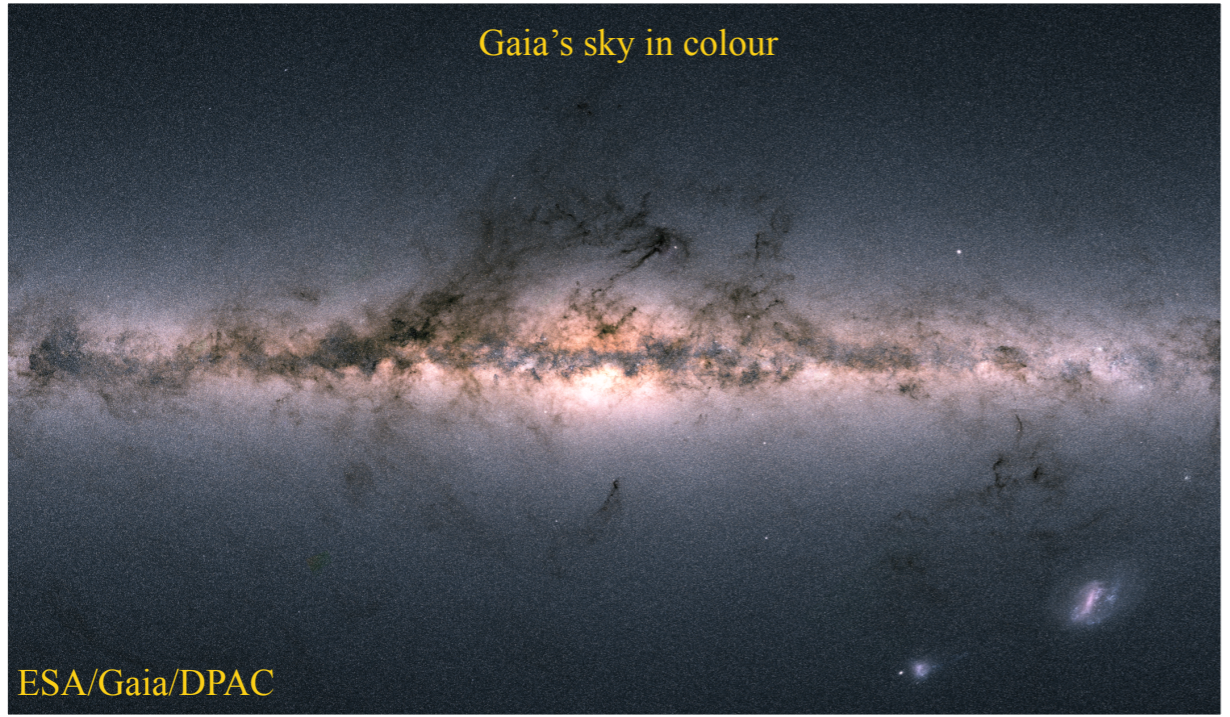
# Need for good ages

(and understanding target selection effects!)





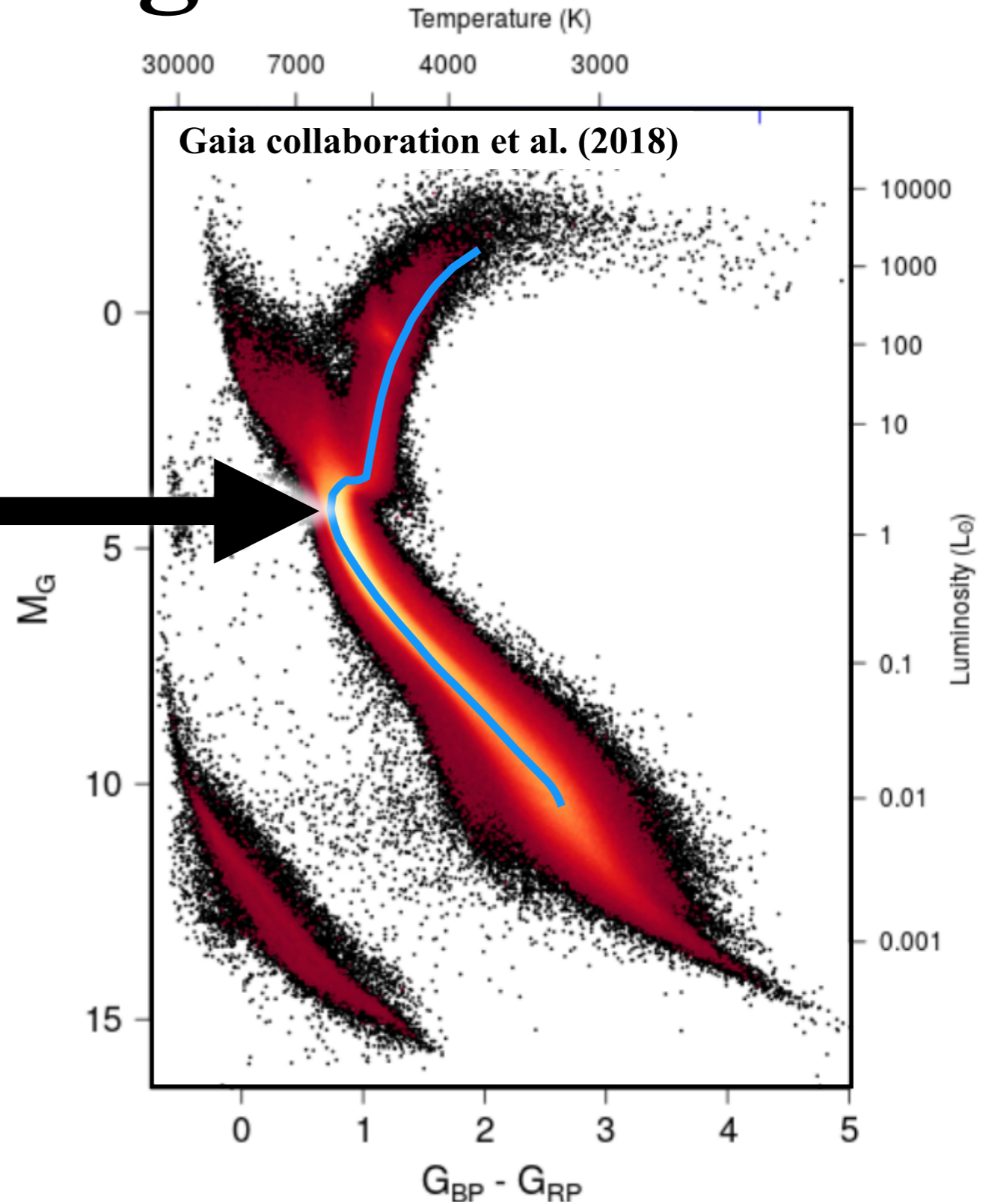




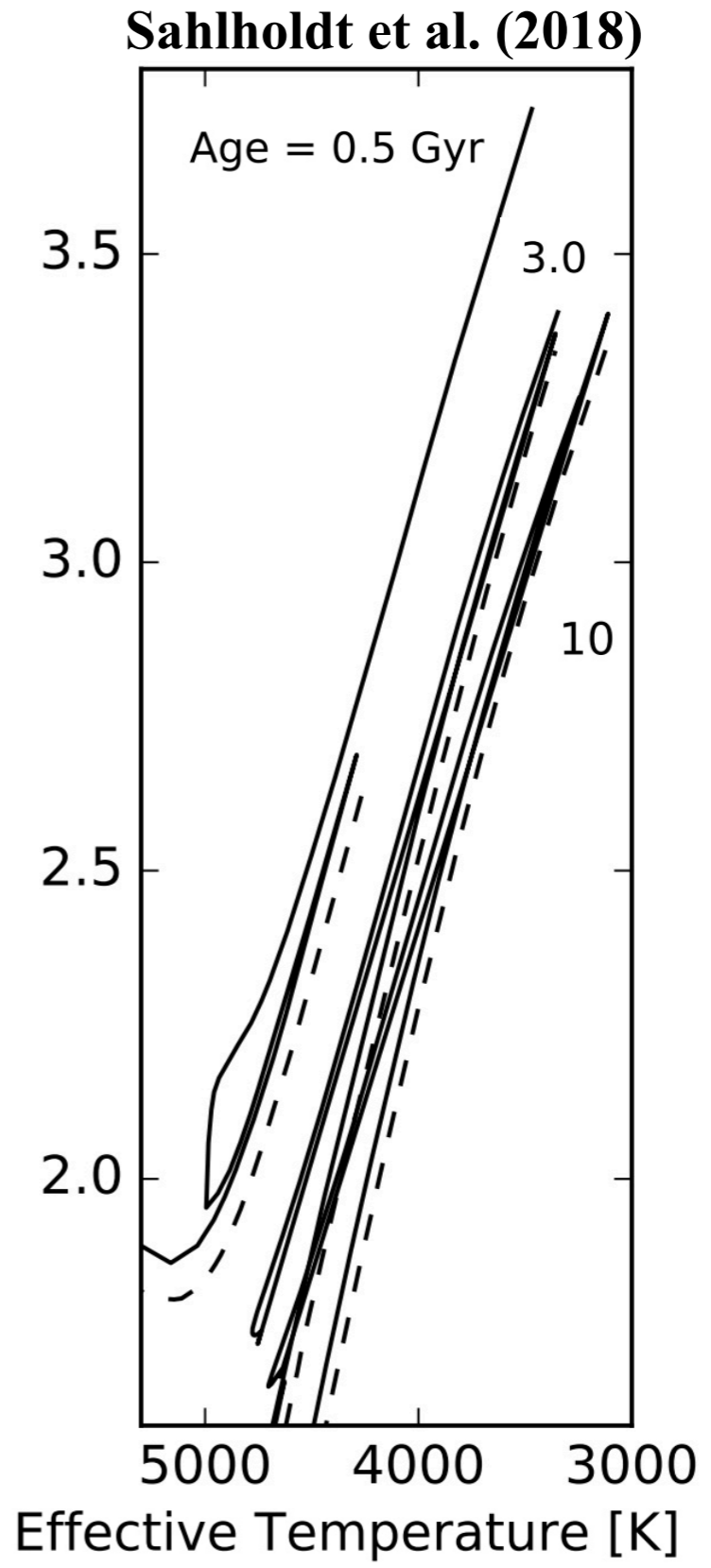
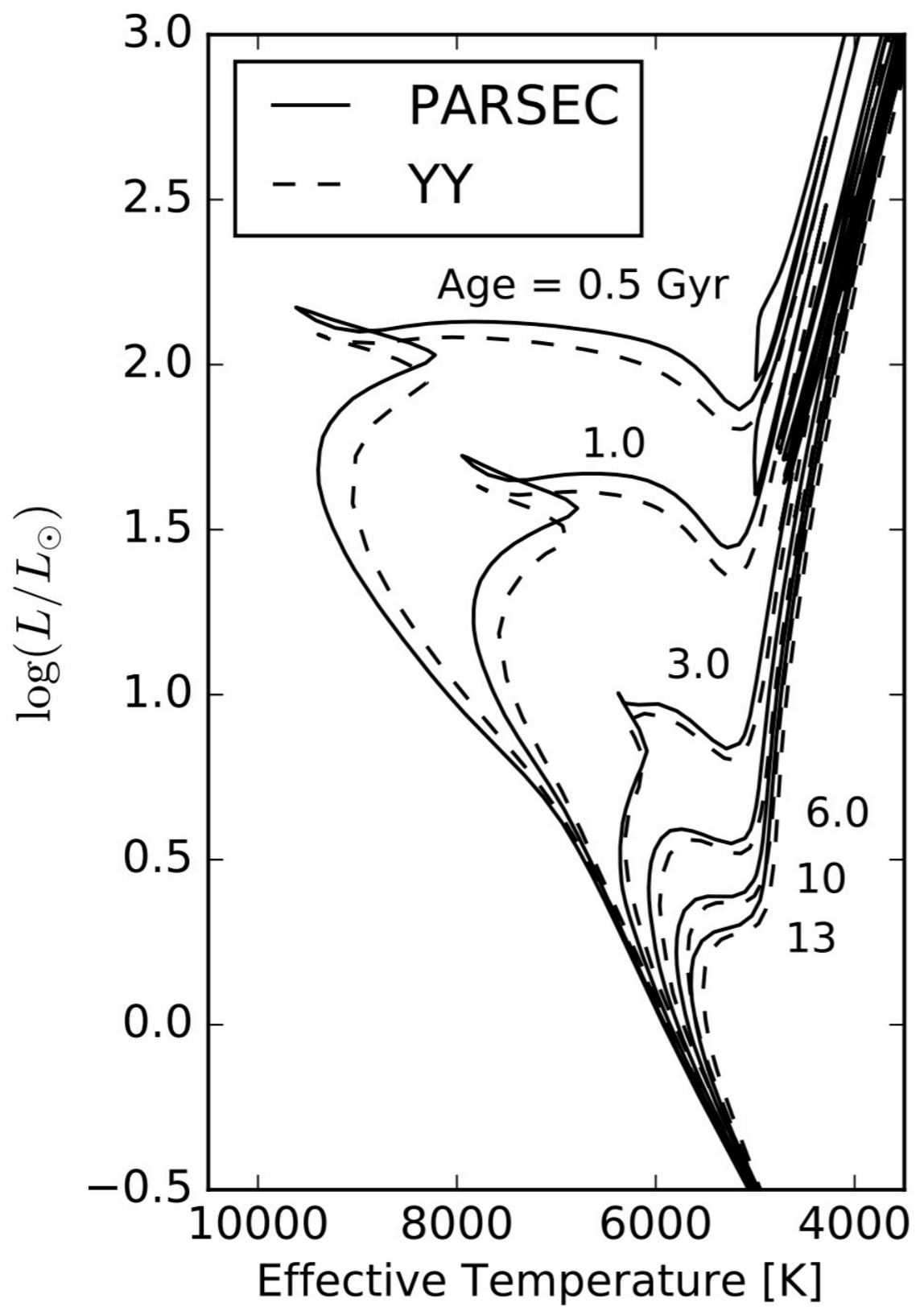


# Stellar Ages

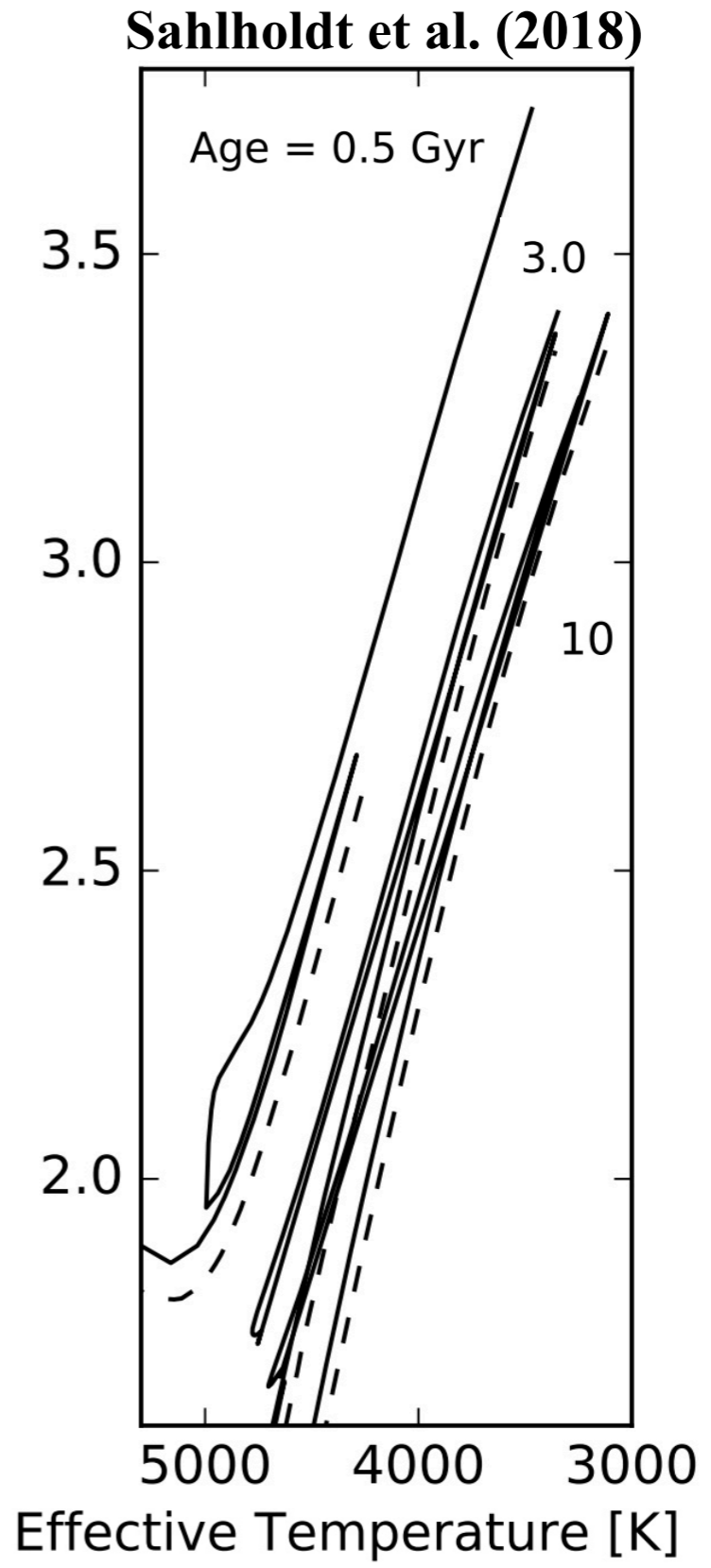
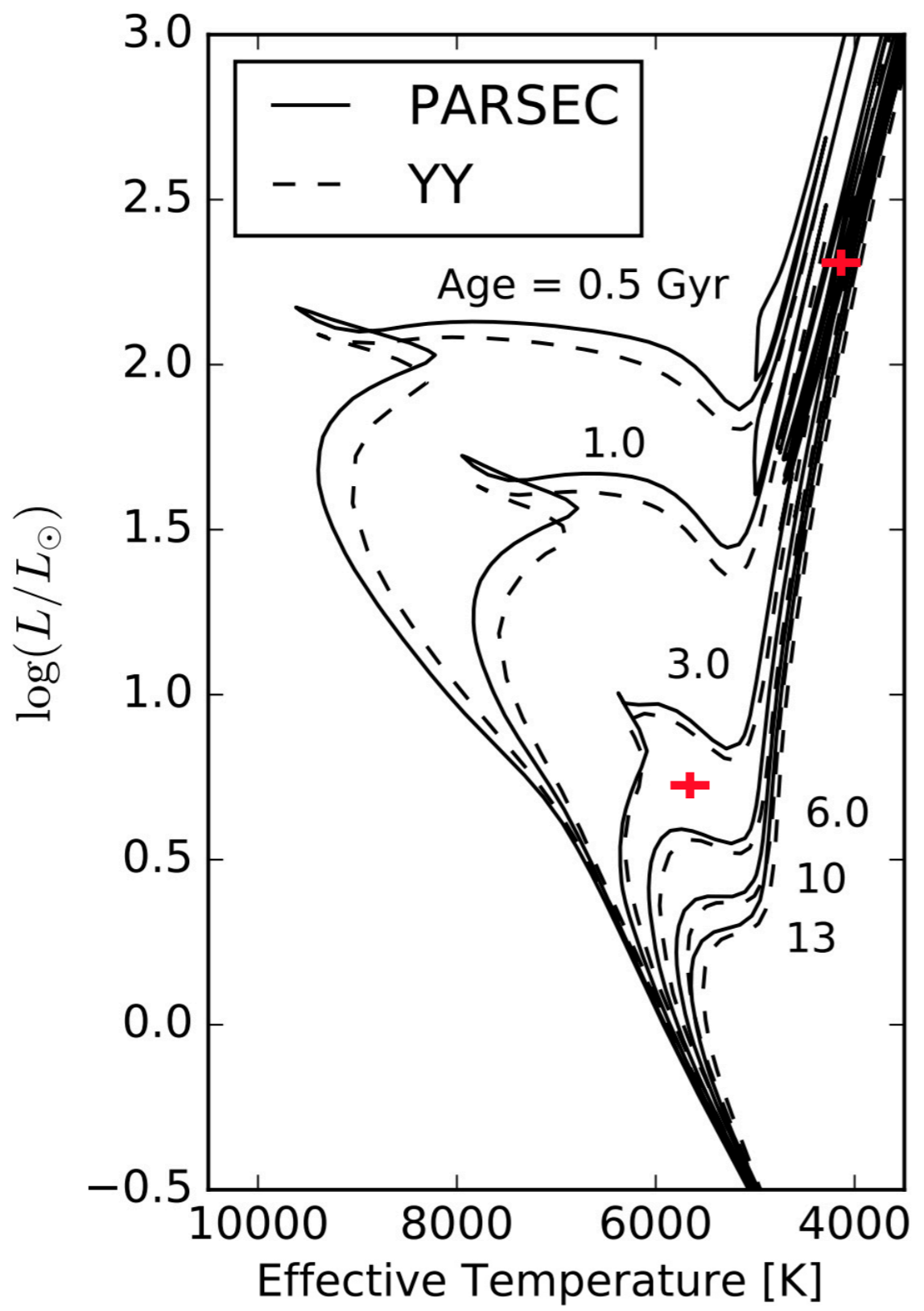
**Astrometry**  
(Gaia distances+isochrones)











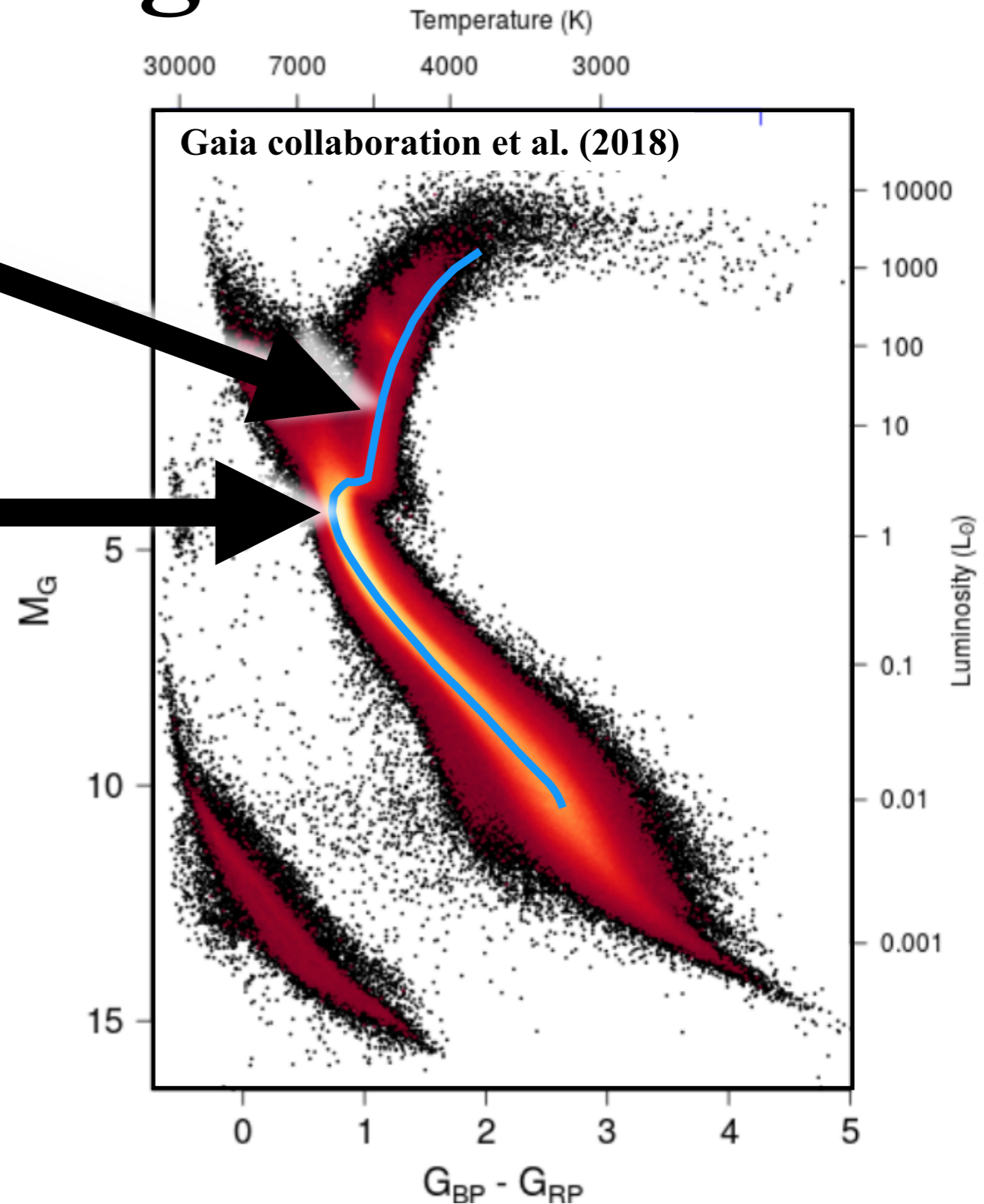


# Stellar Ages

**Asteroseismology**  
(stellar oscillations)

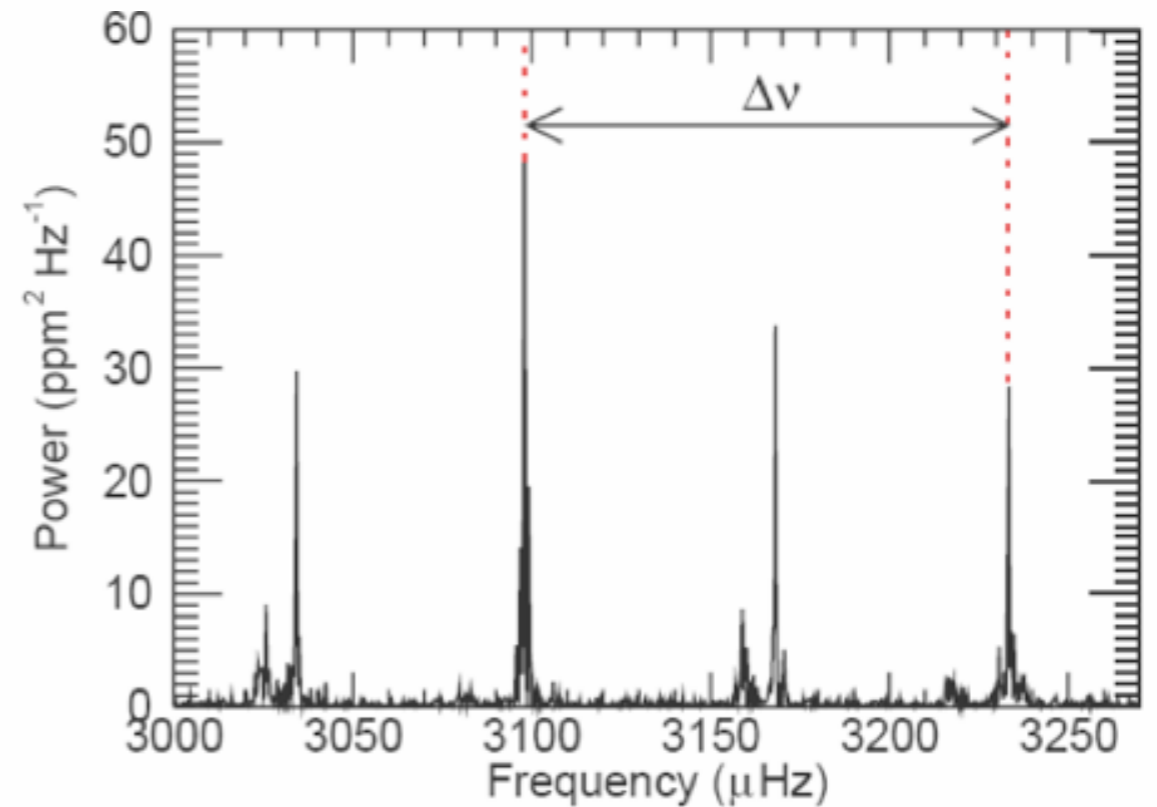
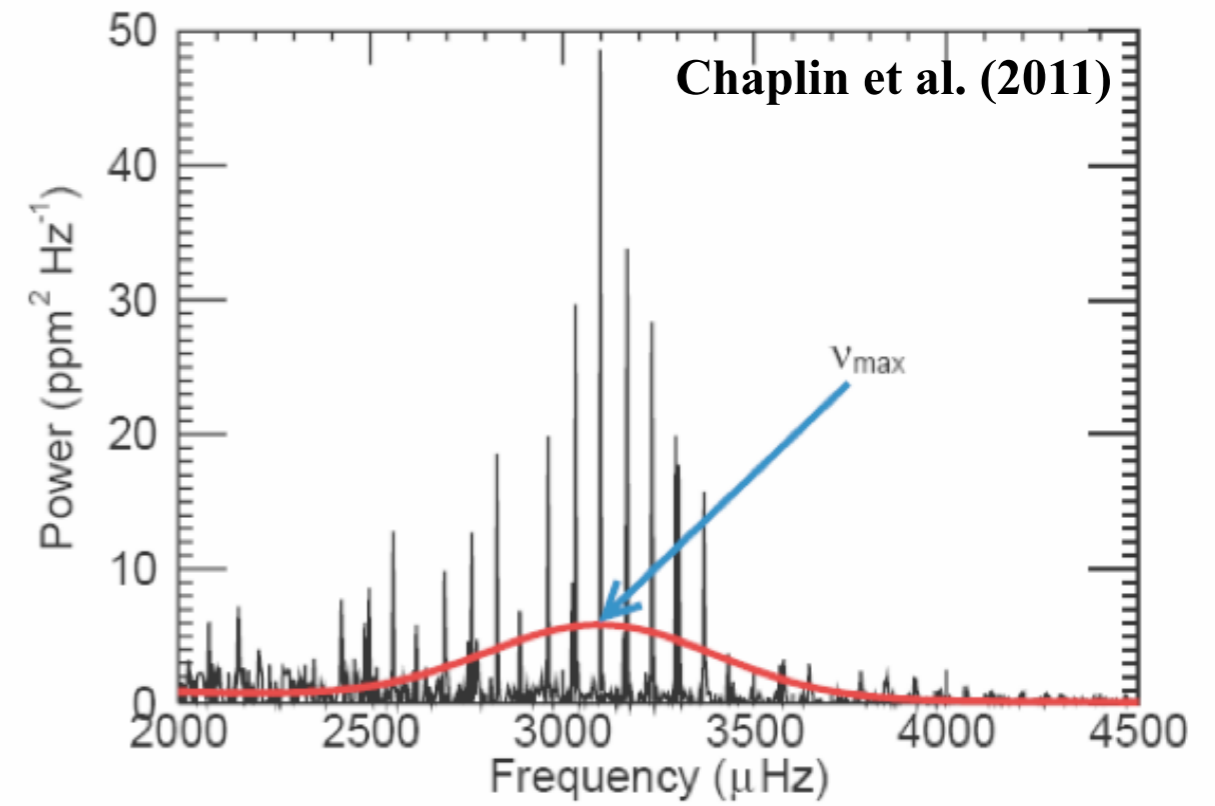
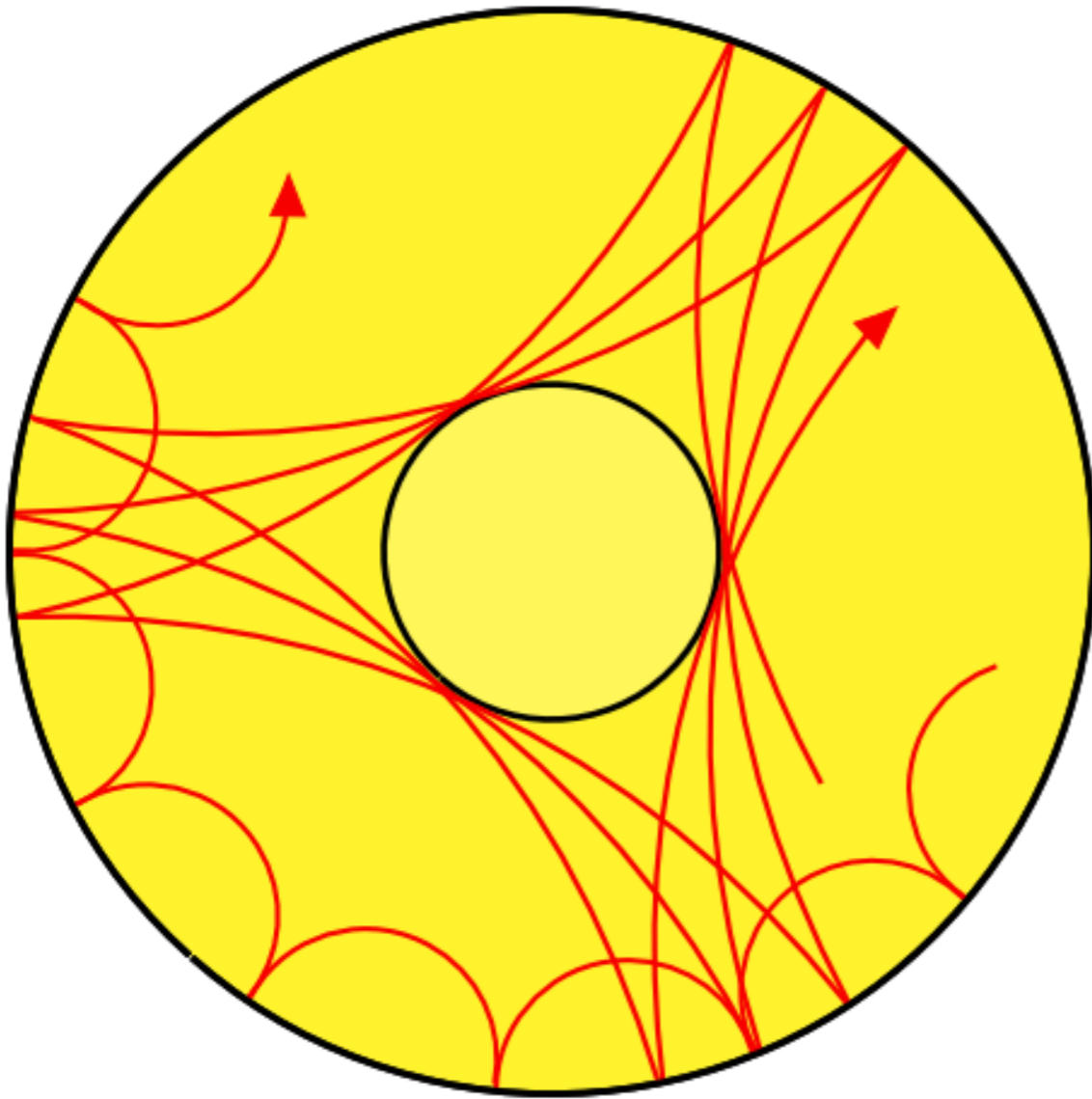
**Astrometry**  
(Gaia distances+isochrones)

Ages for red giant stars allow us to probe a large volume of the Milky Way.





# Solar-like oscillations





# Scaling relations

Brown et al. (1991), Kjeldsen & Bedding (1995)

$$\Delta\nu \propto \left(\frac{M}{R^3}\right)^{1/2}$$

$$\nu_{\max} \propto \frac{M}{R^2 \sqrt{T_{\text{eff}}}}$$



# Scaling relations

Brown et al. (1991), Kjeldsen & Bedding (1995)

$$\Delta\nu \propto \left(\frac{M}{R^3}\right)^{1/2} \qquad \nu_{\max} \propto \frac{M}{R^2 \sqrt{T_{\text{eff}}}}$$

solve to get mass and radius

$$\frac{M}{M_{\odot}} \simeq \left(\frac{\nu_{\max}}{\nu_{\max,\odot}}\right)^3 \left(\frac{\Delta\nu}{\Delta\nu_{\odot}}\right)^{-4} \left(\frac{T_{\text{eff}}}{T_{\text{eff},\odot}}\right)^{3/2}$$

$$\frac{R}{R_{\odot}} \simeq \left(\frac{\nu_{\max}}{\nu_{\max,\odot}}\right) \left(\frac{\Delta\nu}{\Delta\nu_{\odot}}\right)^{-2} \left(\frac{T_{\text{eff}}}{T_{\text{eff},\odot}}\right)^{1/2}$$

e.g., Stello et al. (2008)



# Scaling relations

Brown et al. (1991), Kjeldsen & Bedding (1995)

$$\Delta\nu \propto \left(\frac{M}{R^3}\right)^{1/2} \qquad \nu_{\max} \propto \frac{M}{R^2 \sqrt{T_{\text{eff}}}}$$

solve to get mass and radius

age

$$\left(\frac{M}{M_{\odot}}\right) \approx \left(\frac{\nu_{\max}}{\nu_{\max, \odot}}\right)^3 \left(\frac{\Delta\nu}{\Delta\nu_{\odot}}\right)^{-4} \left(\frac{T_{\text{eff}}}{T_{\text{eff}, \odot}}\right)^{3/2}$$

$$\left(\frac{R}{R_{\odot}}\right) \approx \left(\frac{\nu_{\max}}{\nu_{\max, \odot}}\right) \left(\frac{\Delta\nu}{\Delta\nu_{\odot}}\right)^{-2} \left(\frac{T_{\text{eff}}}{T_{\text{eff}, \odot}}\right)^{1/2}$$

distance

e.g., Stello et al. (2008)

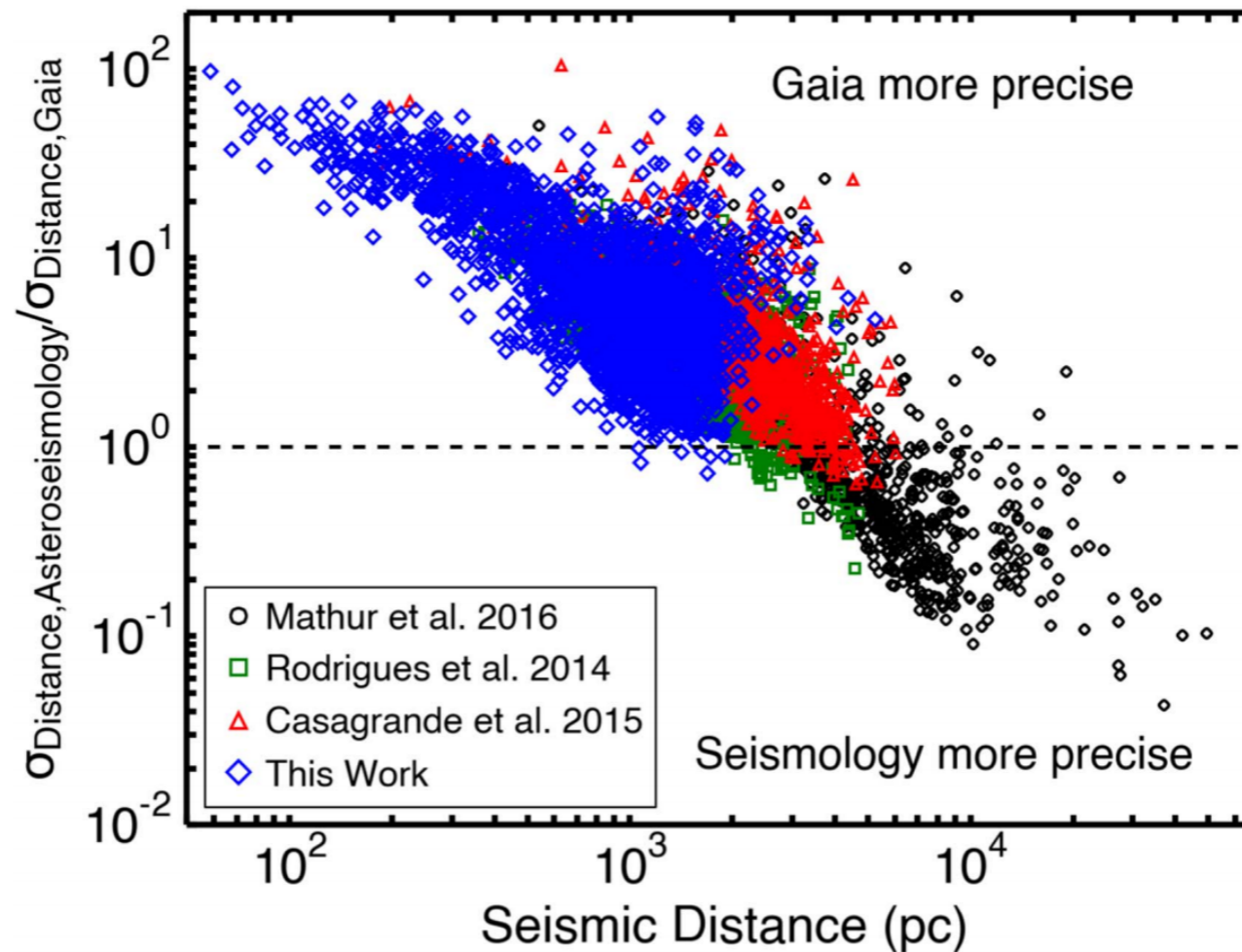


# Scaling relations

Brown et al. (1991), Kjeldsen & Bedding (1995)

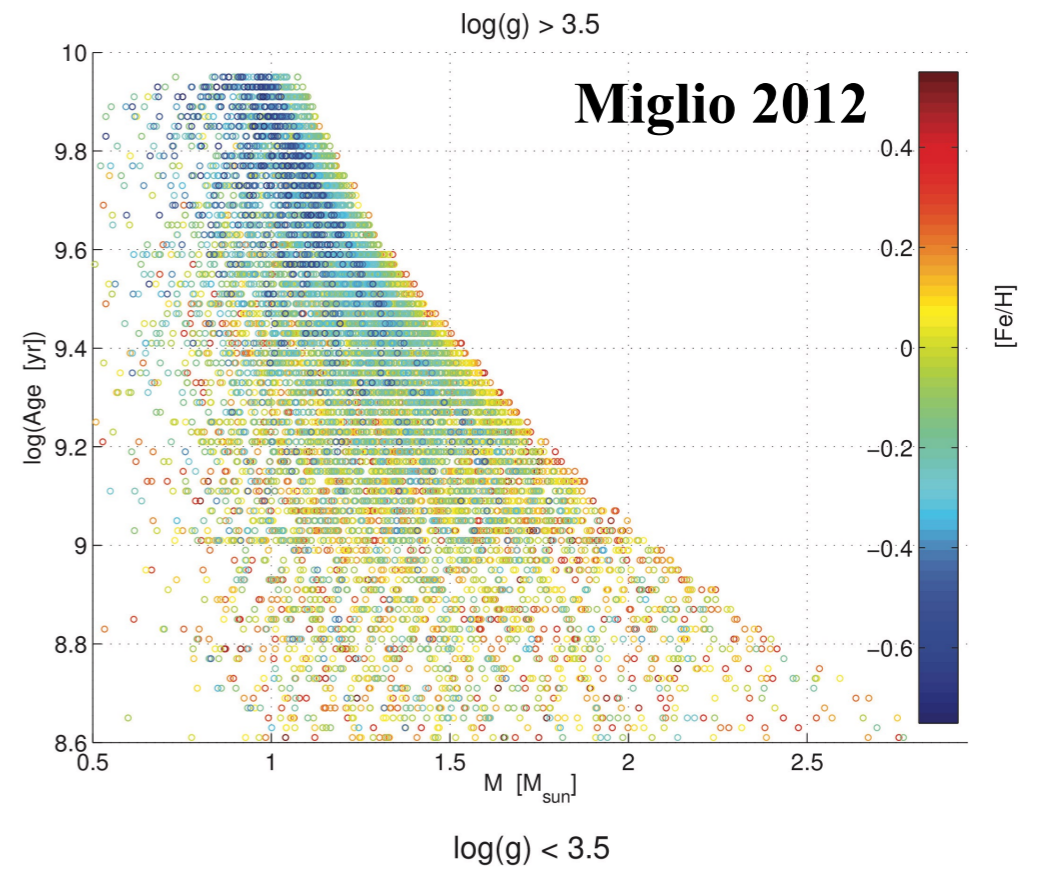
$$\Delta\nu \propto \left(\frac{M}{R^3}\right)^{1/2} \qquad \nu_{\max} \propto \frac{M}{R^2 \sqrt{T_{\text{eff}}}}$$

Huber et al. (2017) (also Chen et al. 2017)





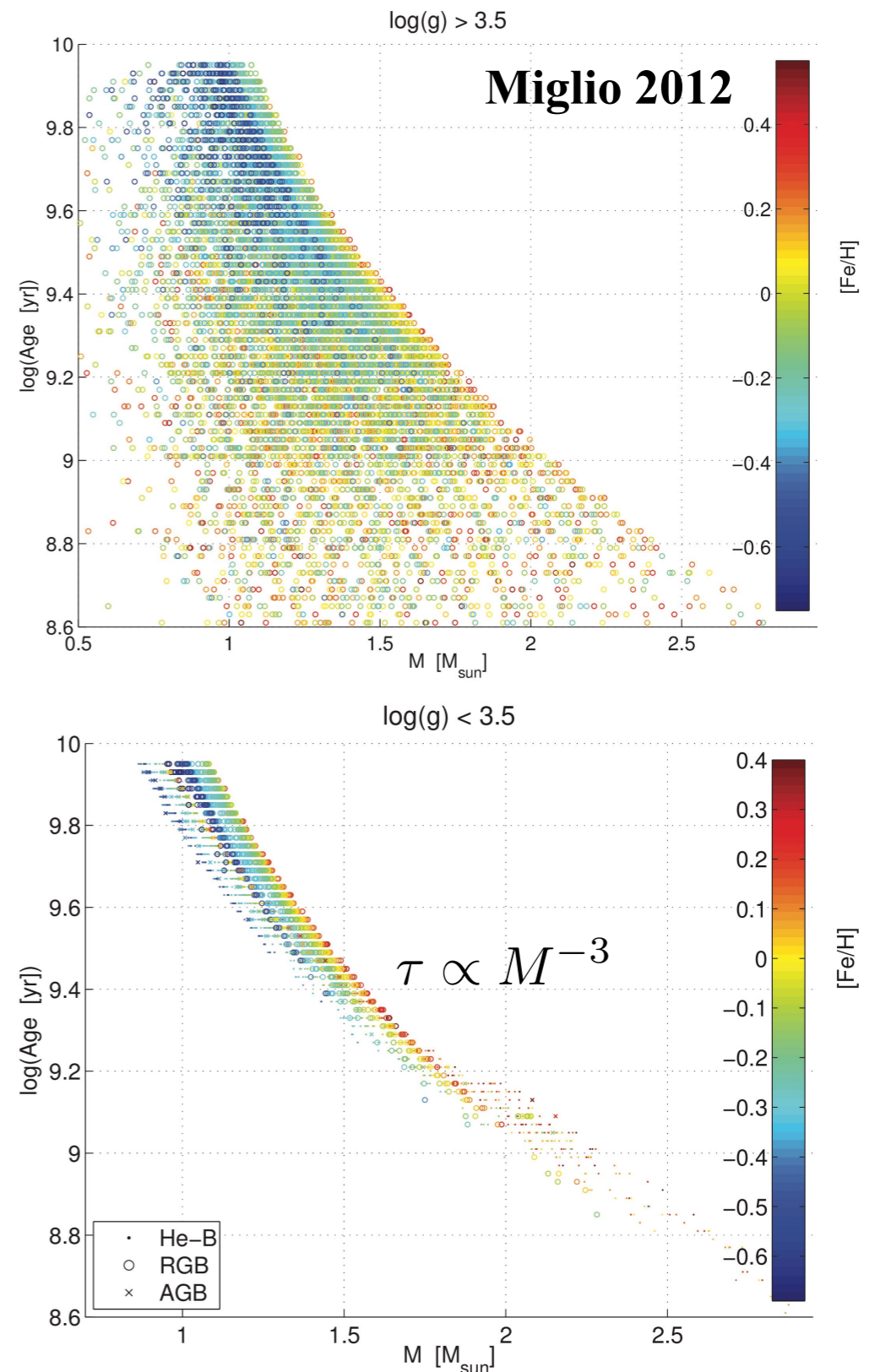
# Mass is an excellent proxy for age





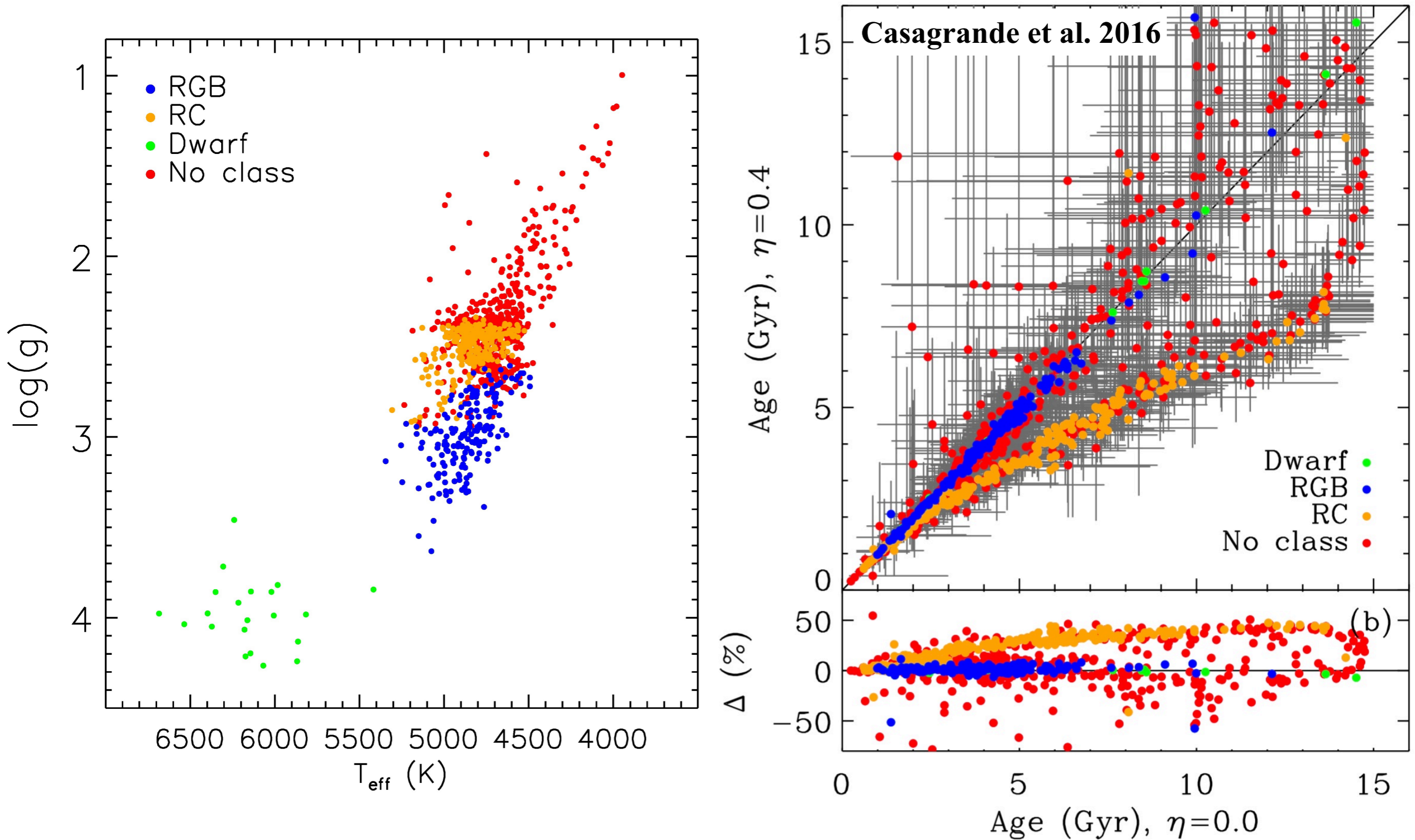
# Mass is an excellent proxy for age

Once a star has evolved to the red-giant phase, its age is determined to good approximation by the time spent in the core-hydrogen burning phase, and this is predominantly a function of mass.





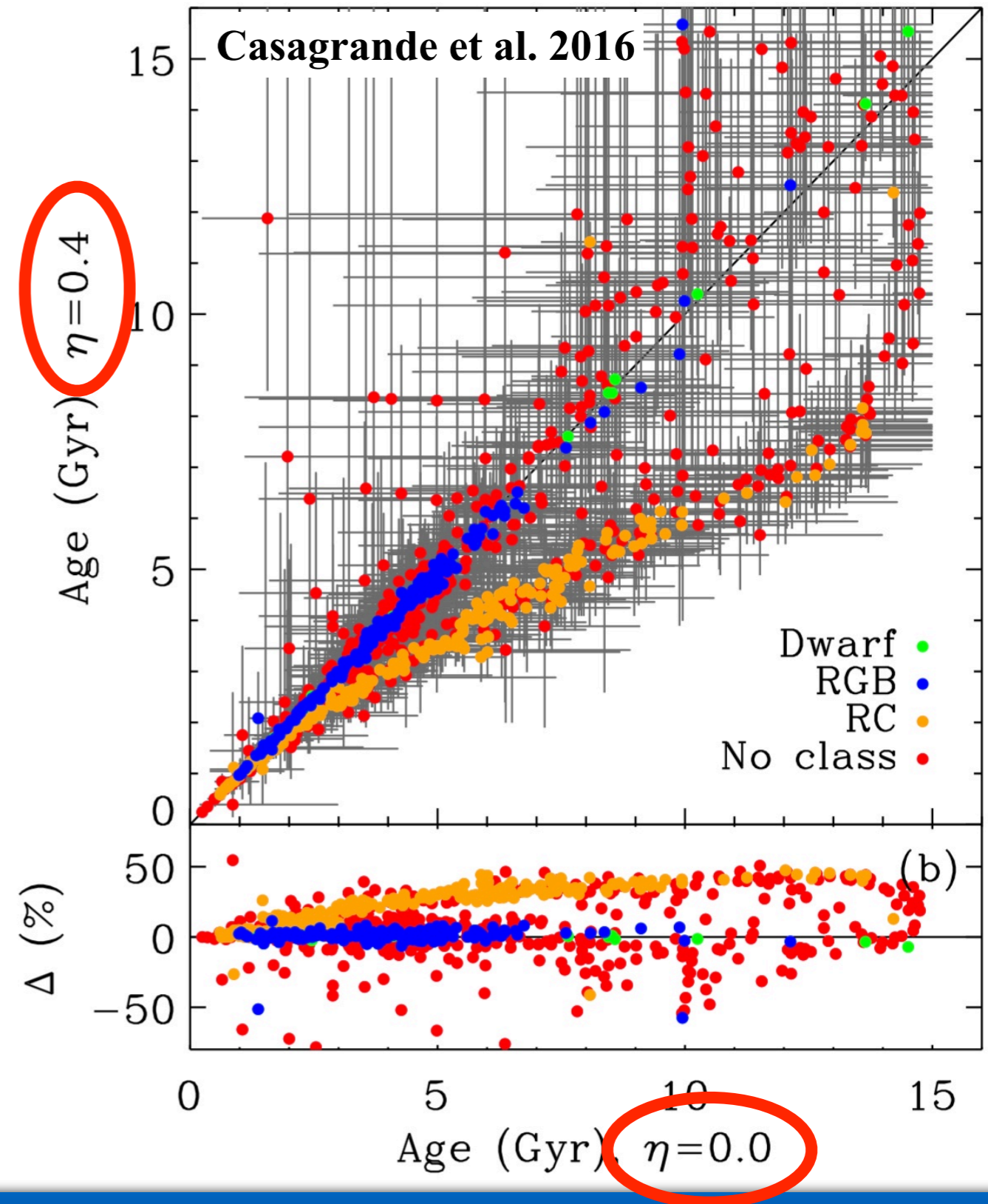
# But RGB stars lose mass!





# But RGB stars lose mass!

Good news is that for disc metallicities, mass-loss seems to be moderate ( $\eta \sim 0.1$  or  $0.2$ , see Miglio et al. 2012, Handberg et al. 2017).

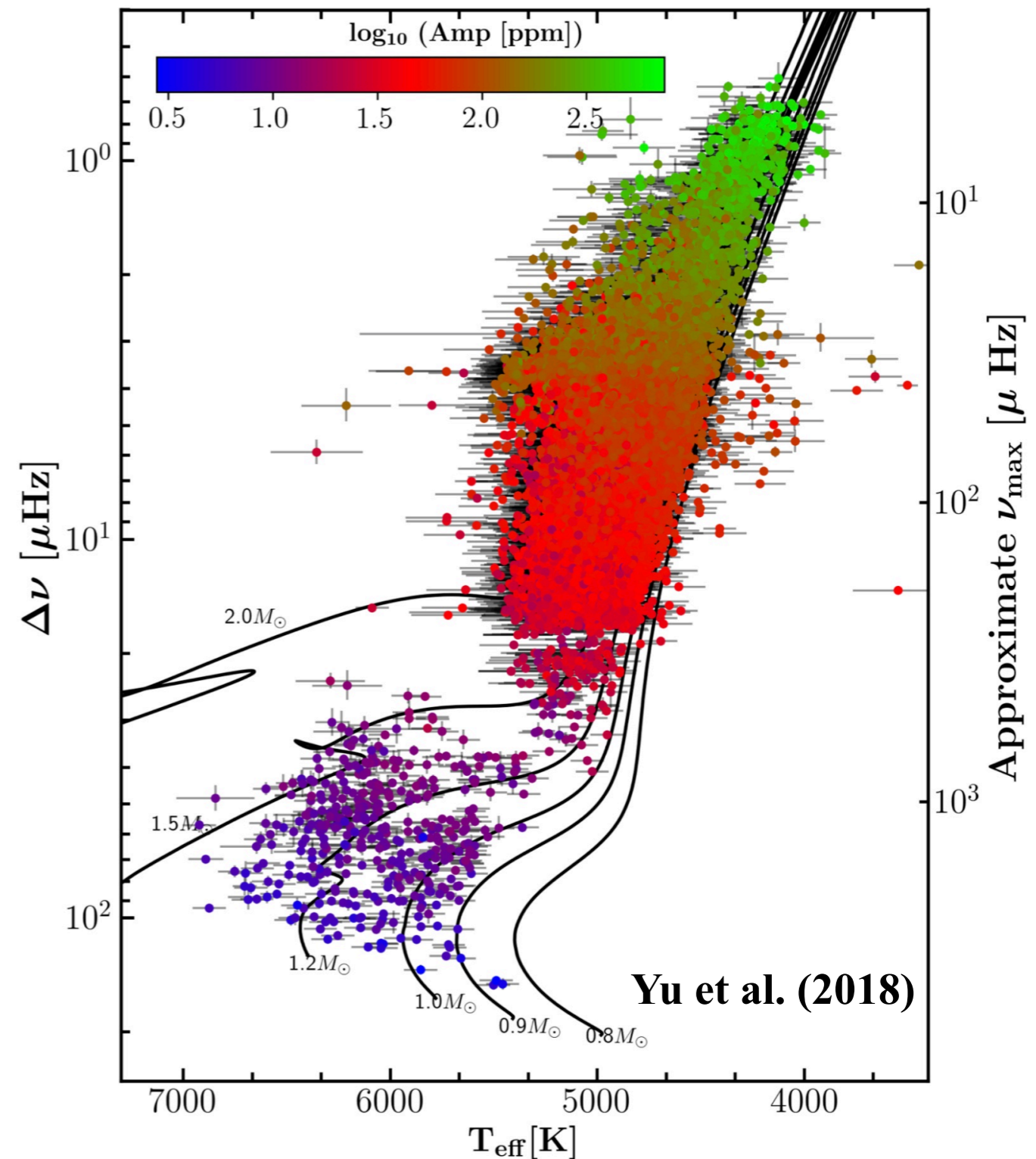




# Scaling relations to rule them all?

$$\frac{M}{M_{\odot}} \approx \left( \frac{\nu_{\max}}{\nu_{\max, \odot}} \right)^3 \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-4} \left( \frac{T_{\text{eff}}}{T_{\text{eff}, \odot}} \right)^{3/2}$$

$$\frac{R}{R_{\odot}} \approx \left( \frac{\nu_{\max}}{\nu_{\max, \odot}} \right) \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-2} \left( \frac{T_{\text{eff}}}{T_{\text{eff}, \odot}} \right)^{1/2}$$





# House of cards?

$$\frac{M}{M_{\odot}} \simeq \left( \frac{\nu_{\max}}{\nu_{\max, \odot}} \right)^3 \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-4} \left( \frac{T_{\text{eff}}}{T_{\text{eff}, \odot}} \right)^{3/2}$$

$$\frac{R}{R_{\odot}} \simeq \left( \frac{\nu_{\max}}{\nu_{\max, \odot}} \right) \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-2} \left( \frac{T_{\text{eff}}}{T_{\text{eff}, \odot}} \right)^{1/2}$$



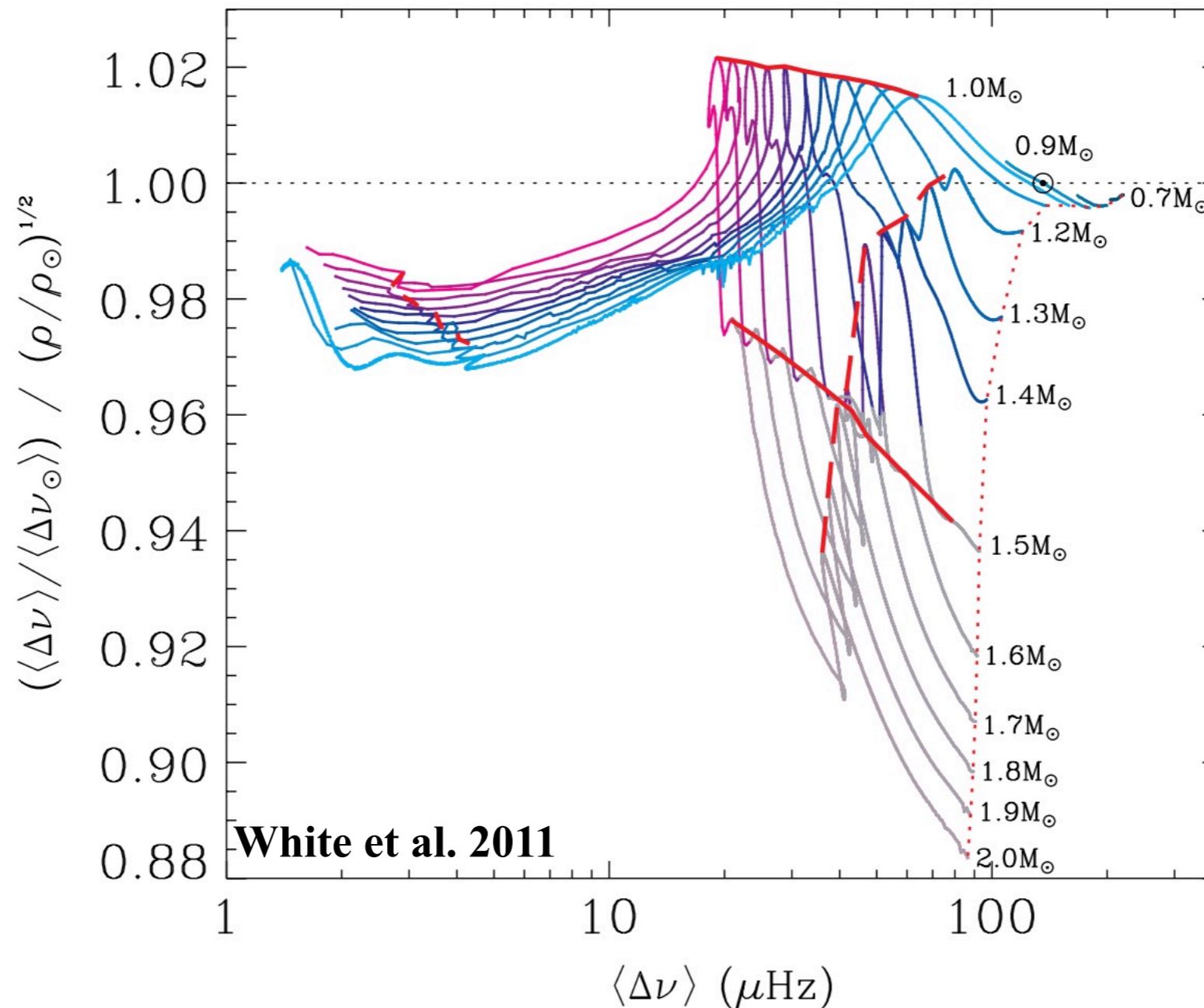
Galactic  
Archaeology

mass  
and  
radius



# The $\Delta\nu$ scaling relation

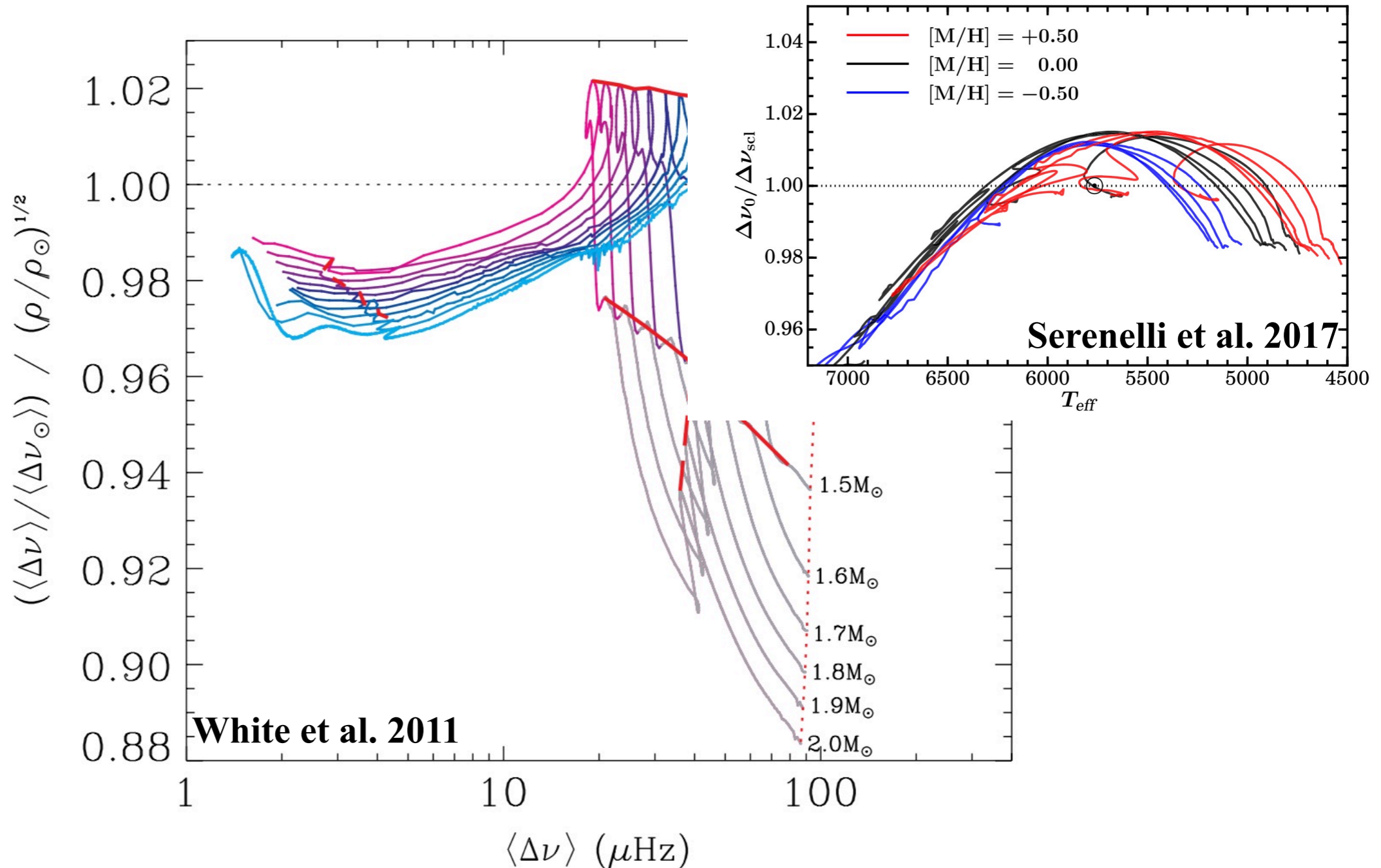
Approximate, but departures well understood from theoretical models.





# The $\Delta\nu$ scaling relation

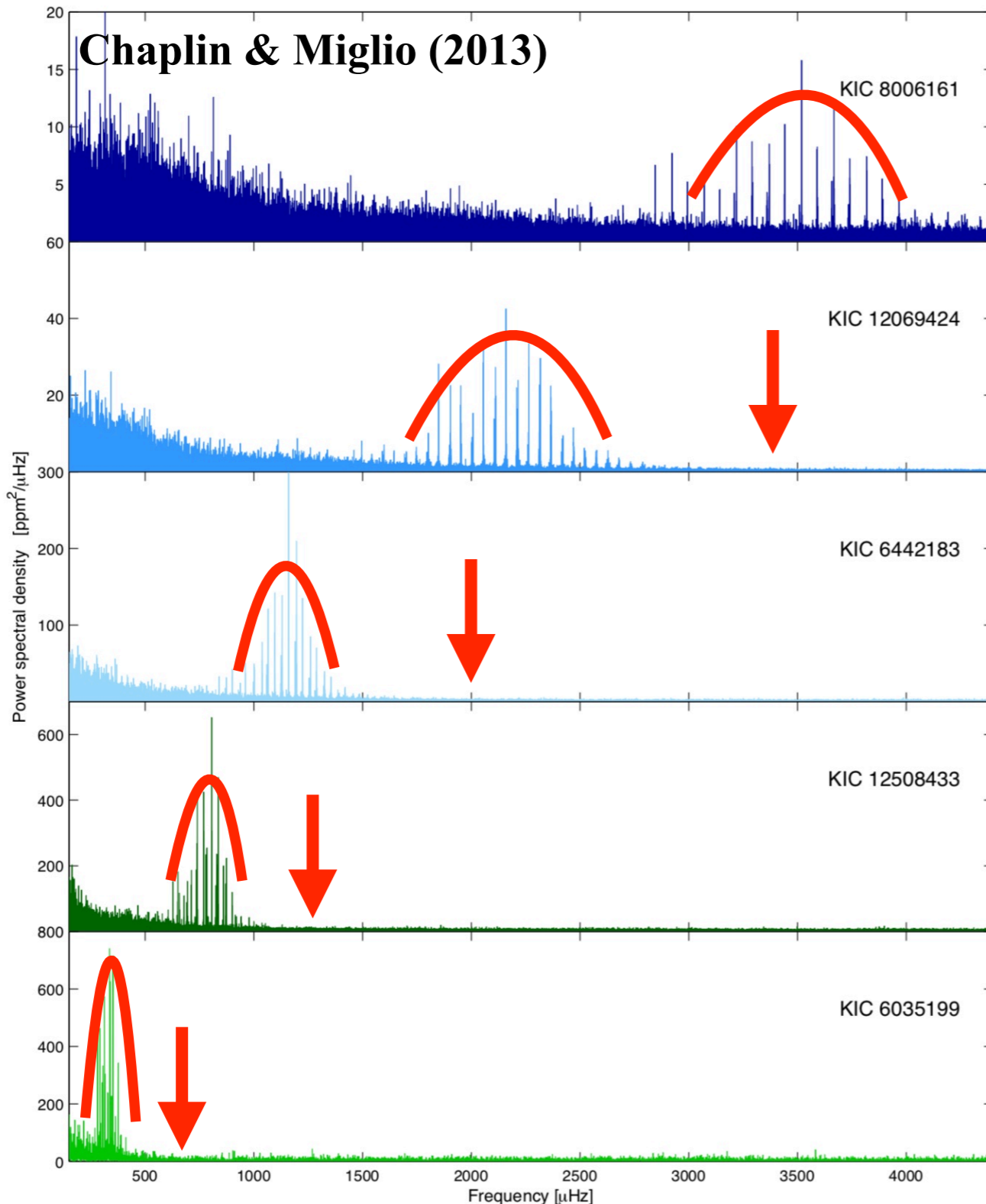
Approximate, but departures well understood from theoretical models.





# The $\nu_{\max}$ scaling relation

decreasing  $\log(g)$



$$\nu_{\max} \propto \nu_{ac} \propto \frac{M}{R^2 \sqrt{T_{\text{eff}}}}$$

Scaling relation *assumes*  $\nu_{\max}$  is a fixed fraction of  $\nu_{ac}$  (Brown et al. 1991).

Surprisingly, it seems to work, although it is not fully understood why! However, see Belkacem et al. (2011), Zhou et al. (2018).

# Corrections to scaling relations

$$\begin{aligned}
 \frac{M}{M_{\odot}} &\simeq \left( \frac{\nu_{\max}}{\nu_{\max,\odot}} \right)^3 \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-4} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{3/2} \\
 \frac{R}{R_{\odot}} &\simeq \left( \frac{\nu_{\max}}{\nu_{\max,\odot}} \right)^2 \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-2} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{1/2}
 \end{aligned}$$

The diagram shows two equations. A red arrow labeled  $f_{\nu_{\max}}$  points from the  $\left( \frac{\nu_{\max}}{\nu_{\max,\odot}} \right)$  term in the first equation to the same term in the second equation. A blue arrow labeled  $f_{\Delta\nu}$  points from the  $\left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)$  term in the first equation to the same term in the second equation.

No correction applied to  $\nu_{\max}$  scaling relation due to its poor theoretical understanding.

Various corrections to  $\Delta\nu$  scaling relation are nowadays used in the literature (e.g., White et al. 2011, Sharma et al. 2016, Guggenberger et al. 2016, Kallinger et al. 2018, Serenelli et al. 2018).



# Testing of scaling relations

$$\frac{M}{M_{\odot}} \simeq \left( \frac{\nu_{\max}}{\nu_{\max, \odot}} \right)^3 \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-4} \left( \frac{T_{\text{eff}}}{T_{\text{eff}, \odot}} \right)^{3/2}$$

$$\frac{R}{R_{\odot}} \simeq \left( \frac{\nu_{\max}}{\nu_{\max, \odot}} \right) \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-2} \left( \frac{T_{\text{eff}}}{T_{\text{eff}, \odot}} \right)^{1/2}$$

The validity of this relation has been tested in several ways by means of interferometry and/or astrometric distances:

Huber et al. (2012, 2017),  
Silva Aguirre et al. (2012),  
Chen et al. (2017),  
Sahlholdt et al. (2019).

**Accuracy < 5%**

# Testing of scaling relations

$$\frac{M}{M_{\odot}} \simeq \left( \frac{\nu_{\max}}{\nu_{\max, \odot}} \right)^3 \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-4} \left( \frac{T_{\text{eff}}}{T_{\text{eff}, \odot}} \right)^{3/2}$$

$$\frac{R}{R_{\odot}} \simeq \left( \frac{\nu_{\max}}{\nu_{\max, \odot}} \right) \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-2} \left( \frac{T_{\text{eff}}}{T_{\text{eff}, \odot}} \right)^{1/2}$$

Testing mass is more difficult because of the paucity stars with empirical mass-measurements (eclipsing binaries). Indirect tests are often used:

Epstein et al. (2014),  
 Gaulme et al. (2016),  
 Miglio et al. (2016),  
 Brogaard et al. (2016, 2018)  
 Pinsonneault et al. (2018).

**~10% (i.e. ~30% in age)**

**However, in relative sense, age precision is better than 30%**



# Asteroseismic ages

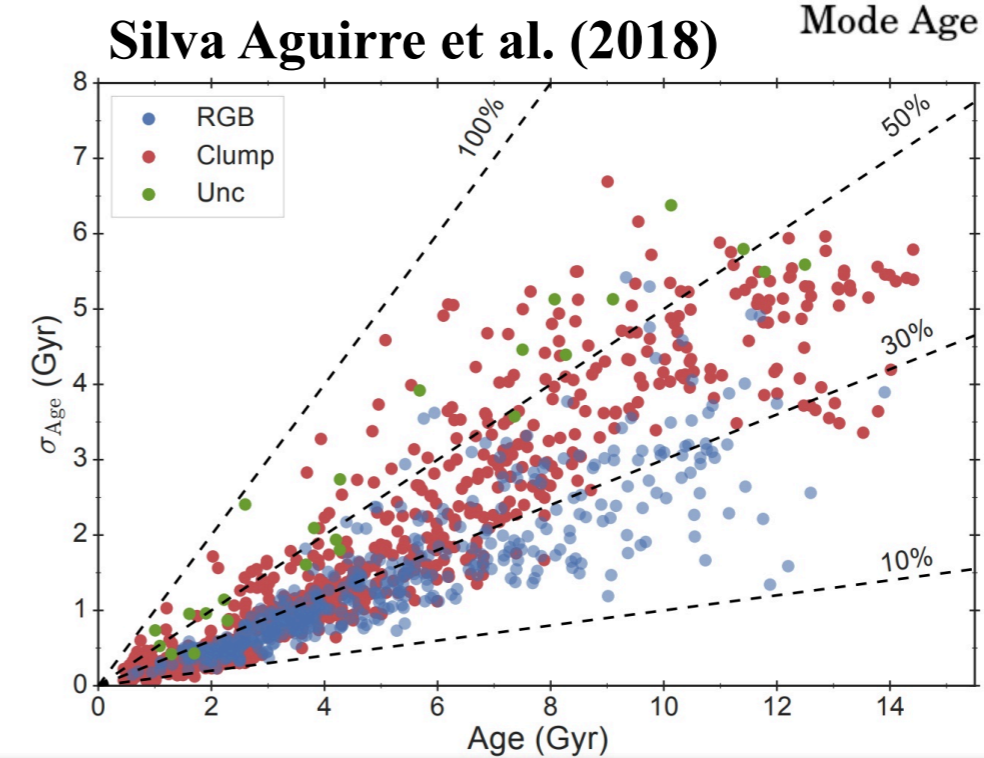
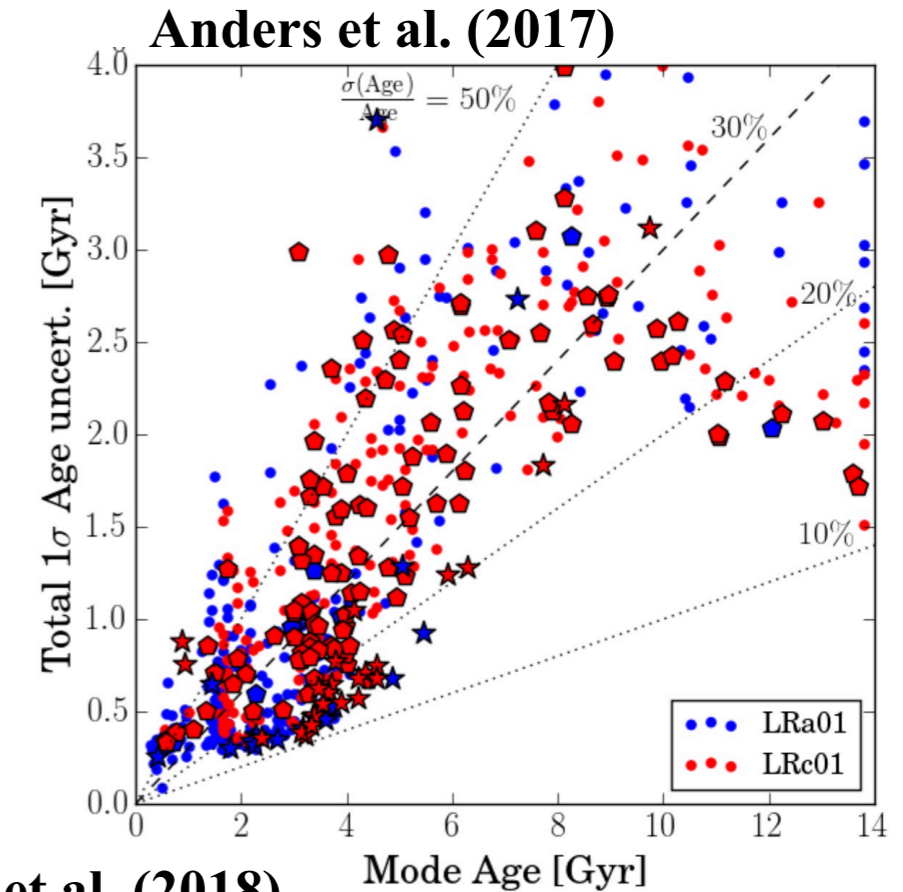
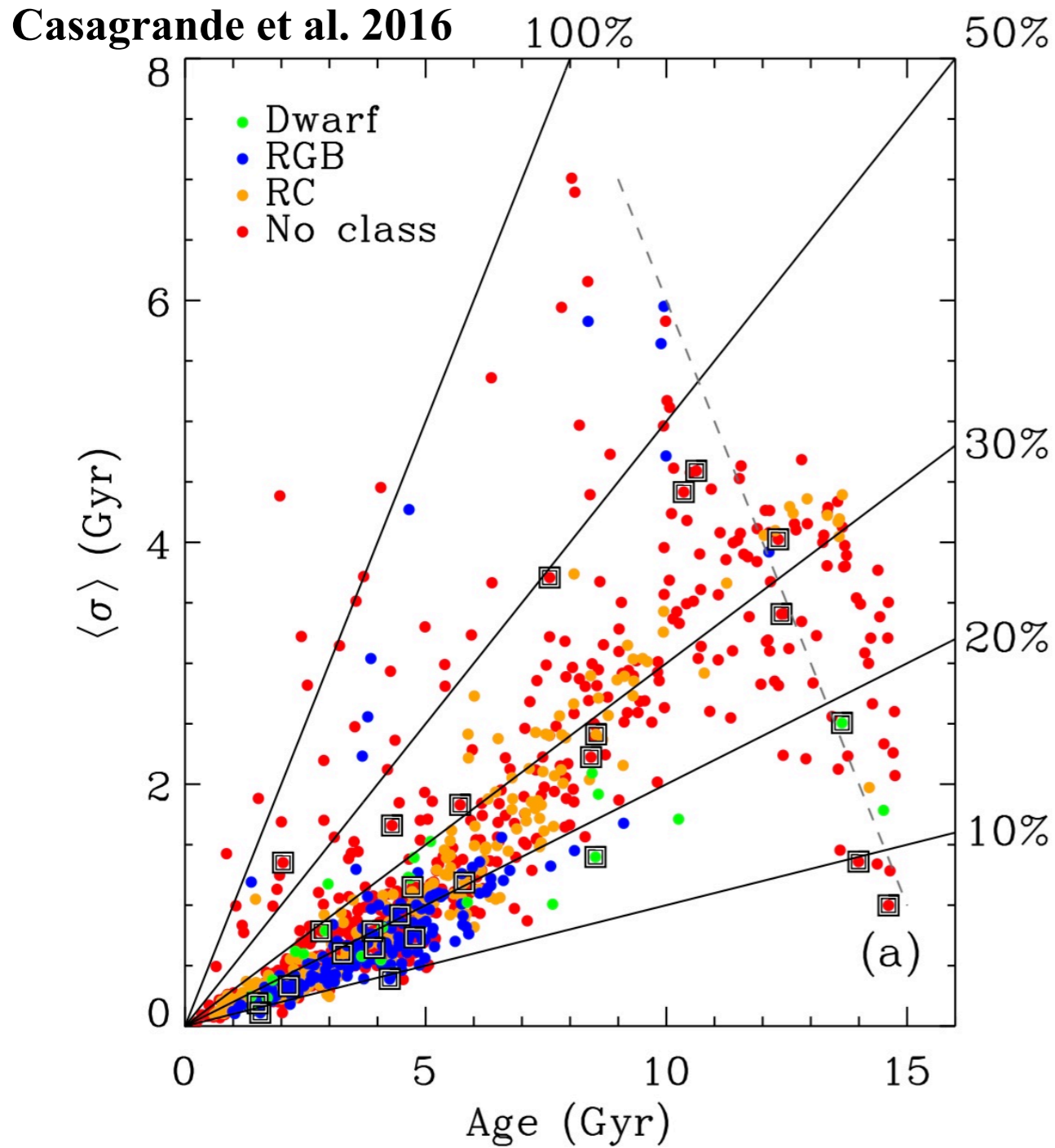
## Scaling relations



Rather than pure scaling relations, grid-based modelling usually adopted (i.e. fitting for  $[\text{Fe}/\text{H}]$ ,  $T_{\text{eff}}$ ,  $\Delta v$ ,  $v_{\text{max}}$ ).



# Uncertainties on asteroseismic ages





# Asteroseismic ages

Scaling relations



Individual frequencies



e.g., Silva Aguirre et al. (2017), Handberg et al. (2017) Buldgen et al. (2018).



# Asteroseismic ages

Scaling relations



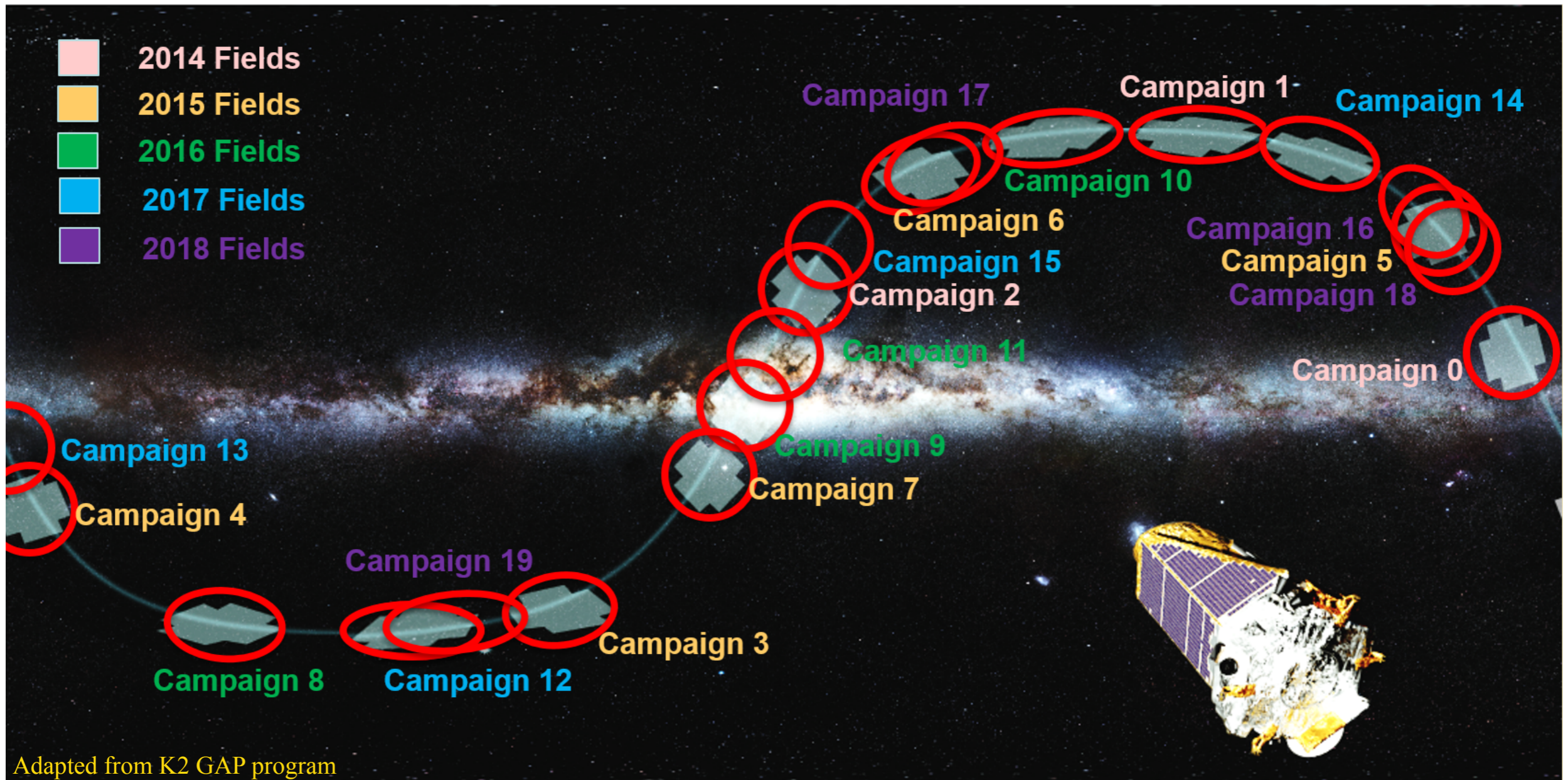
Individual frequencies



e.g., Silva Aguirre et al. (2017), Handberg et al. (2017) Buldgen et al. (2018).



# Data galore

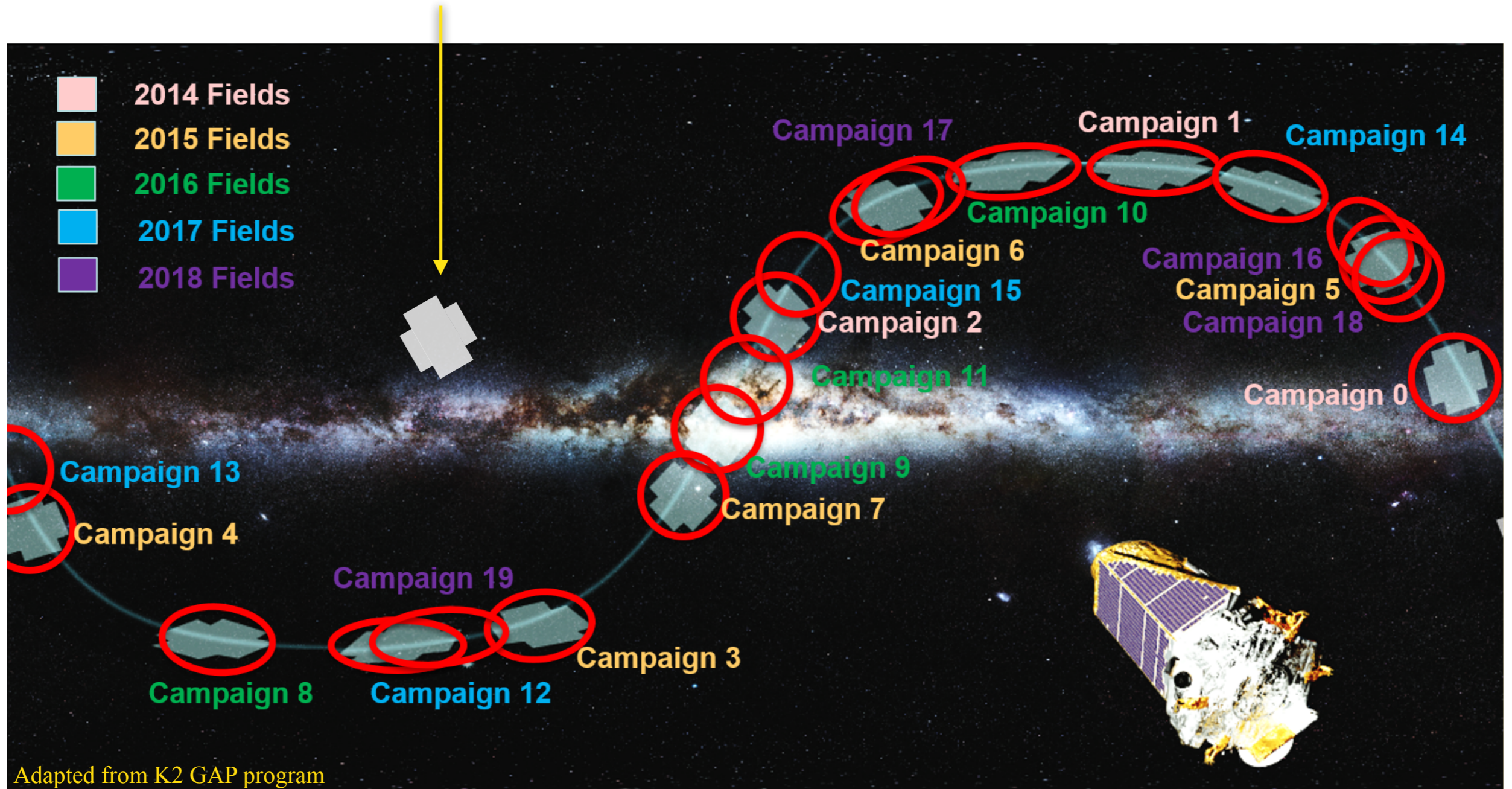


Adapted from K2 GAP program



# Data galore

*Kepler (4 years)*



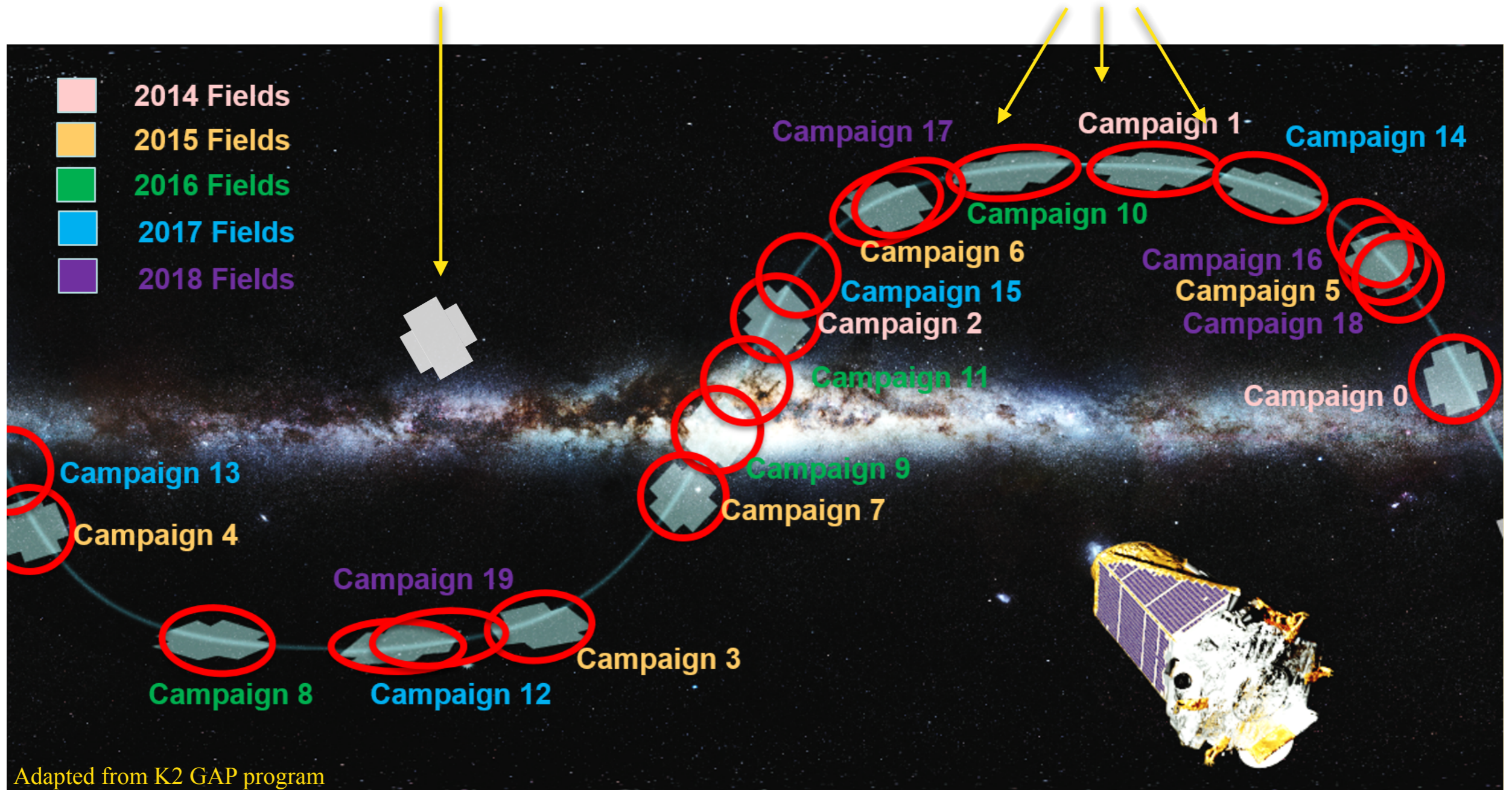
Adapted from K2 GAP program



# Data galore

*Kepler (4 years)*

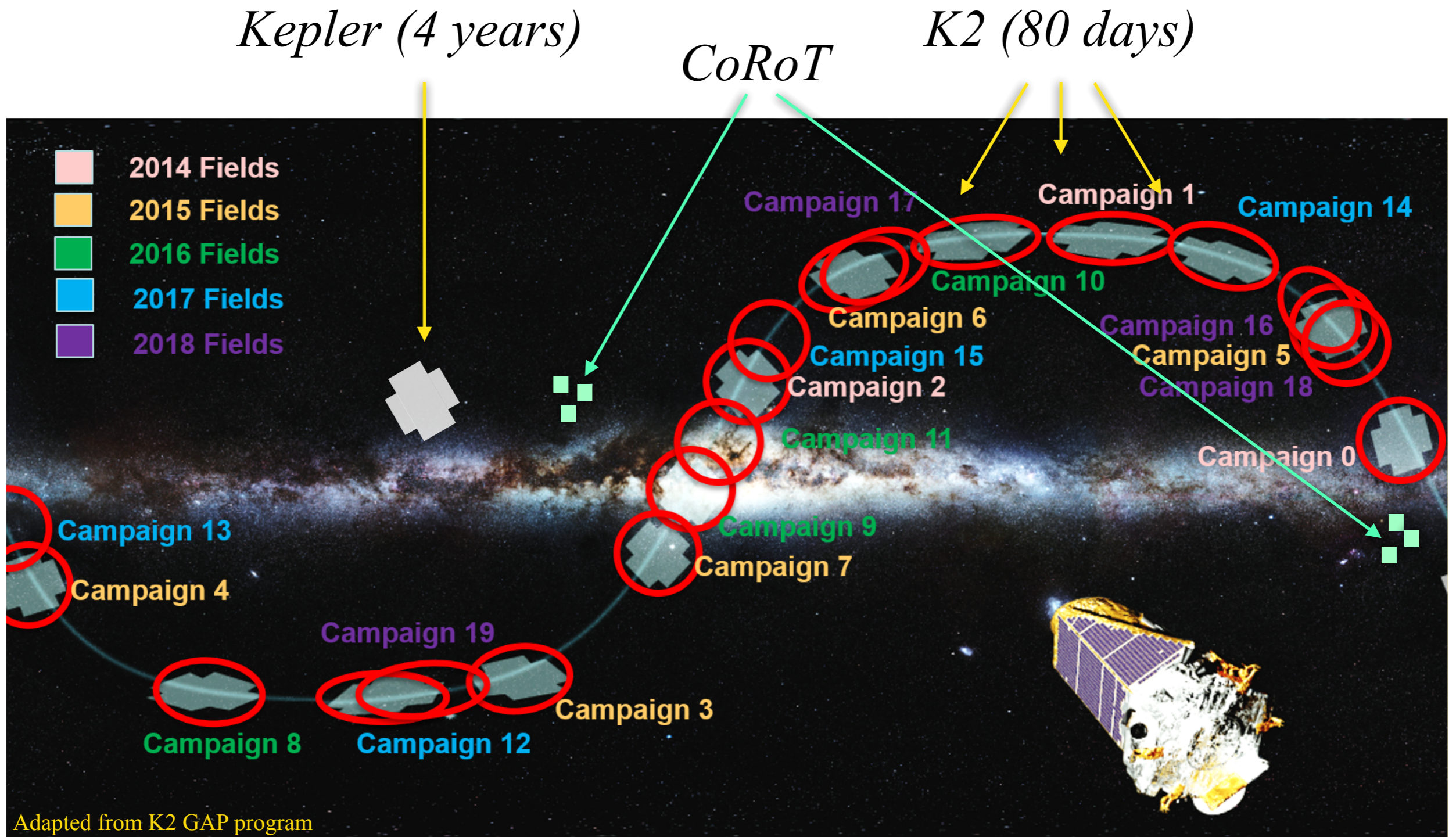
*K2 (80 days)*



Adapted from K2 GAP program



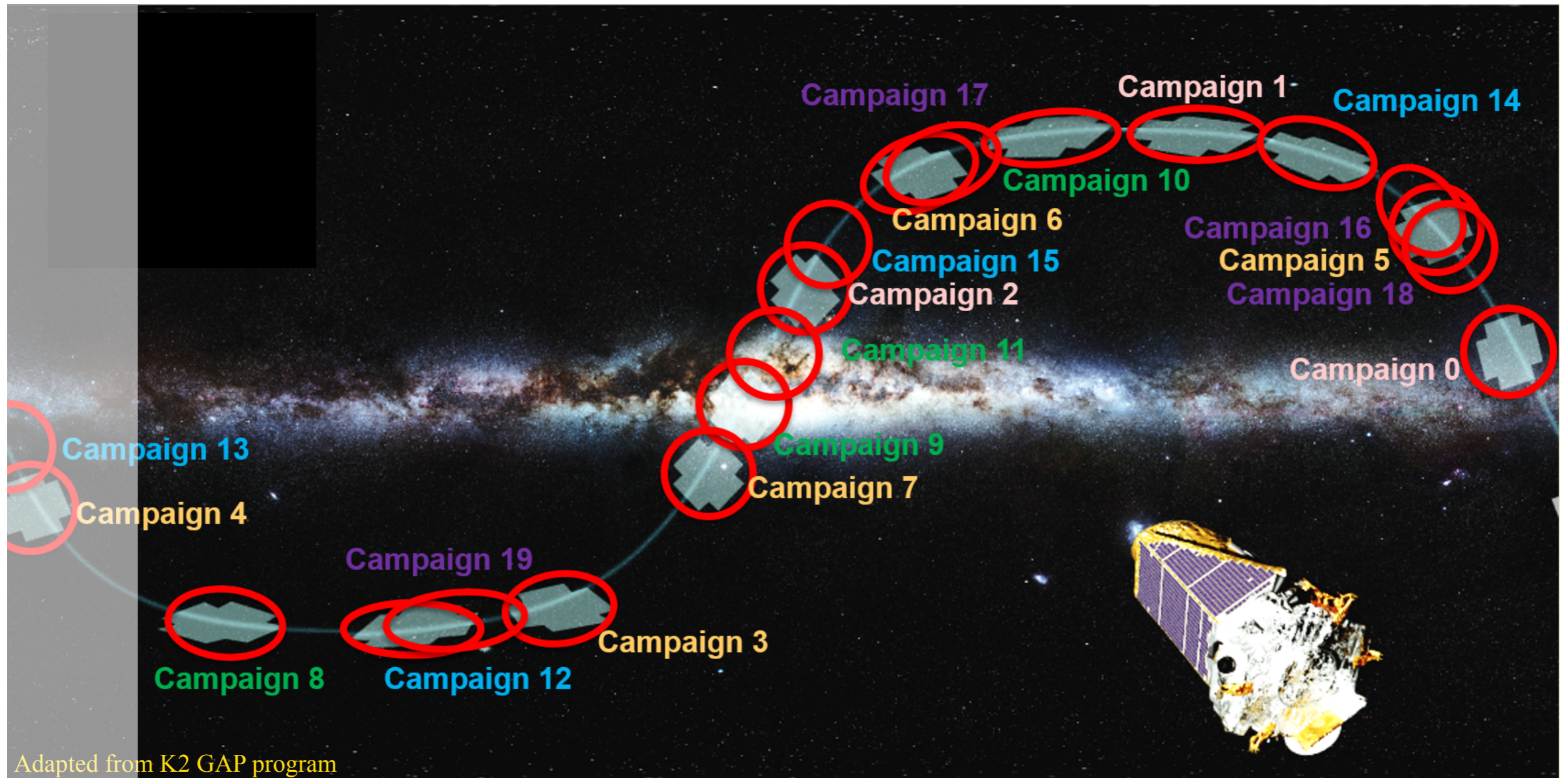
# Data galore





# Data galore

and now much more with TESS!

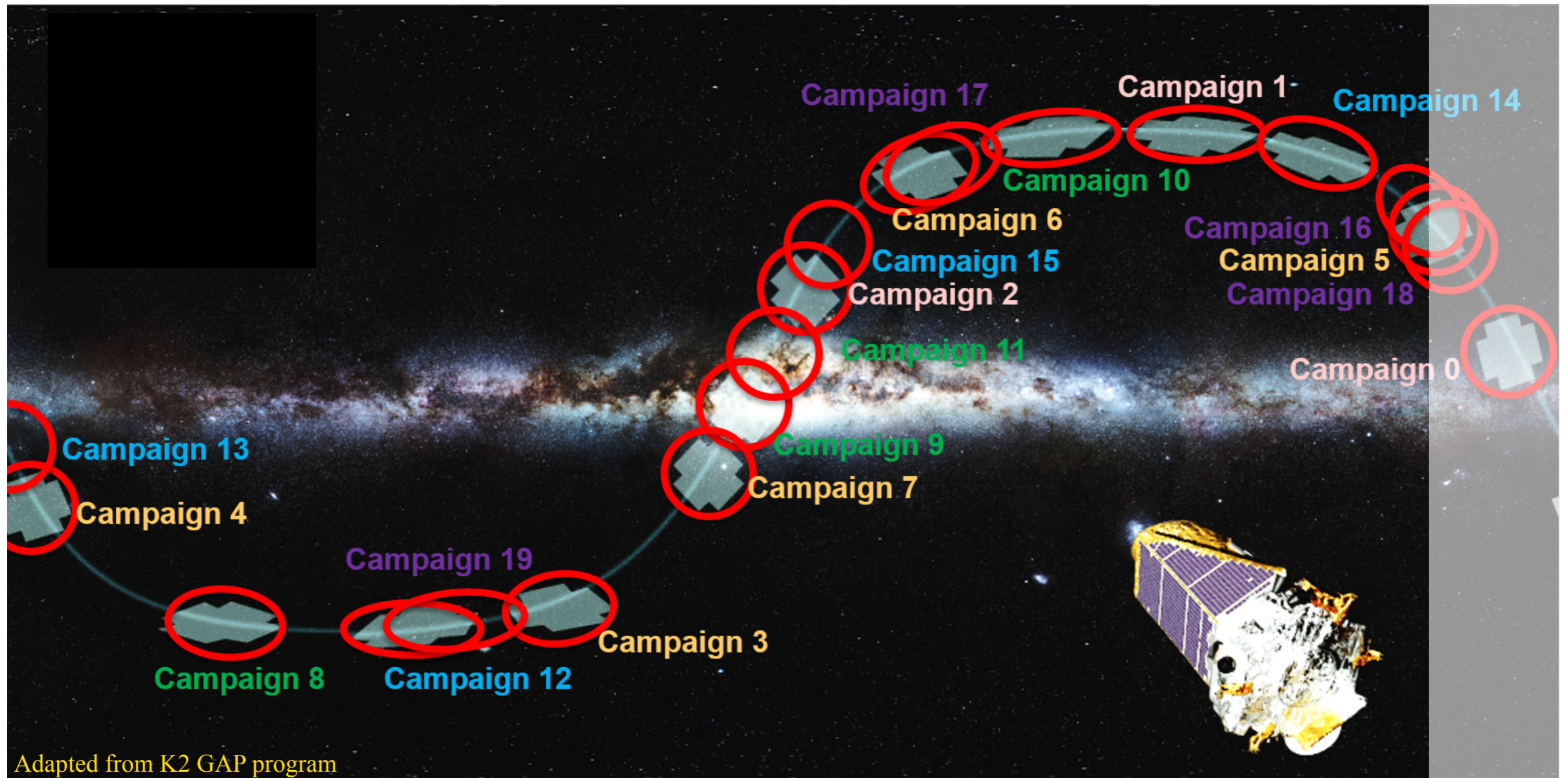


Adapted from K2 GAP program



# Data galore

and now much more with TESS!

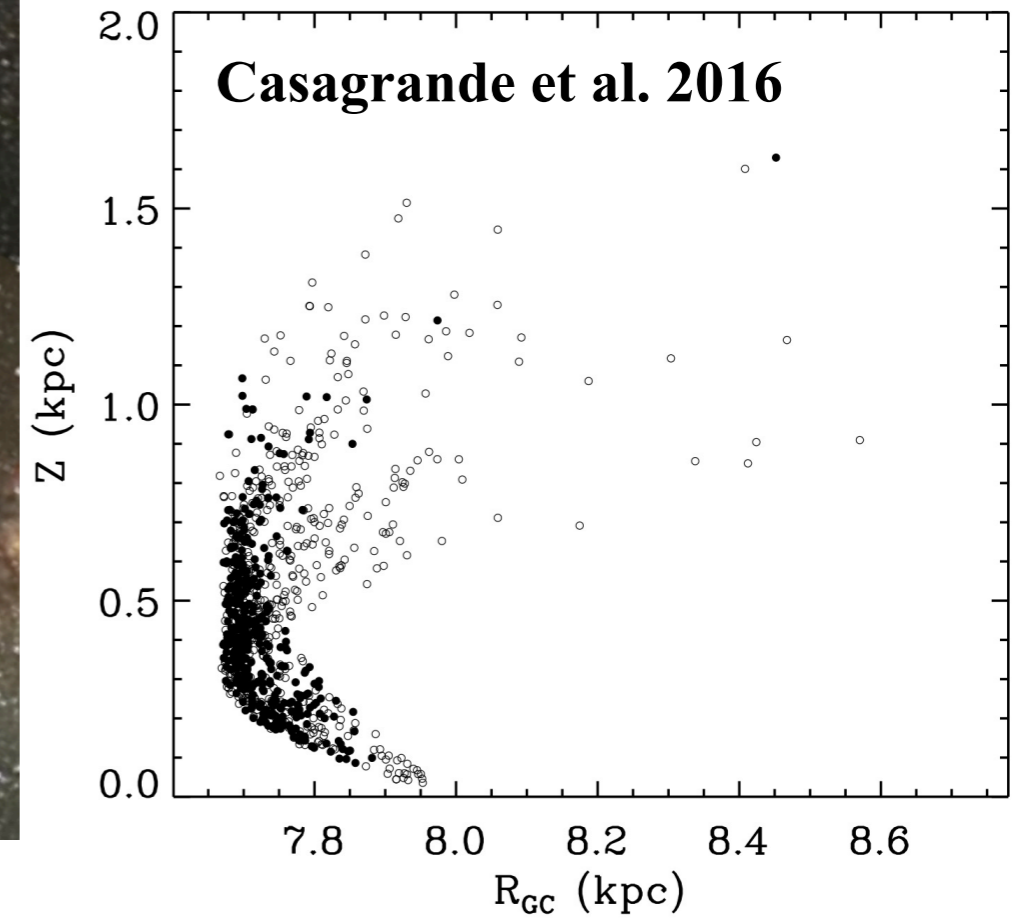


Adapted from K2 GAP program



# Kepler field

Nearly constant Galactocentric radius, thus making it ideal to study the vertical structure of the disc.







# Strömgren surveys for Asteroseismology

Casagrande et al. (2014, 2016)

There was not a selection function for Kepler seismic targets (only for exoplanets).

Photometric surveys on the INT telescope, to derive stellar parameters, and to recover a proper selection function for seismic targets.

*Kepler*





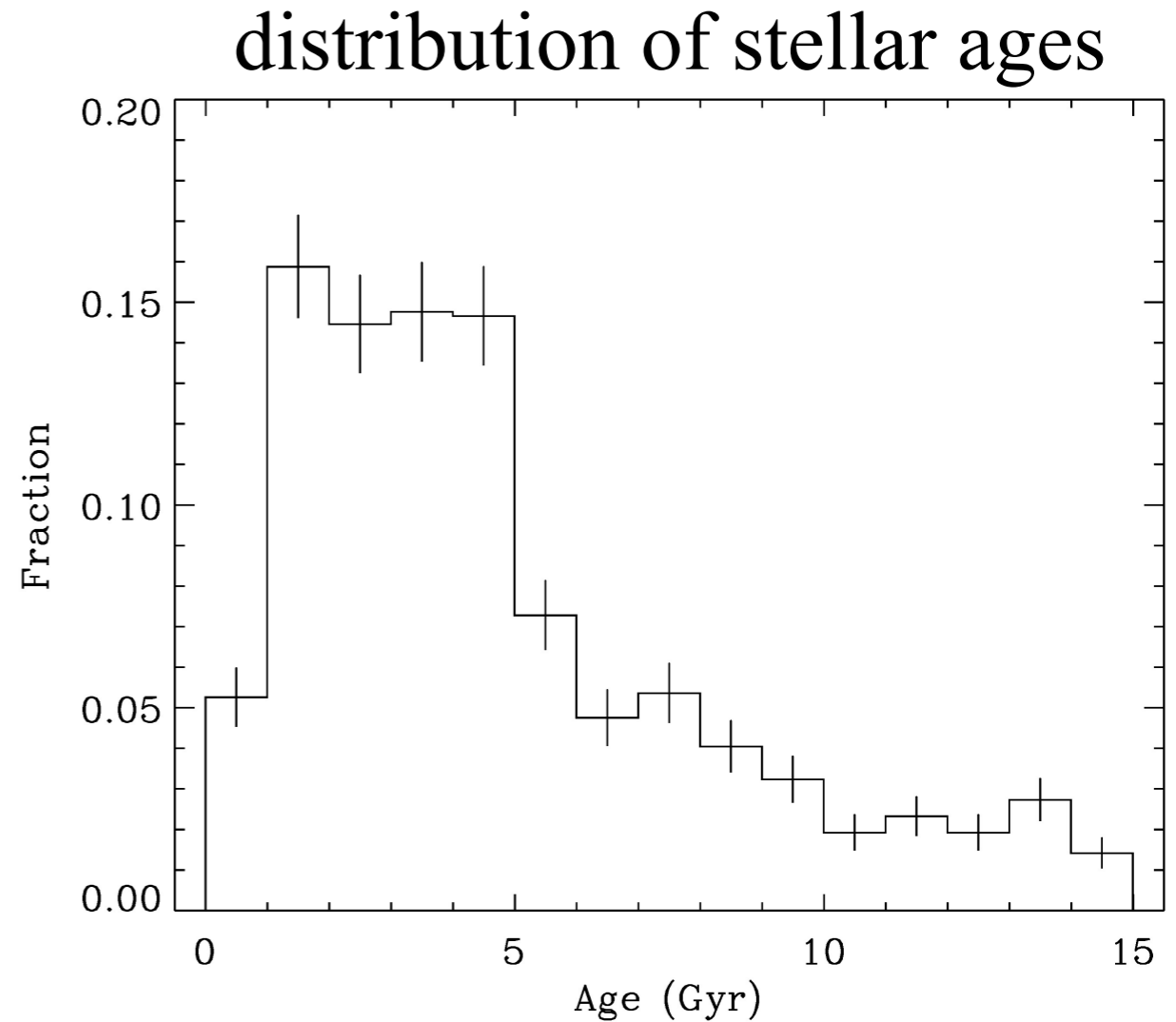


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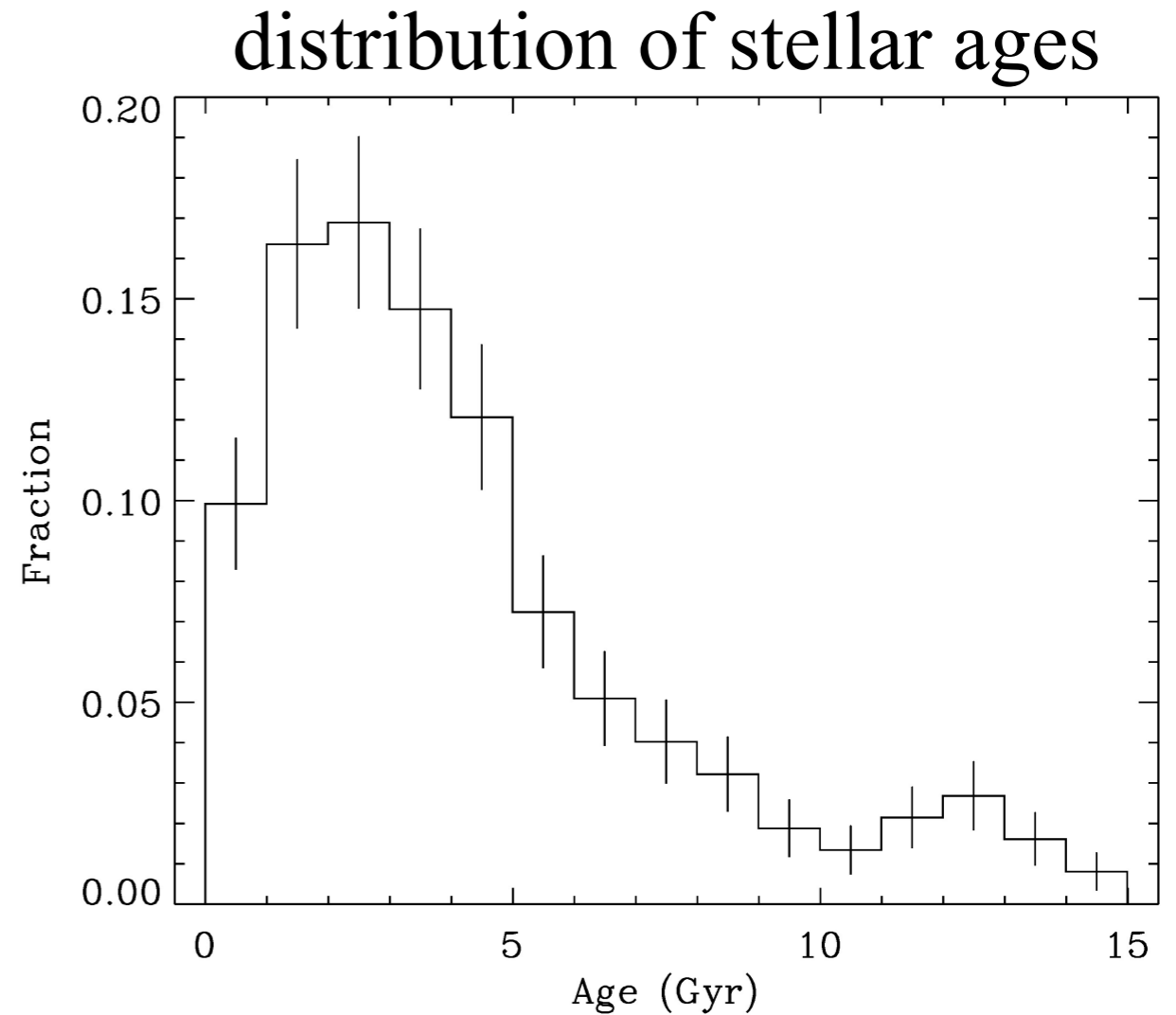
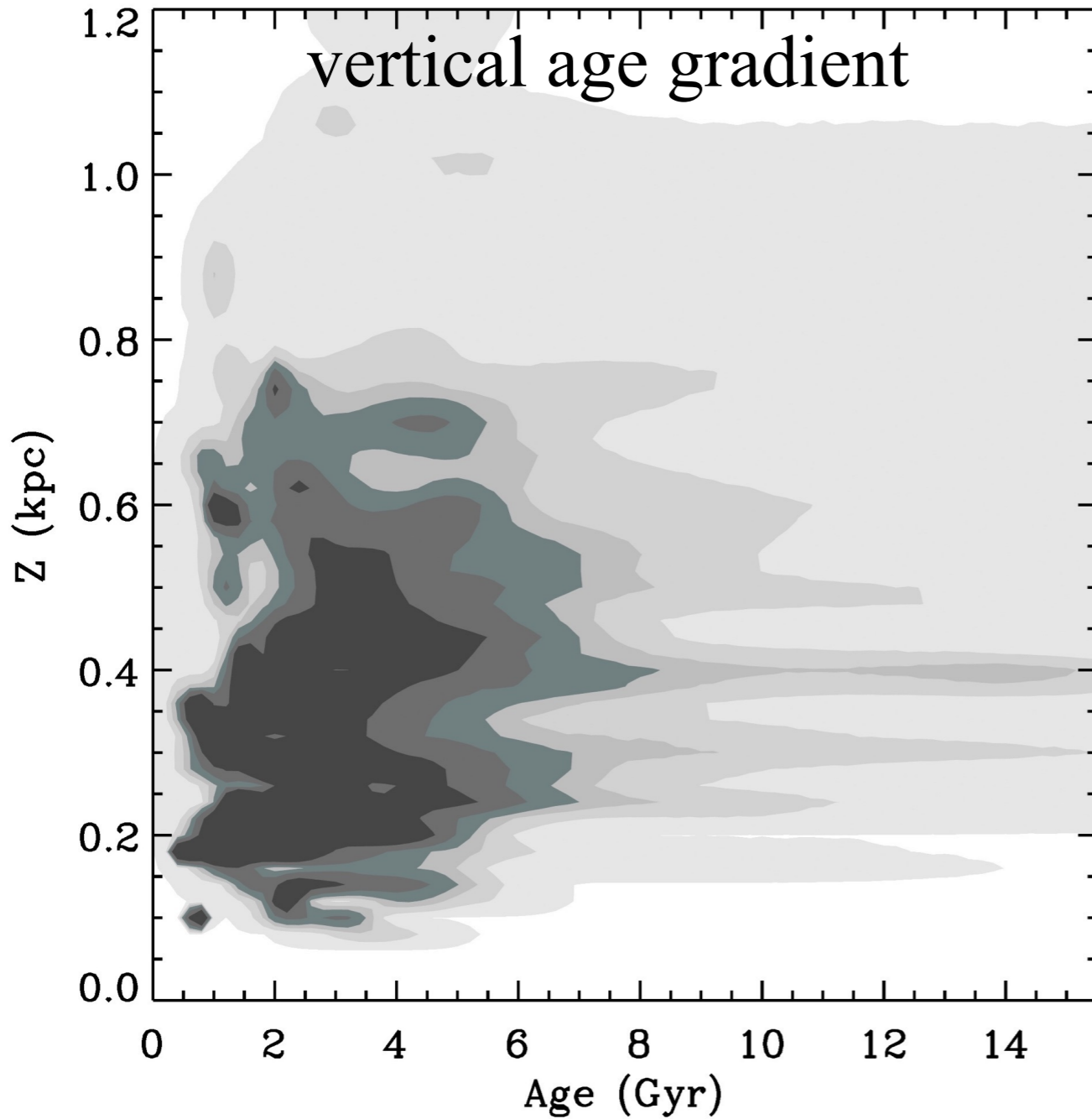






# Strömgren surveys for Asteroseismology

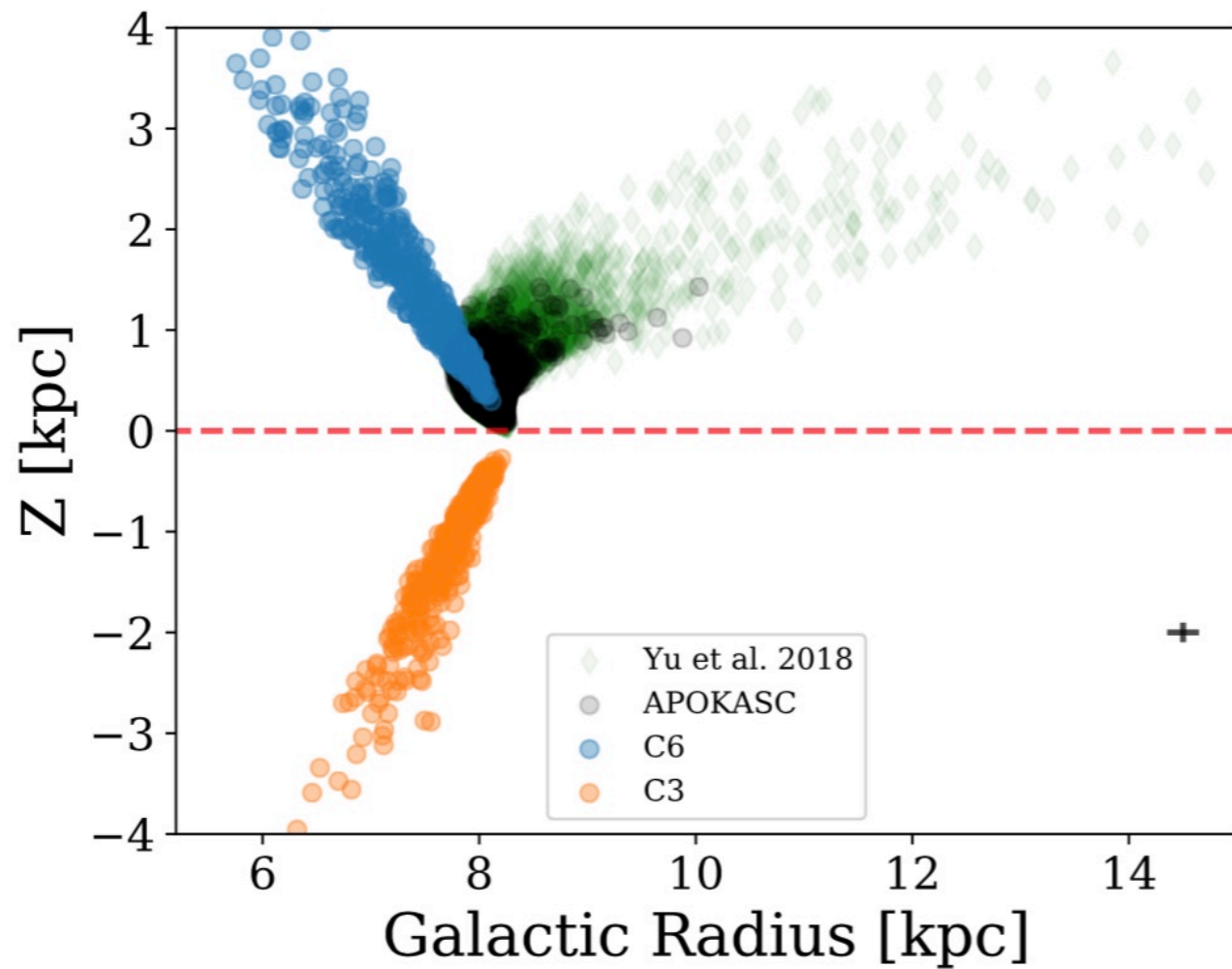
Casagrande et al. (2014, 2016)





# Vertical age structure beyond Kepler

Rendle et al. (submitted)

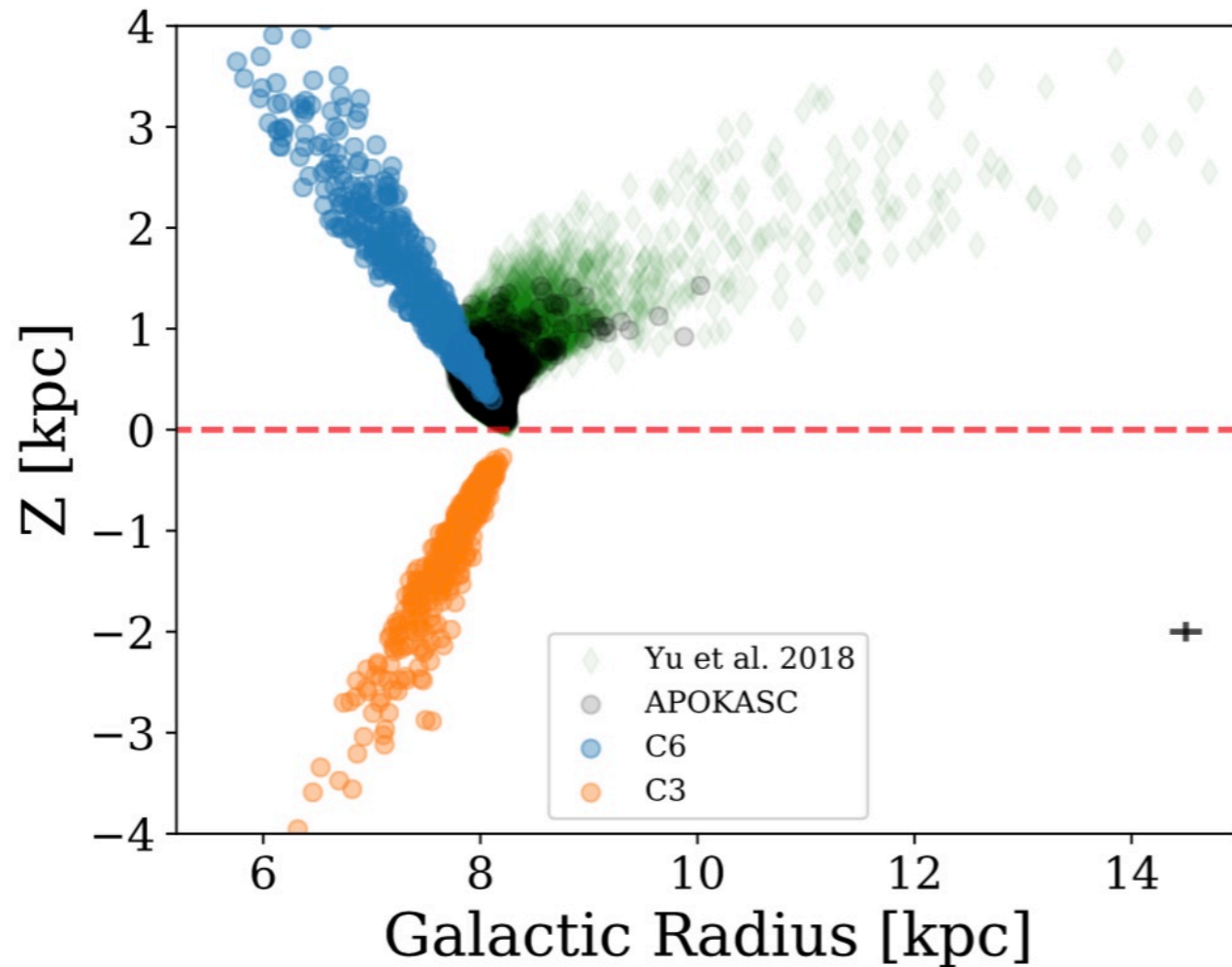


Survey	C3	C6
K2	483	929



# Vertical age structure beyond Kepler

Rendle et al. (submitted)



Survey	C3	C6
K2	483	929
<b>K2 SM</b>	<b>377</b>	<b>646</b>
RAVE	85	83
Gaia-ESO	38	-
APOGEE	101	25
K2 Spec.	128	102

70-80%  
of targets

10-20%  
of targets



# SkyMapper Southern Sky Survey

Wolf et al. (2018), Onken et al. (2019)

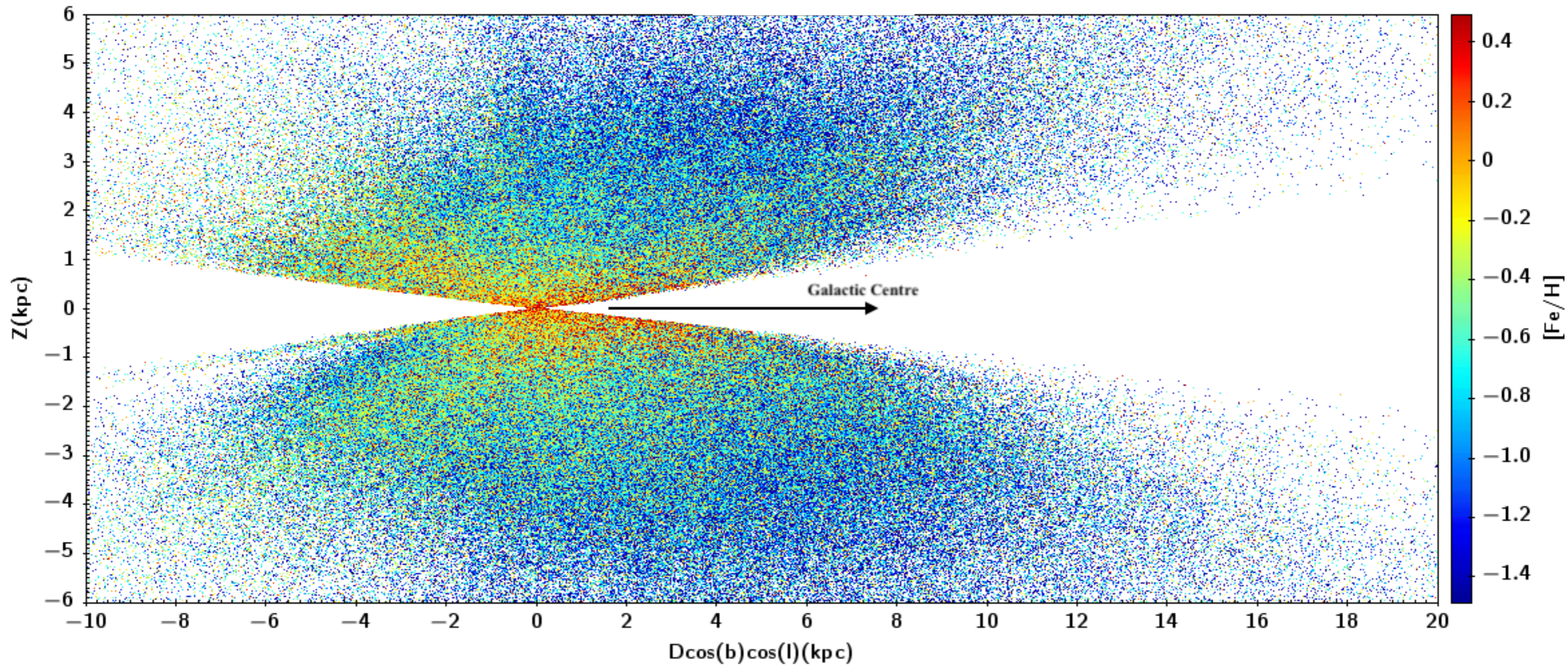


*uvgriz* photometry (300-1000nm) for the entire southern sky.  
Ideal to derive stellar parameters.



# SkyMapper metallicities for 9 million stars

Casagrande et al. (2019)

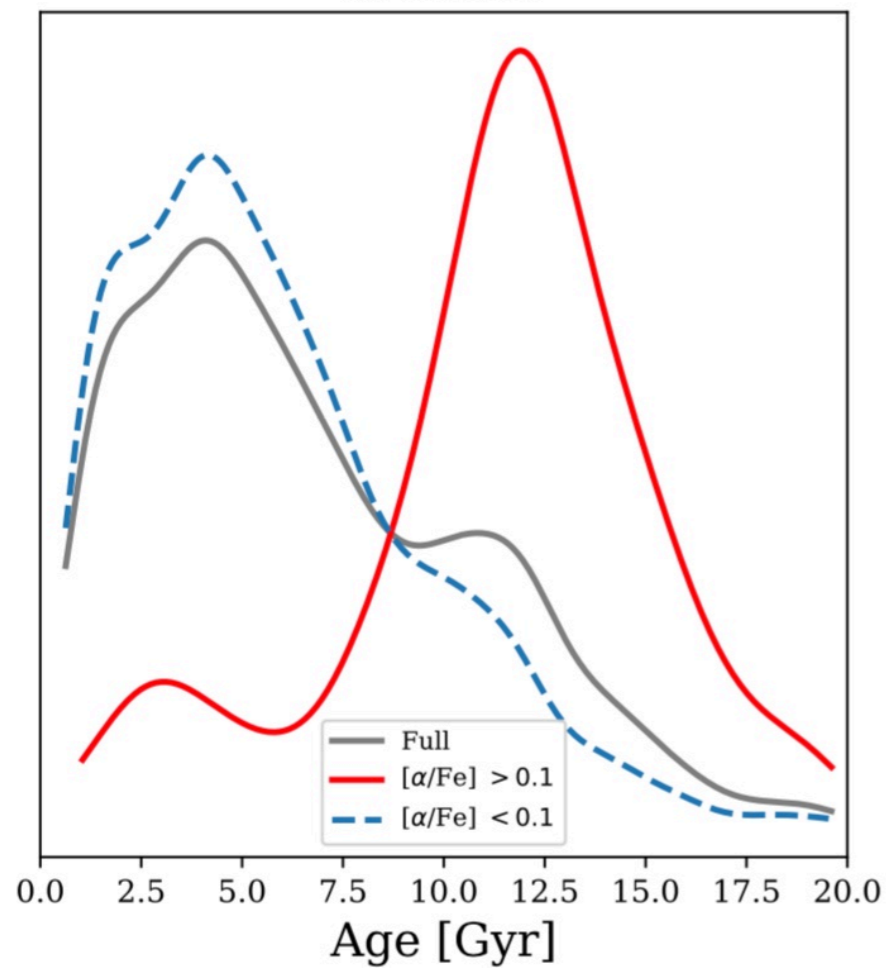




# Vertical age structure beyond Kepler

Rendle et al. (submitted)

APOKASC



all distributions are normalised to equal area



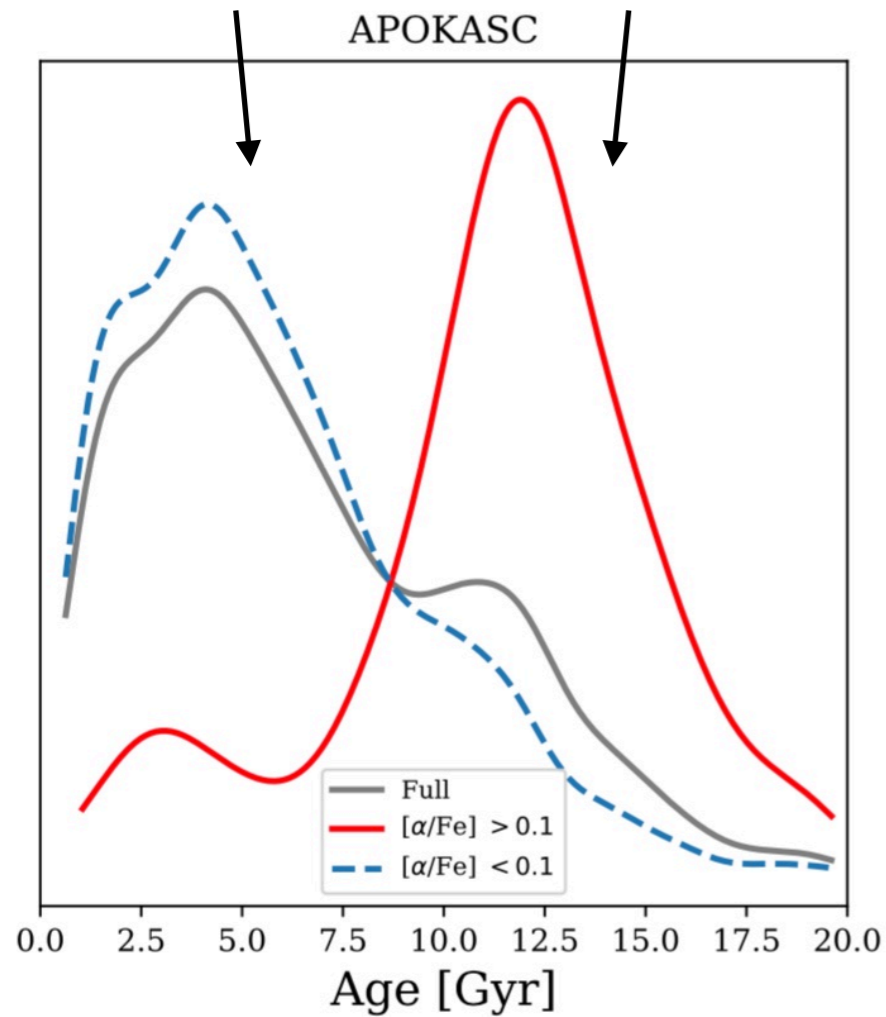
# Vertical age structure beyond Kepler

Rendle et al. (submitted)

thin

thick

see also Silva Aguirre et al. (2018)  
and talk by Jane Lin tomorrow



all distributions are normalised to equal area



# Vertical age structure beyond Kepler

Rendle et al. (submitted)

thin

thick

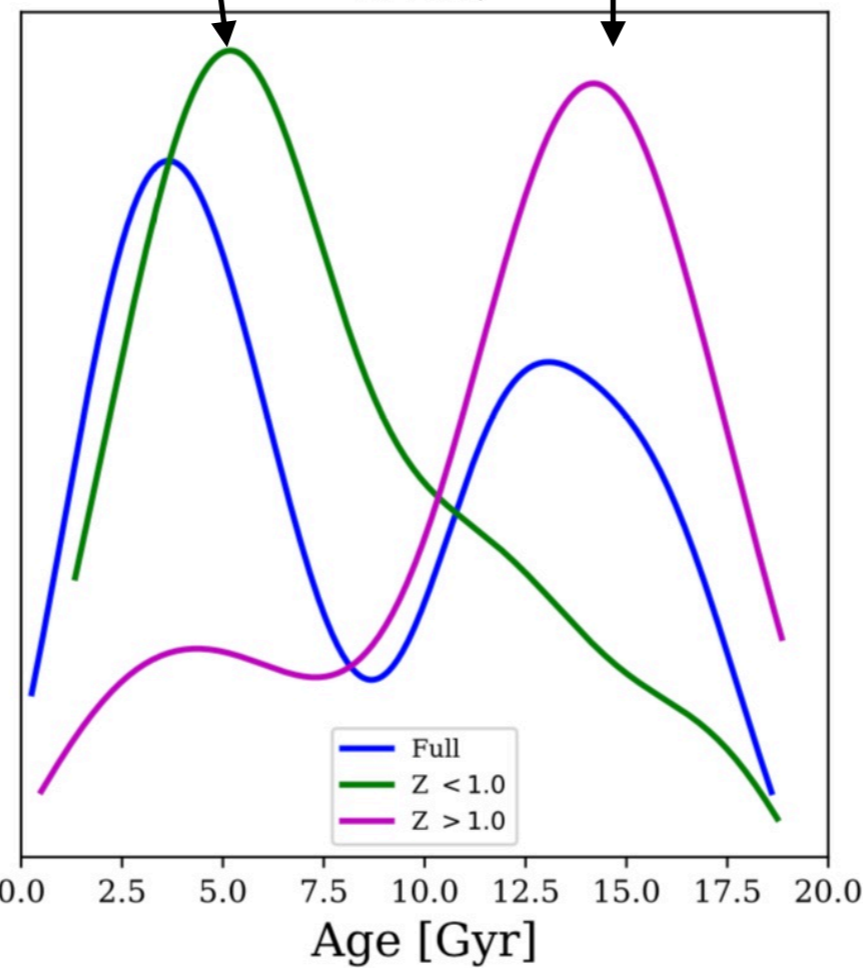
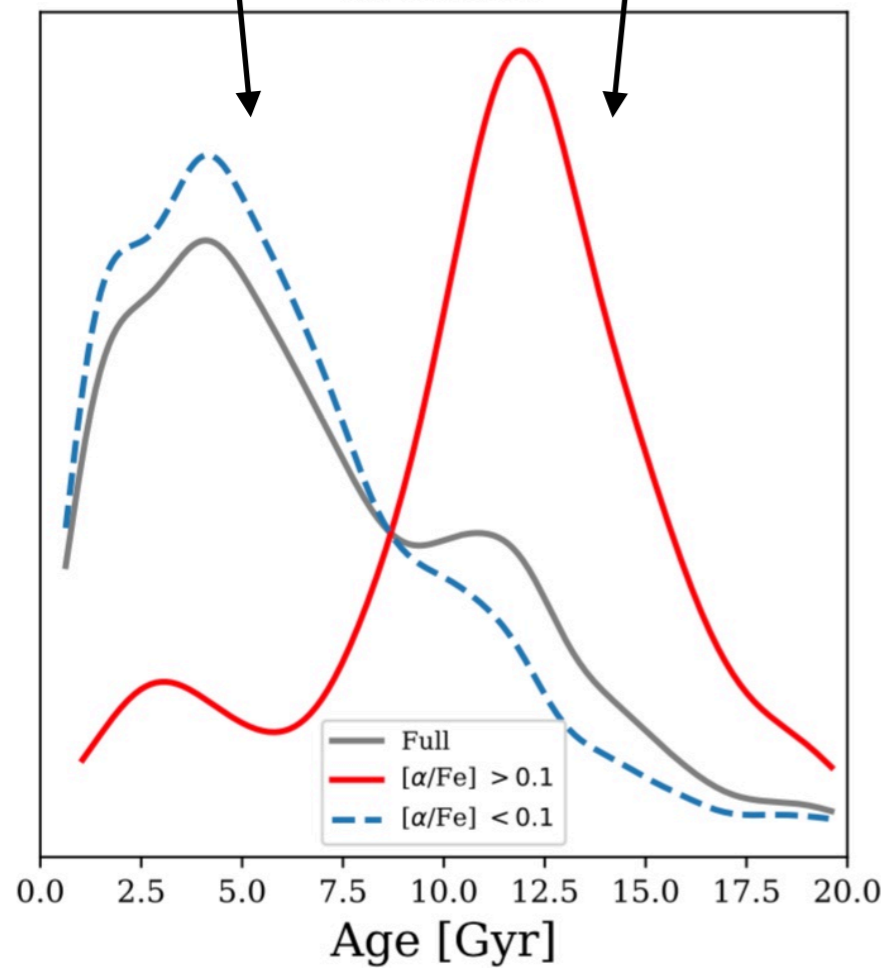
see also Silva Aguirre et al. (2018)  
and talk by Jane Lin tomorrow

thin

thick

APOKASC

K2 HQ



all distributions are normalised to equal area

# Vertical age structure beyond Kepler

Rendle et al. (submitted)

thin

thick

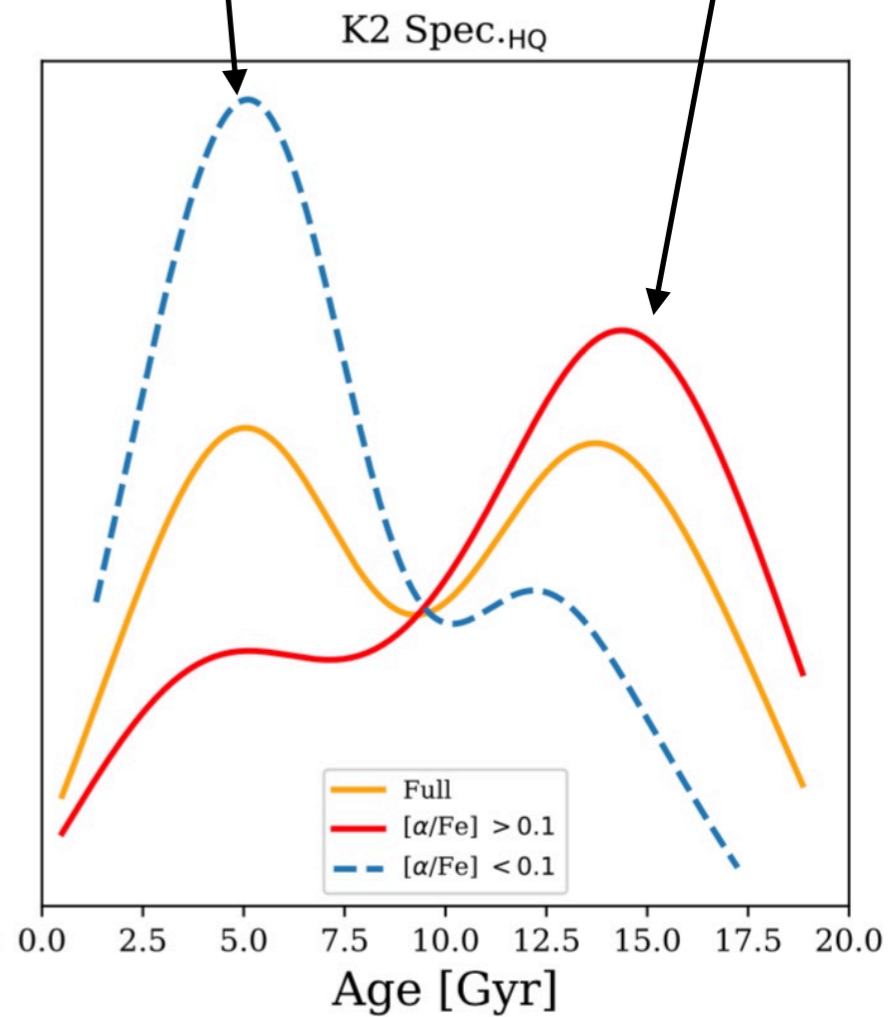
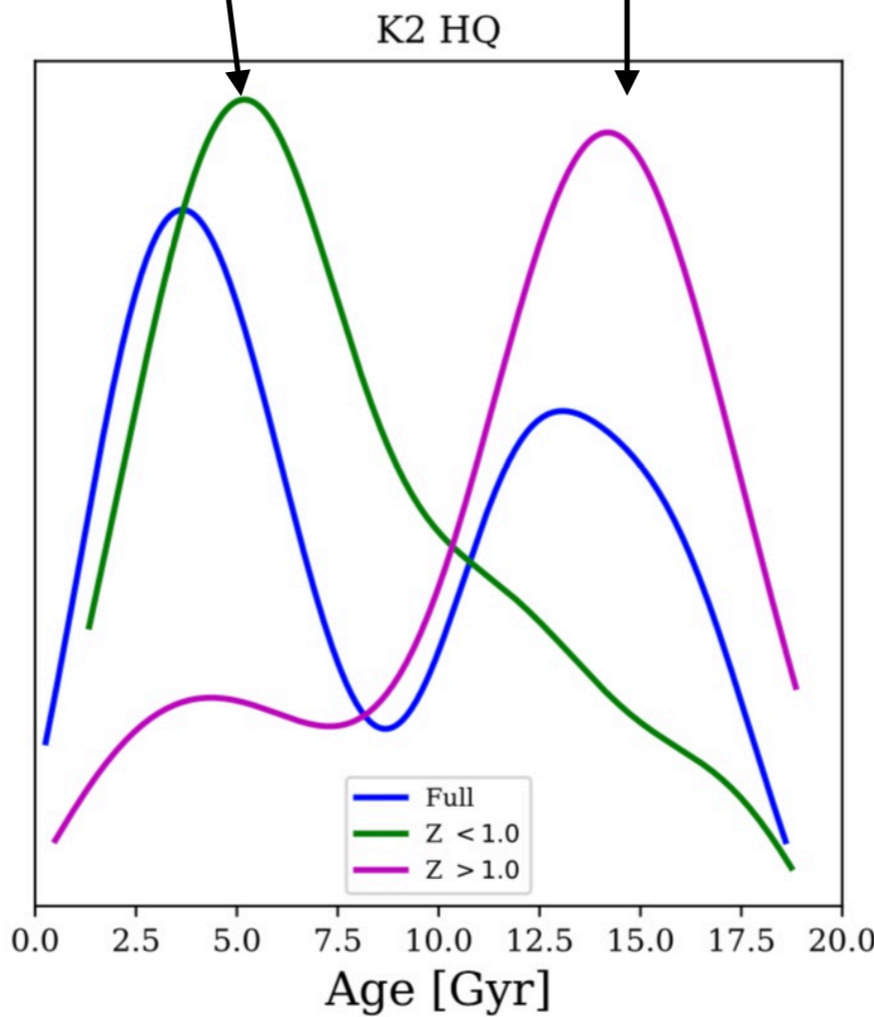
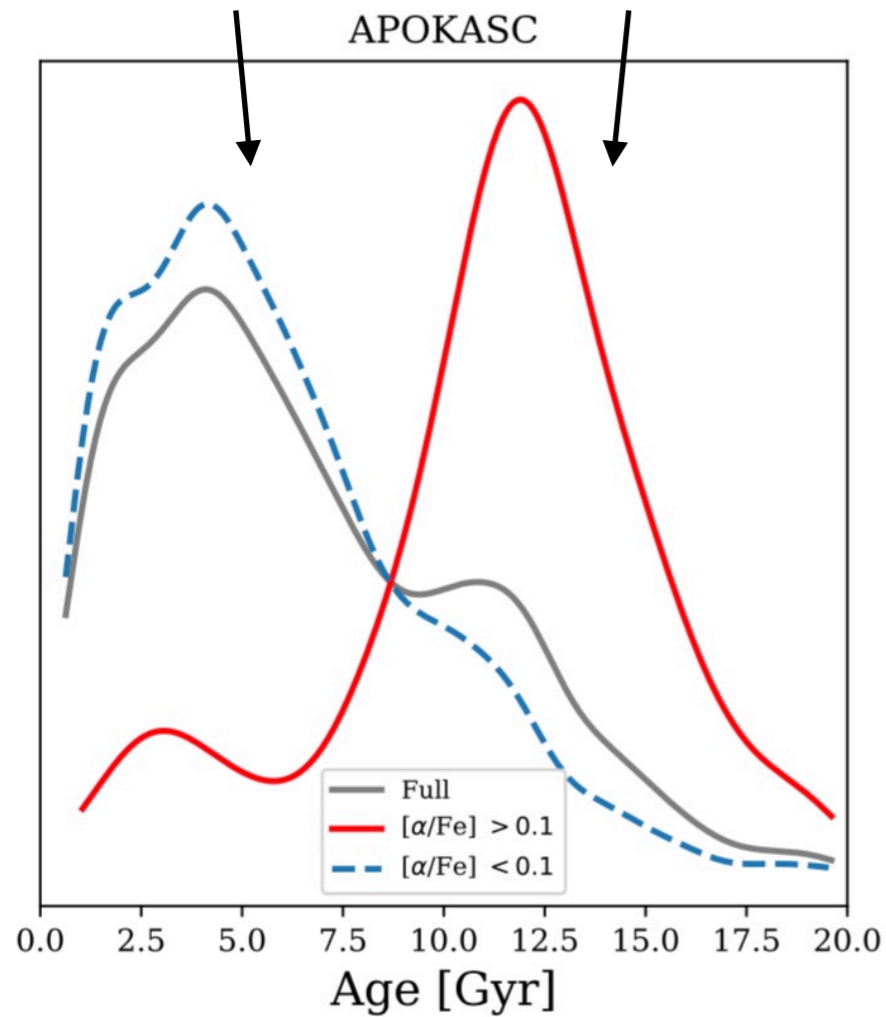
see also Silva Aguirre et al. (2018)  
and talk by Jane Lin tomorrow

thin

thick

thin

thick



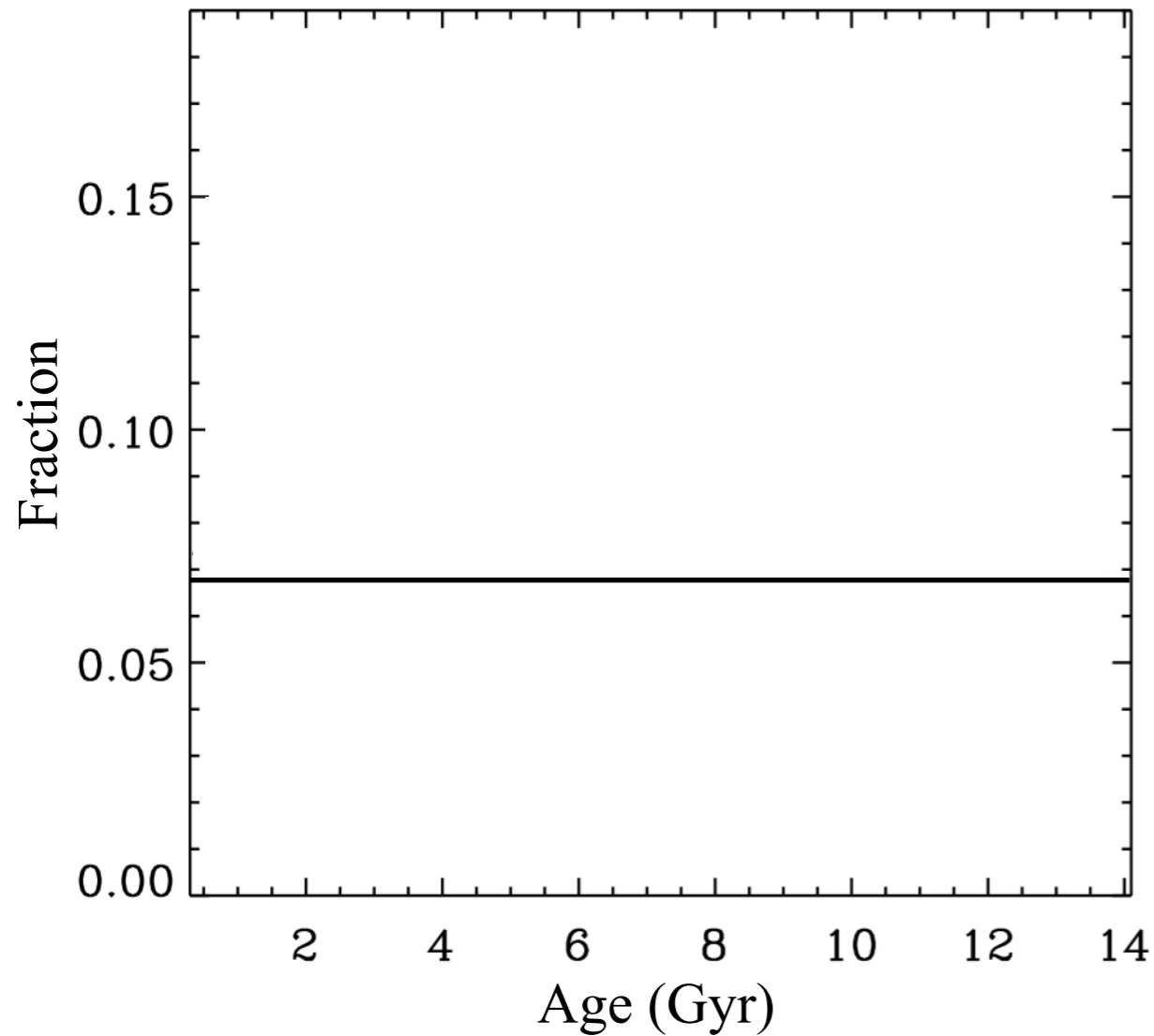
all distributions are normalised to equal area



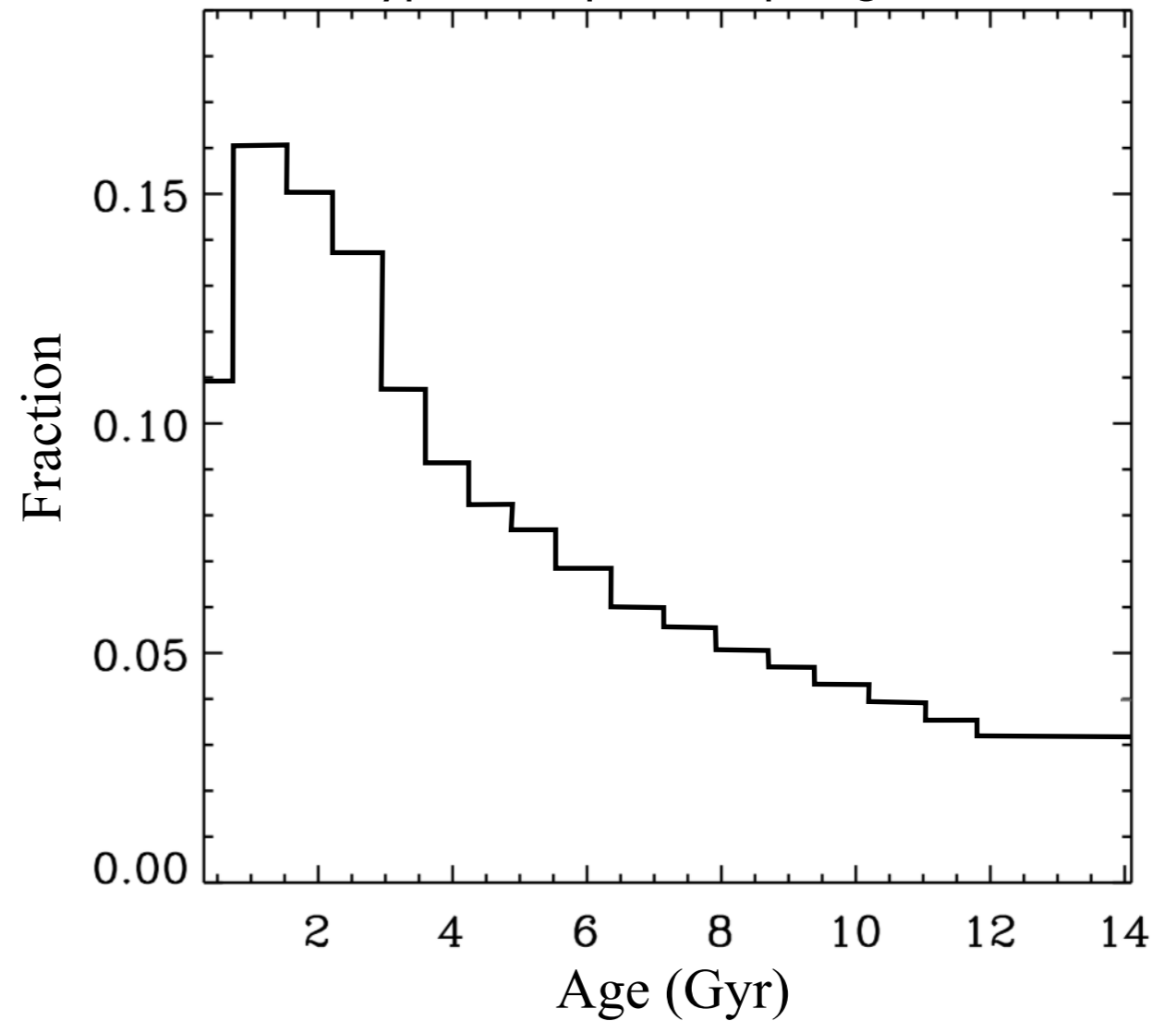
# Distribution of stellar ages

heavily biased by target selection effects

constant SFR



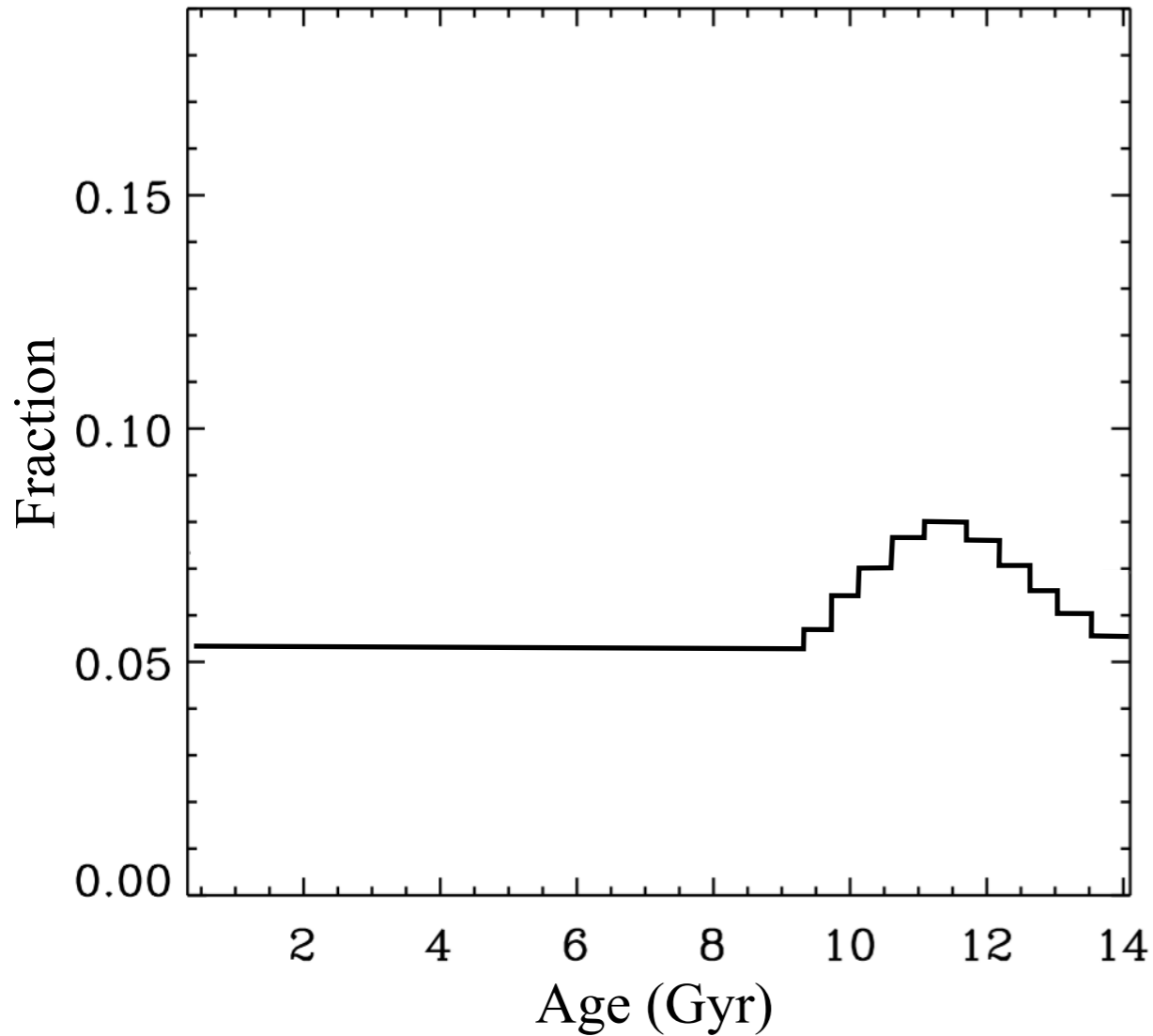
typical sample of Kepler giants



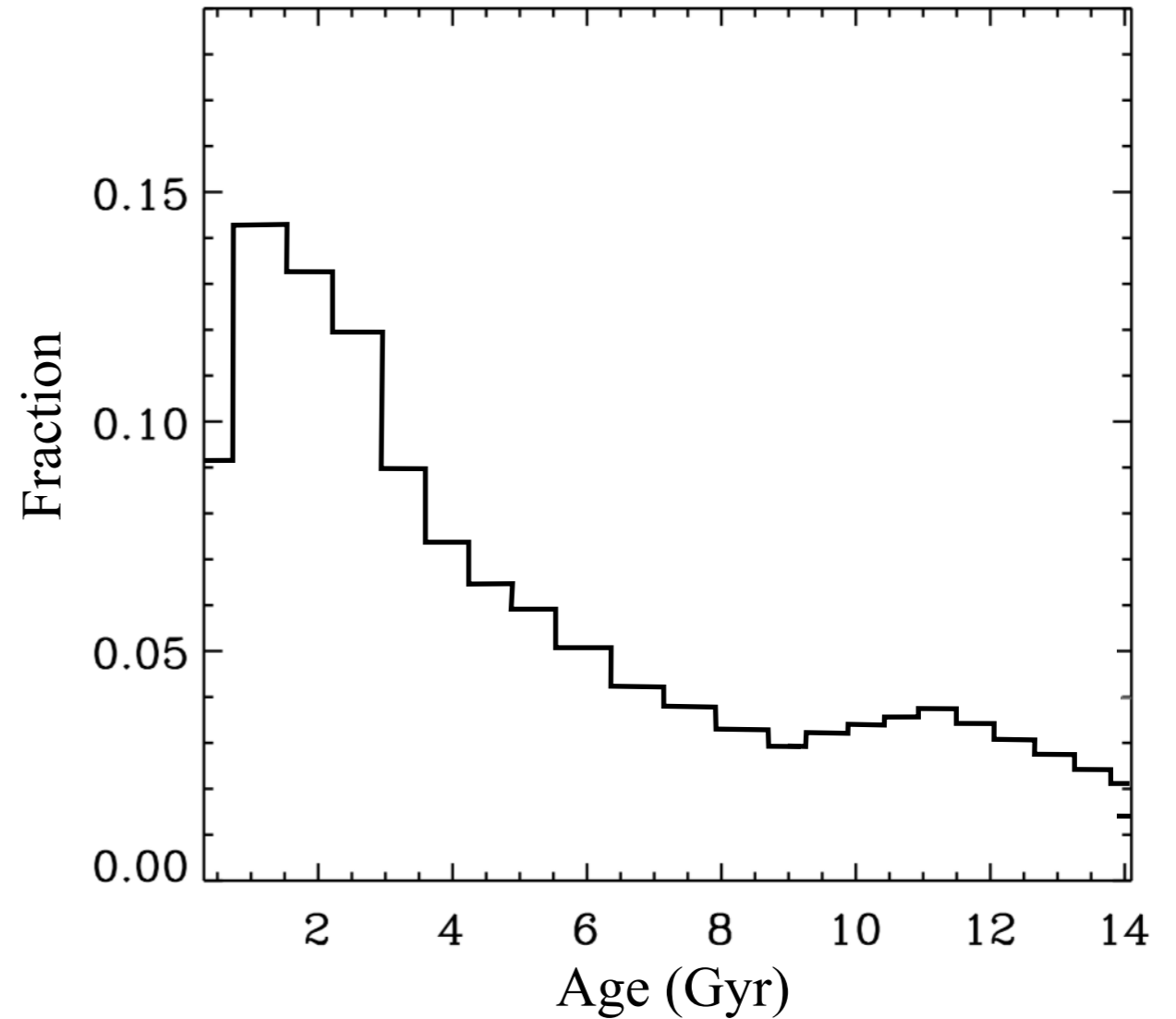
# Distribution of stellar ages

heavily biased by target selection effects

constant SFR + burst at ~11 Gyr



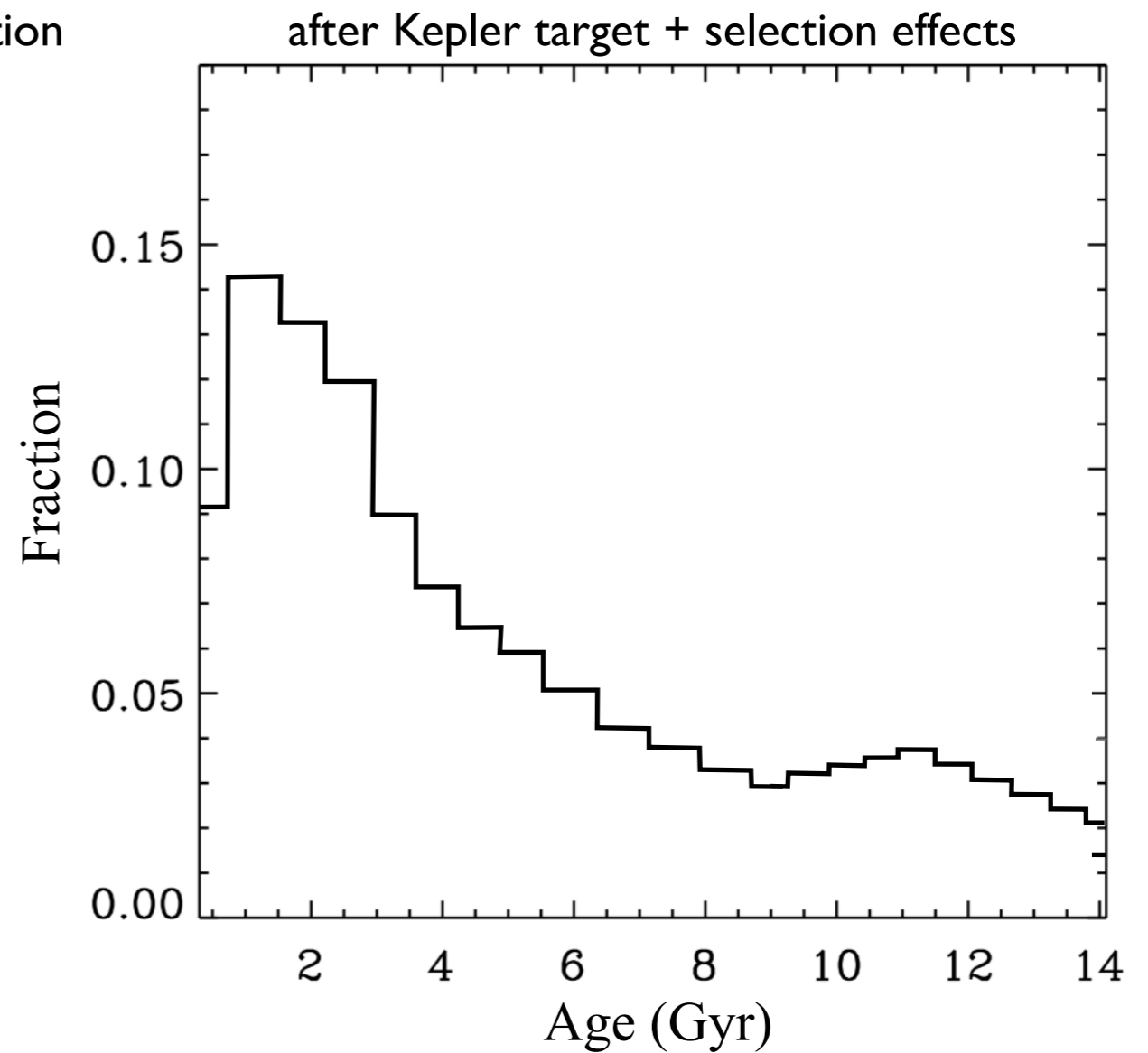
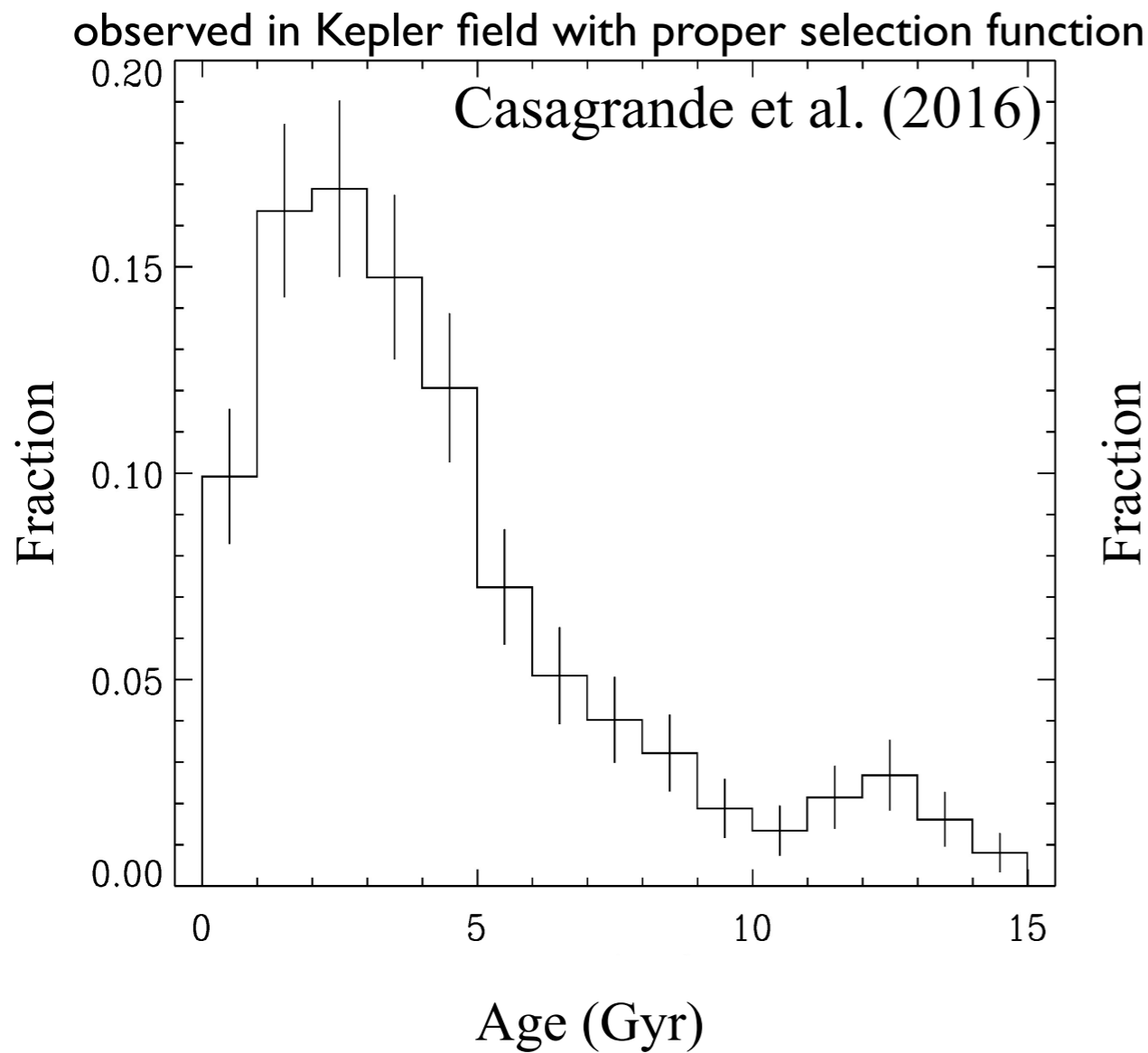
after Kepler target + selection effects





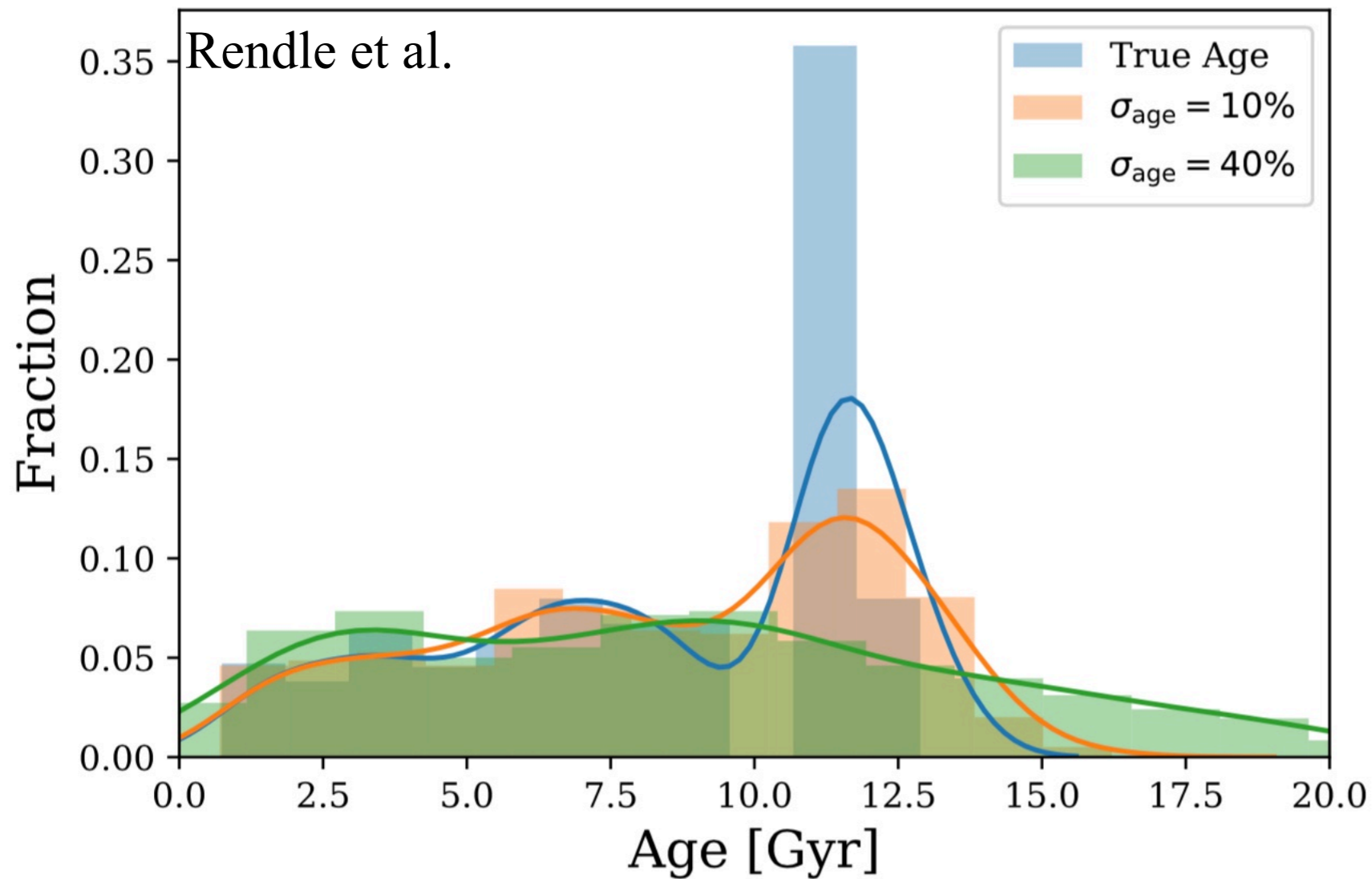
# Distribution of stellar ages

heavily biased by target selection effects



# Distribution of stellar ages

smoothed by uncertainties

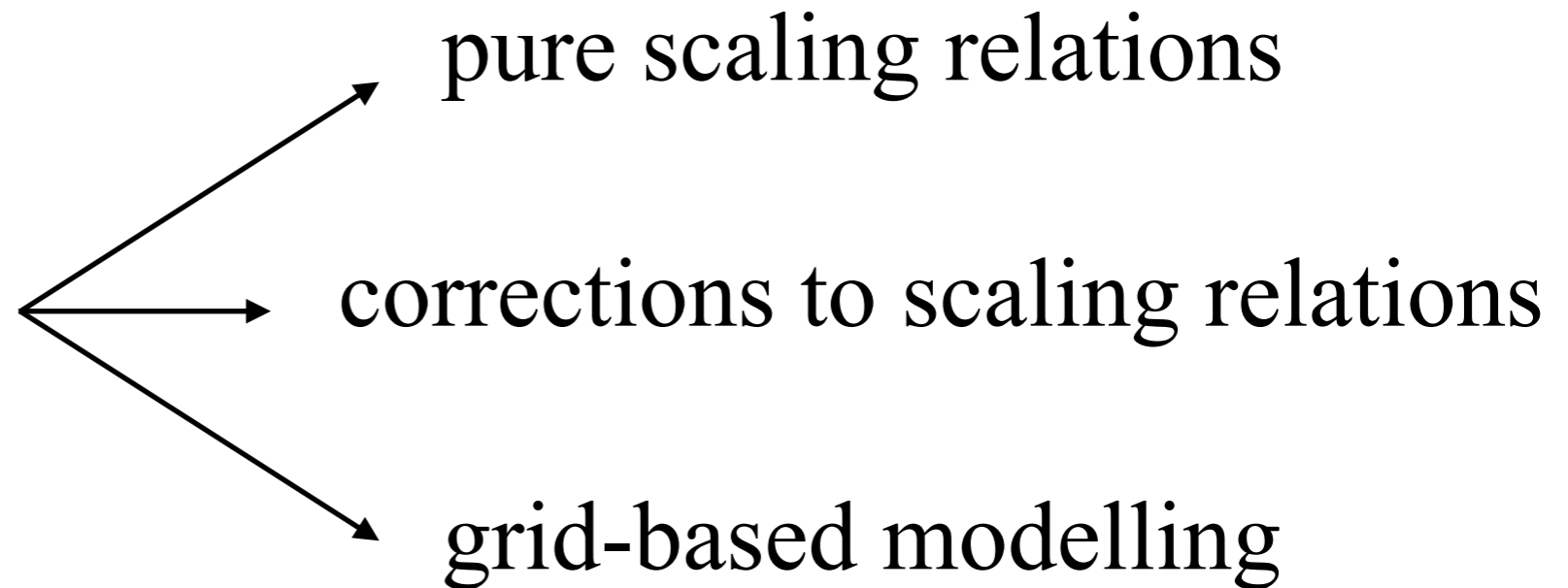


Age distribution from a synthetic Milky Way model (blue) once different age uncertainties are applied.



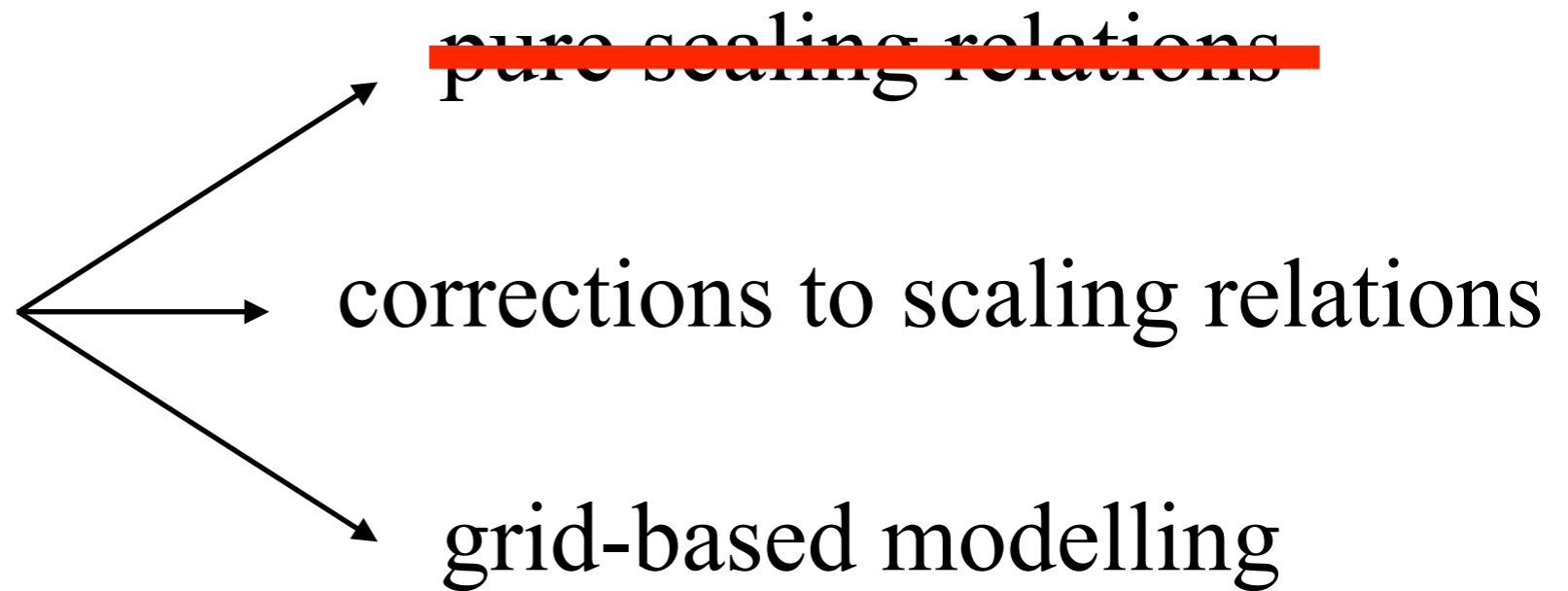
# Asteroseismology & better stellar ages

Asteroseismic ages  
for solar-like  
oscillators



# Asteroseismology & better stellar ages

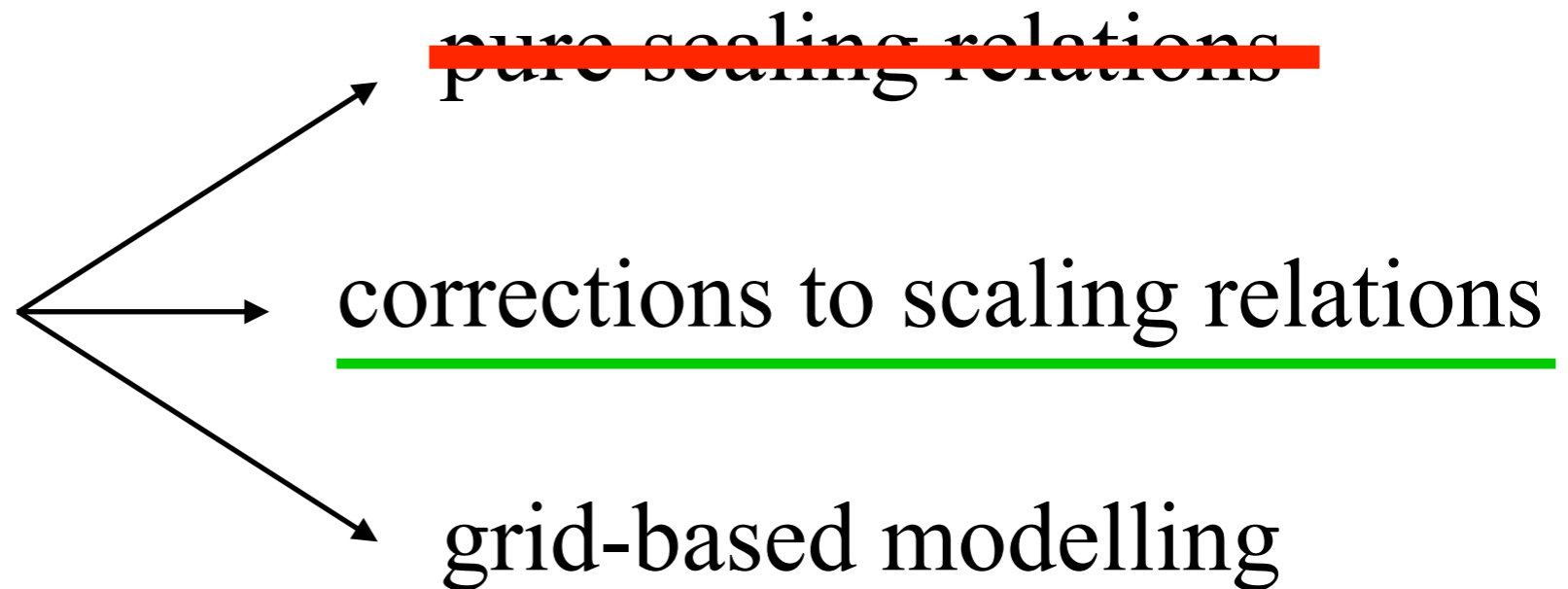
Asteroseismic ages  
for solar-like  
oscillators





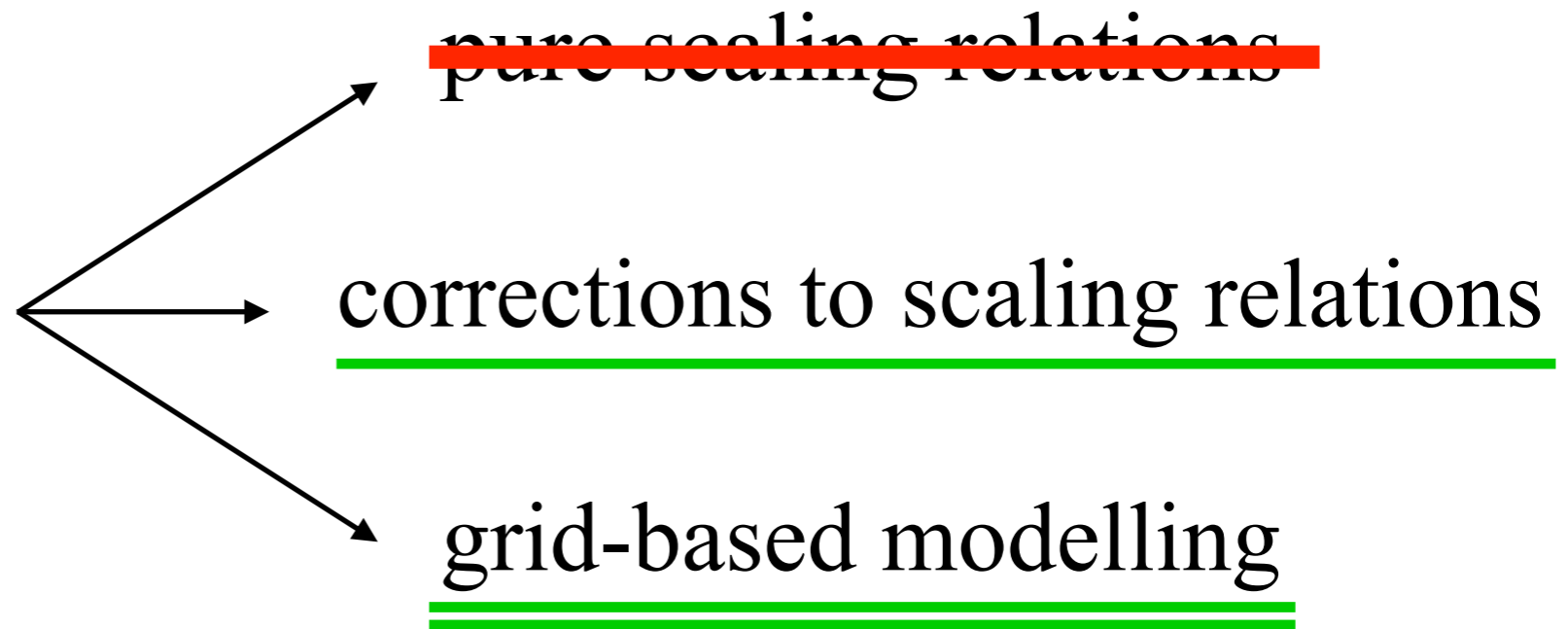
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Asteroseismic ages  
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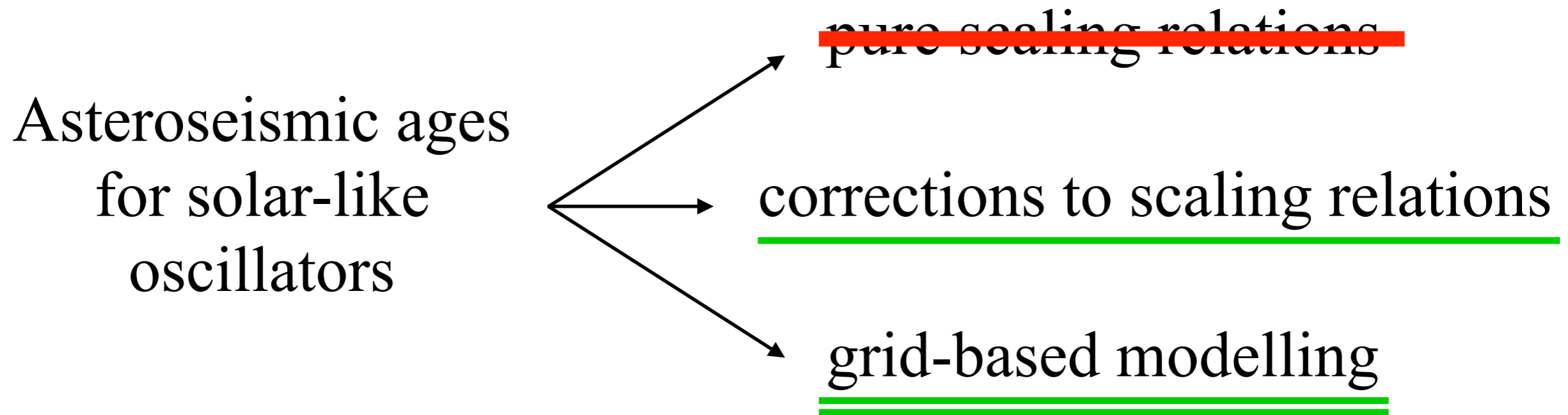
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Asteroseismic ages  
for solar-like  
oscillators



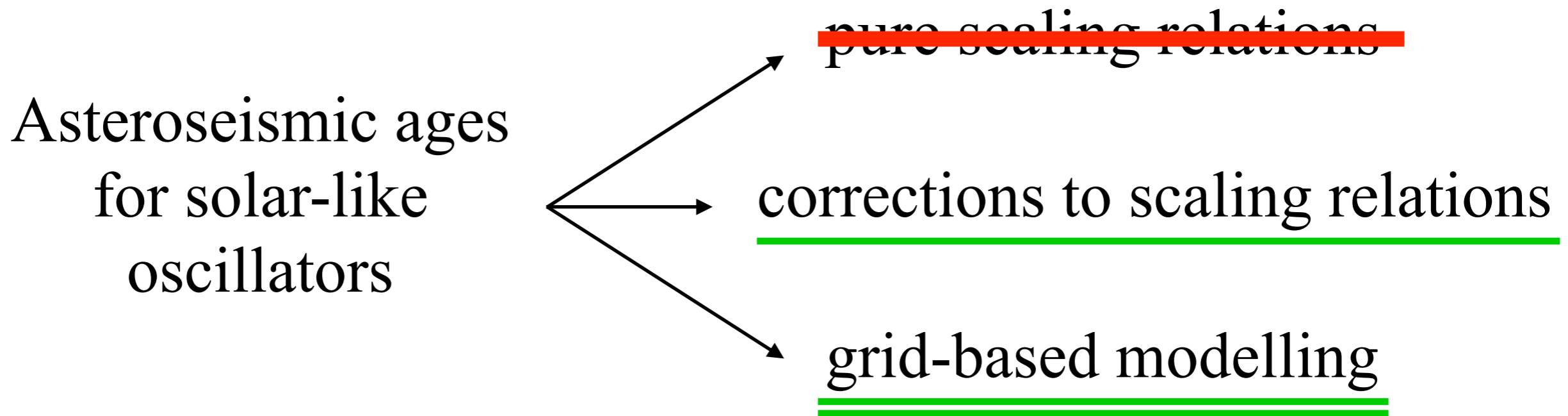


# Asteroseismology & better stellar ages



Age uncertainties around 30%

# Asteroseismology & better stellar ages



Age uncertainties around 30%

Good enough to start seeing major events/epochs in the history of the Milky Way. However modelling of target selection effects is as important as having good ages.